Global anisotropic phase velocity maps for fundamental mode surface waves between 40 and 150 s

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Accepted 2003 February 10. Received 2003 February 5; in original form 2002 August 28

\section*{SUMMARY}

We constructed global phase velocity maps including azimuthal anisotropy. Azimuthal anisotropy is expanded on a basis of generalized spherical harmonics, which makes the calculation of path integrals of the phase velocity particularly simple. It is generally accepted that the major difficulty in such modelling is determining the strength of the anisotropy relative to the isotropy. We propose a technique which finds the optimum relative weighting of the anisotropic terms prior to inversion. It is clear from our analyses that phase data require azimuthal anisotropy. We further find that Love wave data do not require a $2\psi$ term, whereas Rayleigh wave data need $2\psi$ and $4\psi$ terms. The main effect of azimuthal anisotropy upon the isotropic maps is a loss of power in the highest spherical harmonic degrees, resulting in an overall lower lateral resolution compared with a purely isotropic inversion for the same number of recovered parameters. The correlation of $2\psi$ and $4\psi$ components at different periods is relatively high, indicating a shallow source for the azimuthal anisotropy. Overall, fast $2\psi$ Rayleigh directions agree well with absolute plate motions in the hotspot reference frame.

\textbf{Key words:} azimuthal anisotropy, inverse theory, phase velocity, surface waves, tomography.

\section*{INTRODUCTION}

It is now well established that the Earth’s uppermost mantle is anisotropic. The earliest evidence is the possibility of a discrepancy between the dispersion of Love and Rayleigh waves (Anderson 1961; Harkrider & Anderson 1962) and the azimuthal dependence of oceanic $P_n$ velocities (Hess 1964). Surface waves are particularly well suited to studying anisotropy since they carry information on the radial and azimuthal anisotropy of the upper mantle. Radial anisotropy was first observed when it was established that isotropic velocity models failed to explain simultaneously Love and Rayleigh wave dispersion data (Aki & Kaminuma 1963; McEvilly 1964). This is referred to as the Love–Rayleigh discrepancy and is an indirect observation of anisotropy. A directly observable manifestation of anisotropy is the azimuthal variation of phase velocities, first noticed by Forsyth (1975) in the Pacific Ocean. Since these pioneering studies, many more observations followed and detailed overviews may be found in Anderson (1989), Babuška & Cara (1991) and Montagner (1998). Radial and azimuthal anisotropy in surface waves are the result of the same underlying anisotropy of the Earth’s interