

Self-Organized Flocking with a Heterogeneous Mobile Robot Swarm

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Abstract

In this paper, we study self-organized flocking in a swarm of behaviorally heterogeneous mobile robots: aligning and non-aligning robots. Aligning robots are capable of agreeing on a common heading direction with other neighboring aligning robots. Conversely, non-aligning robots lack this capability. Studying this type of heterogeneity in self-organized flocking is important as it can support the design of a swarm with minimal hardware requirements. Through systematic simulations, we show that a heterogeneous group of aligning and non-aligning robots can achieve good performance in flocking behavior. We further show that the performance is affected not only by the proportion of aligning robots, but also by the way they integrate information about their neighbors as well as the motion control employed by the robots.

INTRODUCTION

Flocking is the cohesive and aligned motion of a group of individuals along a common direction. All studies about flocking within computer science and robotics root back to the seminal work of Reynolds (1987). He was the first to simulate flocking of birds based on three behaviors: *separation* — individuals try to keep a minimum distance between their neighbors, *cohesion* — individuals try to stay together with their neighbors, and *alignment* — individuals try to match their velocities to the average speed of their neighbors. The vast majority of the studies about flocking assume that all the robots in the swarm are behaviorally identical and exploit the three behaviors described above.

In this paper, we consider flocking in a behaviorally heterogeneous swarm of robots. All robots in the swarm use the separation and the cohesion behavioral rule. However, only a fraction of the robots, which we call the *aligning* robots, uses the alignment behavior. The rest of the robots, which we call the *non-aligning* robots, do not use the alignment behavior.

We believe that studying heterogeneity in alignment in self-organized flocking is very important from the practical point of view. The alignment behavior is more demanding in terms of robotics hardware requirements than the separation and cohesion behaviors. In fact, it requires either an elaborate sensing device, through which robots can detect the

orientation of neighboring robots or, as explained in this paper, a communication device. Therefore, understanding if a swarm can achieve flocking with only a few aligning robots can support the design of swarms with minimal hardware requirements.

We conduct simulation-based experiments and we measure self-organized flocking performance in terms of the degree of group order, group cohesiveness and average group speed. With respect to these criteria, we found that the swarm achieves good flocking performance when the proportion of aligning robots is high. Conversely, this performance decreases as the proportion gets lower. To tackle this problem, we propose a new model of robot motion. In the new model, non-aligning robots modulate their forward speed, instead of moving at a fixed forward speed as the other robots.

The rest of the paper is organized as follows. In the next section, we present the related works in flocking, starting from studies in biology and then in robotics. We then introduce our heterogeneous flocking model, the robots and we explain how we implement flocking on the robots. Subsequently, we describe the experimental setup, the metrics and the results. Finally, we conclude the paper and propose future directions of research.

RELATED WORK

Flocking is a widely observed phenomenon in social animals (Camazine et al., 2001) such as locusts (Buhl et al., 2006), birds (Ballerini et al., 2007) or human beings (Dyer et al., 2008). Animal groups show a great diversity in their population due to the differences in age, morphology (Krause et al., 1998), nutritional state (Krause, 1993), personality (Michelena et al., 2010), and leadership status (Reebs, 2000) of the individuals. This diversity mainly results in behavioral differences among the individuals. Couzin et al. (2002) showed that behavioral differences between the individuals in a group change both the dynamics and the organization of the group. Subsequently, Couzin et al. (2005) conducted a seminal study about leadership in animal groups. They modeled a heterogeneous group of in-

dividuals of which only a few are aware of a target direction. They showed that the few informed individuals are able to move the whole group along the target direction. In Janson et al. (2005), the authors propose a model to explain how scout bees are able to direct large swarms of uninformed bees towards a new nesting site. Even when the proportion of scout bees is low, they are able to lead the swarm by flying through it at a slightly faster speed. Sayama (2009) presented the preliminary results obtained in simulation using the Swarm Chemistry framework. They studied the movement of a swarm consisting of two different chemical species, and found that a chaser-escaper relationship between the two different populations of agents is established. More recently, Diwold et al. (2011) showed how a swarm can still fly towards a common direction even when the agents are not all aligned, and when the location of the nesting site is not known with precision.

In robotics, most of the studies about flocking assume a homogeneous set of behaviorally equivalent individuals. One of the earliest studies in robotics was performed by Mataric (1994). She devised a set of “basis behaviors” to implement flocking in a group of robots: safe-wandering, aggregation, dispersion and homing. With the proposed set of behaviors, robots are able to move cohesively towards a homing direction. Kelly and Keating (1996), following a behavior-based approach, designed a leader-following behavior to realize flocking. Hayes and Dormiani-Tabatabaei (2002) proposed a flocking behavior having collision avoidance and alignment behaviors based on local range and bearing measurements. Spears et al. (2004) proposed a framework based on artificial physics. The robots were able to form a regular lattice structure using attraction/repulsion virtual forces and move along a direction indicated by a light source in the environment. Holland et al. (2005) proposed a flocking behavior for unmanned ground vehicles based on separation, cohesion and alignment behaviors. Turgut et al. (2008) proposed a flocking behavior based on separation/cohesion and alignment behaviors. They implemented this behavior in robots with limited sensing capabilities and conducted a systematic study on the effect of sensing noise in heading measurement on flocking. In a recent study, Moslinger et al. (2009) proposed a flocking behavior for robots with limited sensing capabilities. It is based on only attraction and repulsion behaviors. By adjusting the sizes of attraction and repulsion zones, they achieved flocking for a small group in a constrained environment.

Other works in robotics considered a group of behaviorally heterogeneous robots. Momen et al. (2007) studied flocking with a heterogeneous robotic swarm inspired by mixed-species foraging flocks of birds (Graves and Gotelli, 1993). Using simulations, they showed some aspects of mixed-species flocking, such as behavioral differences in their attraction and repulsion rules. Çelikkanat and Şahin (2010), inspired by Couzin et al. (2005) extended the flock-

ing behavior proposed by Turgut et al. (2008) and created a heterogeneous robot swarm by informing some of the robots about a target direction. Recently, in another follow-up study, Ferrante et al. (2010) introduced a new communication strategy to improve flocking performance in case of both static and changing target directions.

To the best of our knowledge, most of the studies in swarm robotics about self-organized flocking have not considered diversity in alignment capabilities.

METHOD

We follow a design method based on the artificial physics framework introduced by Spears et al. (2004). According to this method, robots exert virtual forces on each other. The swarm consists of aligning and non-aligning robots. Aligning robots are subject to the following virtual forces

$$\mathbf{f} = \alpha_1 \mathbf{p} + \beta_1 \mathbf{h},$$

whereas for the non-aligning robots the virtual force is computed as

$$\mathbf{f} = \alpha_2 \mathbf{p}.$$

We define \mathbf{p} as the *proximal control vector* and \mathbf{h} as the *alignment control vector*. The proximal control vector \mathbf{p} accounts for attraction and repulsion rules for keeping the robot together with its neighbors and to avoid collisions.

The alignment control vector \mathbf{h} is used to make the aligning robots match the average heading direction of its neighboring aligning robots. The parameters α_1 , β_1 and α_2 are used to adjust the contribution of the corresponding vectors.

Proximal control

Let m_p denote the number of neighbors of a robot within a range D_p . Let also d_i and ϕ_i denote the relative range and bearing of the i^{th} neighbor, respectively. The proximal control vector \mathbf{p} is given by:

$$\mathbf{p} = \sum_{i=1}^{m_p} p_i(d_i) e^{j\phi_i}.$$

p_i is calculated as a function of d_i using a force function derived from the Lennard-Jones potential function, which results in the formation of regular structures as shown in Hettiarachchi and Spears (2009):

$$p_i(d_i) = 12\epsilon \left[\frac{d_{des}^{12}}{d_i^{13}} - \frac{d_{des}^6}{d_i^7} \right].$$

The parameter ϵ determines the strength of the attractive and repulsive force, and d_{des} is the desired distance between the robots.

Alignment control

Let θ_0 denote the orientation of a given robot. Furthermore, let m_a denote the number of aligning robots within the range D_a of this robot, and $\theta_i, i \in \{1, \dots, m_a\}$ their orientation. All orientations are expressed in the body-fixed reference frame of the robot under consideration¹. The robot calculates the alignment control vector, that is, the average orientation of the m_a robots, including its own:

$$\mathbf{h} = \frac{\sum_{i=0}^{m_a} e^{j\theta_i}}{\left\| \sum_{i=0}^{m_a} e^{j\theta_i} \right\|},$$

where $\|\cdot\|$ denotes the norm of a vector.

Motion control

We present two motion control rules. The two rules differ in the way the forward speed u and the angular speed ω are determined. The first rule is denoted as *constant forward speed motion control* (henceforth CMC). In CMC, robots are always moving at a constant forward speed, but can change their angular speed. According to the second rule, denoted as *variable forward speed motion control* (henceforth VMC), robots move not only at a variable angular speed but also at a variable forward speed.

CMC: The forward speed is kept constant at

$$u = U.$$

The angular speed is proportional to the angular component of the total force \mathbf{f} . Hence, it ignores the magnitude $\|\mathbf{f}\|$ of the force:

$$\omega = K \angle \mathbf{f}.$$

VMC: First, let $\mathbf{f}_x = \|\mathbf{f}\| \cos(\angle \mathbf{f})$ and $\mathbf{f}_y = \|\mathbf{f}\| \sin(\angle \mathbf{f})$ denote the projection of the total force \mathbf{f} on the x -axis and y -axis of the robot body-fixed reference frame respectively. Accordingly, the forward speed u is directly proportional to the x component of the total force and the angular speed ω is directly proportional to the y component of the force. Hence:

$$\begin{aligned} u &= K_1 \mathbf{f}_x \\ \omega &= K_2 \mathbf{f}_y. \end{aligned}$$

K, K_1, K_2 are constants, whose values are given in Table 1.

In this work, we consider and study two different cases in which we vary the motion control rule applied to the non-aligning robots. In the first case, referred as the *CMC-CMC*

¹In our study, we define two reference frames, both of which use the right-hand convention. One is the reference frame common to all of the robots, which is available due to the light source. The other is the body-fixed reference frame specific to each robot. The body-fixed reference frame is fixed to the center of a robot: its x -axis points to the front of the robot and its y -axis is coincident with the rotation axis of the wheels.

case, all robots share the same motion control rule, that is, CMC. In the second case, referred as the *CMC-VMC* case, aligning robots use CMC, whereas non-aligning robots use VMC.

FLOCKING WITH ROBOTS

In this study, the swarm is composed of simulated versions of the foot-bot robot developed by Bonani et al. (2010). The foot-bot is a differentially-driven mobile robot with the following sensors and actuators: i) A light sensor used to measure the orientation of robot (θ_0) with respect to a light source present in the environment perceived by all robots. ii) A range and bearing sensing and communication device (henceforth called RAB), with which a robot can communicate with its neighbors and perceive their range and bearing measurements (Roberts et al., 2009). iii) Two wheels actuators, that are used to control independently the left and right wheels speed of the robot.

To achieve proximal control with the foot-bot the RAB is used for measuring the relative range and bearing d_i and ϕ_i of the i^{th} neighbor. For achieving alignment control, we use communication to simulate orientation sensing as in Turgut et al. (2008). In particular, each aligning robot sends its orientation, expressed in the global reference frame, using the communication unit present in the RAB. At the same time, it receives the orientation θ_i of its i^{th} neighboring aligning robot. It transforms this angle into its body-fixed reference frame. In this way, we are able to simulate a robot sensing the orientation of its neighboring aligning robots.

To achieve motion control, we first limit the forward speed within $[0, U_{max}]$, and the angular speed within $[-\Omega_{max}, \Omega_{max}]$. We then use the differential drive model used in Turgut et al. (2008) to convert the forward speed u and the angular speed ω into the linear speeds of the left (N_L) and right (N_R) wheel:

$$N_L = \left(u + \frac{\omega}{2} l \right),$$

$$N_R = \left(u - \frac{\omega}{2} l \right),$$

where l is the distance between the wheels.

The values of the constants that we used in our experiments are given in Table 1.

EXPERIMENTS

We execute simulation-based experiments with a swarm of foot-bots using the ARGoS simulator (Pinciroli et al., 2011), an open-source², plug-in based, multi-physics engine simulator.

²<http://iridia.ulb.ac.be/argos/>

Variable	Description	Value(s) / Range
N	Number of robots	{25, 100}
ρ	Prop. of aligning robots	{0.4, 0.8}
β_1/α_1	Align. robots parameters	{1, 2, 4, 6, 8, 10}
α_2	Non align. robots parameter	{1, 2, 4, 6, 8, 10}
U	Maximum forward speed	1.5 cm/s
K	CMC angular gain	0.5 1/s
K_1	VMC linear gain	0.25 s/kg
K_2	VMC angular gain	0.1 s/(kg · m)
l	Inter-wheel distance	0.1 m
U_{max}	VMC max forward speed	20 cm/s
Ω_{max}	VMC max angular speed	$\pi/2$ rad/s
ϵ	Strength of pot. function	0.5
d_{des}	Inter-robot distance	0.6 m
σ	Amount of noise	0.1
T	Experiment duration	600 secs

Table 1: Experimental values or range of values for all constants and variables

Experimental setup

At the beginning of each experiment, N mobile robots are randomly placed (position and orientation-wise) with a proportion $\rho \in [0, 1]$ of aligning robots. The density of robots is kept fixed and equal to 6 robots per square meter on a square shaped area. A light source is placed at a fixed position in the environment, far away from the swarm, to provide the common reference frame.

In the experiments, noise is added to the orientation measurement and the angle of the proximal control vector. Noise is modeled as a uniformly distributed random variable within the range $[-\sigma\pi, \sigma\pi]$.

We conduct experiments considering the two different cases of motion control.

CMC-CMC In this case, all robots use CMC. Here, we study the effect of the ratio $\frac{\beta_1}{\alpha_1}$, and we do not change α_1 and β_1 independently, since CMC does not utilize the magnitude of \mathbf{f} , but only its angular component. As such, multiplying both α_1 and β_1 with the same constant value will produce no difference in the robot motion. For the same reason, α_2 does not effect the robot motion.

CMC-VMC In this case, aligning robots use CMC whereas non-aligning robots are using VMC. For the non-aligning robots, the magnitude of \mathbf{f} plays a role in their motion. Thus, additionally to the effect of changing $\frac{\beta_1}{\alpha_1}$ of the aligning robots, we study the effect of changing α_2 of the non-aligning robots.

We show the results in heterogeneous self-organized flocking with medium ($N = 25$) and large ($N = 100$) swarm sizes and with low ($\rho = 0.4$) and high ($\rho = 0.8$) proportions

of aligning robots. We study the effect of changing the ratio $\frac{\beta_1}{\alpha_1} \in \{1, 2, 4, 6, 8, 10\}$ and, for the heterogeneous case, we also study the effect of changing $\alpha_2 \in \{1, 2, 4, 6, 8, 10\}$, but we report here only the results obtained with the best case, that is, $\alpha_2 = 10$ (refer to Stranieri et al. (2011) for the complete set of results). In our supplementary page (Stranieri et al., 2011), we also report the flocking performance as a function of $\rho \in \{0.2, 0.4, 0.6, 0.8, 1.0\}$.

For each experimental setting, we execute R runs and report median and interquartile range of the results. The duration of one run is T simulated seconds.

We study how the heterogeneous flocking performance is influenced by: i) the way robots implement their motion (CMC-CMC motion versus CMC-VMC motion), ii) the parameters that affect the strength of the proximal control vector and of the alignment control vector, that is, $\frac{\beta_1}{\alpha_1}$ and α_2 , and iii) the ratio of aligning robots ρ .

We also experiments in the VMC-VMC case, but we didn't obtain any positive results, even with $\rho = 1$.

Metrics

In this study, we are interested in having a swarm of robots that move cohesively as a single group. Furthermore, the swarm should be aligned towards the same direction and move towards it as fast as possible. We use three metrics to measure the degree of attainment of these objectives: order, group cohesion and rescaled group speed.

Order: The order metric ψ measures the angular order of the robots (Vicsek et al., 1995), $\psi \approx 1$ when the group shares a common heading and $\psi \ll 1$ when each robot is pointing in a different direction. The order is defined as:

$$\psi = \frac{1}{N} \left\| \sum_{i=1}^N e^{j\theta_i} \right\|.$$

Group cohesion: To measure group cohesion ξ , we determine the number of groups g present at the end of each experiment (Couzin et al., 2005). Group cohesion is computed as:

$$\xi = 2 - \min(2, g).$$

and therefore takes values in $\{0, 1\}$.

Rescaled Group speed: We calculate the average group speed as:

$$s = \left\| \frac{\mathbf{c}_T - \mathbf{c}_0}{T} \right\|,$$

where \mathbf{c}_T and \mathbf{c}_0 are the position of the center of mass of the swarm at the end and at the beginning of the experiment, respectively. We then rescale the average group speed:

$$s_r = \frac{s}{U},$$

where U is the maximum forward speed of CMC.

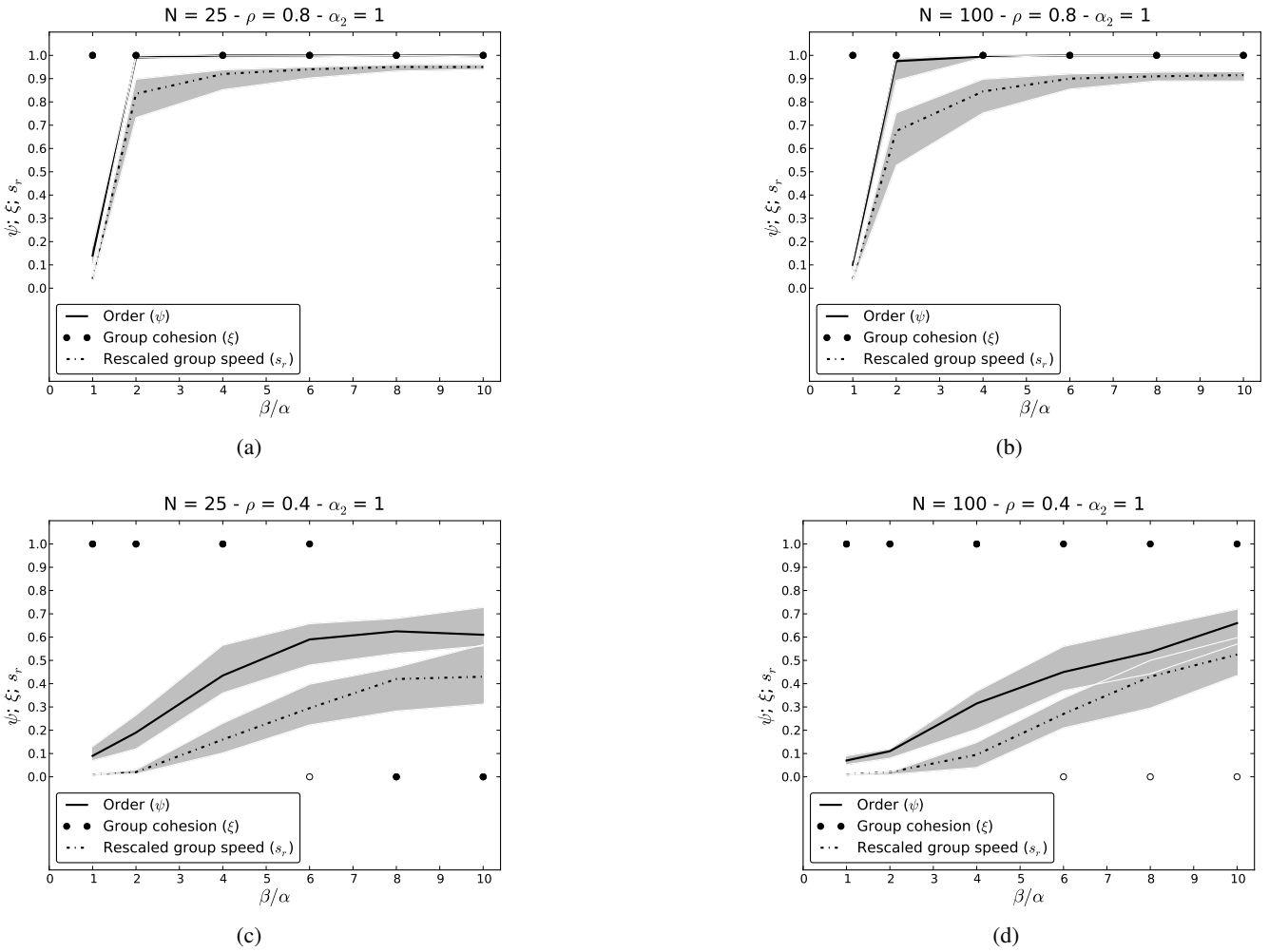


Figure 1: CMC-CMC case experiments for varying swarm size ($N \in \{25, 100\}$) and ratio of aligning robots ($\rho \in \{0.4, 0.8\}$). Thick lines show the median values, whereas the gray areas show the 25% and the 75% interquartile range of the data. For group cohesion, filled circles correspond to median values and empty circles to the 25% percentile score of the data.

Results in the CMC-CMC case

The experimental results for CMC-CMC case are depicted in Figure 1. We first focus on the $\rho = 0.8$ case, for both $N = 25$ (Figure 1a) and $N = 100$ (Figure 1b). Results show that the swarm is cohesive in most runs. However, order and speed are high only when $\frac{\beta_1}{\alpha_1} \geq 2$. Furthermore, while order is high at different values of the ratio $\frac{\beta_1}{\alpha_1}$, speed increases with increasing values of $\frac{\beta_1}{\alpha_1}$, until it saturates at around $\frac{\beta_1}{\alpha_1} = 6$. This shows that, when the alignment control vector is higher, robots tend to move faster. This is explained by the fact that the alignment control vector is more stable, over time, than the proximal control vector. Thus, the higher the weight of the alignment control vector, the more the robots tends to move forward rather than to turn. This allows the swarm to move faster, until speed saturates at the

maximum forward speed U .

When the proportion of aligning robots is $\rho = 0.4$, performance gets sensibly worse (Figures 1c and 1d). In both cases ($N = 25$ and $N = 100$), we observe two possible outcomes: for small values of the ratio $\frac{\beta_1}{\alpha_1}$, the swarm remains cohesive, but does not move. This happens because the relative contribution of the alignment control vector is not enough for the aligning robots to pull the entire swarm towards the agreed goal direction. For larger values of the ratio $\frac{\beta_1}{\alpha_1}$, group speed and order get higher. However, in at least 25% of the runs, the swarm splits. This happens because, in those runs, clusters of non-aligning robots are present. Since the motion of these robots is governed only by the proximal control vector, they are not able to match the higher speed of the aligning robots since they tend to turn more rather than to move forward, thus they remain disconnected from the group.

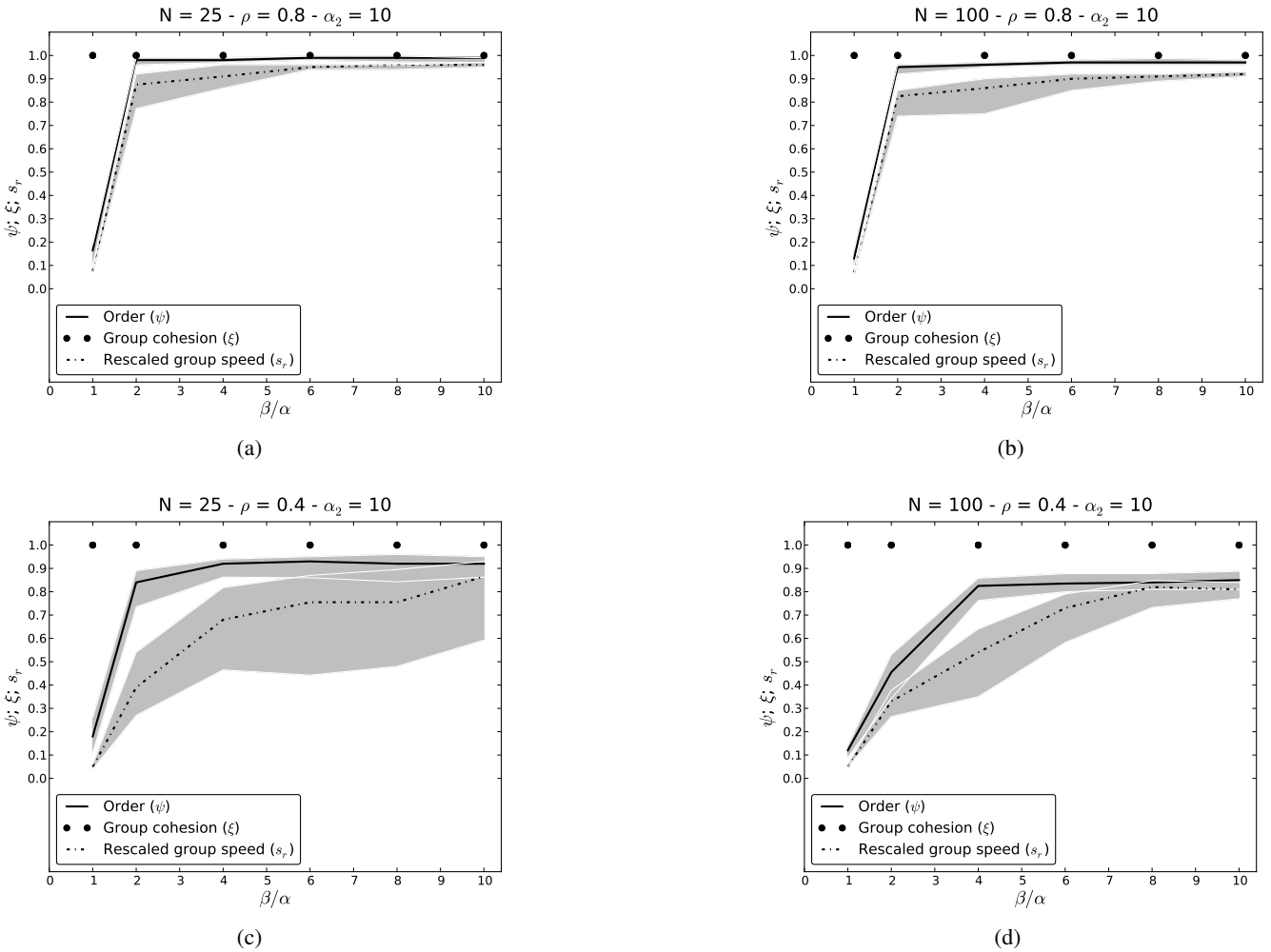


Figure 2: CMC-VMC case experiments for varying swarm size ($N \in \{25, 100\}$) and ratio of aligning robots ($\rho \in \{0.4, 0.8\}$). Thick lines show the median values, whereas the gray areas show the 25% and the 75% interquartile range of the data. For group cohesion, filled circles correspond to median values and empty circles to the 25% percentile score of the data.

In Stranieri et al. (2011), we also report the performance as function of ρ . We consider the case $\frac{\beta_1}{\alpha_1} = 10$, as it generally provides the best overall results. As shown in Stranieri et al. (2011), the flocking performance is acceptable in terms of the metrics used for $\rho \geq 0.6$ in both cases $N = 25$ and $N = 100$.

Results in the CMC-VMC case

In the CMC-VMC case, results with $\rho = 0.8$ (Figures 2a and 2b), are similar to the results obtained, with the same ratio, in the CMC-CMC case. The results with $\rho = 0.4$ are much better in the CMC-VMC case (Figures 2c and 2d) with respect to the CMC-CMC case (Figures 1c and 1d). With both swarm sizes we have that, when $\frac{\beta_1}{\alpha_1} > 2$, the swarm is able to effectively flock together at the cost of a reduced speed.

In Stranieri et al. (2011), we also report the flocking performance as a function of ρ for $\frac{\beta_1}{\alpha_1} = 10$ and $\alpha_2 = 10$. Differently from the CMC-CMC case, in the CMC-VMC case the performance of flocking degrades more gracefully as the proportion of non-aligning robots decreases.

The improved capability of the swarm to stay together is due to the advantage of using VMC in the non-aligning robots. In fact, non-aligning robots are able to respond to the high variations in the proximal control vector much more when they can also change their forward speed. As such, they are also able to stay together with the aligning robots, both when they are alone and when they are in small or big clusters. Finally, the reduced speed and the high variation of speed among runs is due to the following fact. In presence of a low proportion of aligning robots, we observed that the group heading direction is stable over short periods

of time but changes over long periods of time due to the disturbances caused by the non-aligning robots. This results in a non-linear trajectory executed by the entire swarm, which is different for each run. Since the rescaled group speed is computed assuming a linear trajectory, this measurement has large variation in the total displacement changes from run to run.

CONCLUSIONS AND FUTURE WORKS

In this paper, we studied self-organized flocking in a swarm composed of behaviorally heterogeneous mobile robots. The swarm is composed of aligning robots, which are able to agree on a common heading direction, and non-aligning robots which lack this capability. We furthermore propose a new model for achieving motion in self-organized flocking. According to this model, aligning robots only change their angular speed, whereas non-aligning robots change both their forward and their angular speed.

We study the performance in terms of group alignment order, cohesiveness and speed. Results show that self-organized flocking is also possible when some individuals in the swarm lack the capability to agree on a common direction. More in particular, we showed that: i) a higher proportion of aligning robots always corresponds to a better performance; ii) performance is affected by the relative contribution of alignment and proximal control, and iii) for smaller proportions of aligning robots, flocking is possible only when the non-aligning robots also change their forward speeds.

Possible directions for future work are the following: First, we plan to study energy efficiency within the same framework of study. In particular, the use of a heterogeneous group of aligning and non-aligning robots poses a trade-off between efficiency of the motion and energy utilized. In fact, we observed that, in order for the swarm to hold cohesiveness, the non-aligning robots spend a lot of energy to vary their speed more reactively. Second, we would like to study the correlation between spatial aspects of the swarm composition. In particular, we would like to study whether particular configurations (i.e., topology, connectivity, ...) have different effects on the flocking performance. Third, we plan to perform experiments involving two different types of real robots.

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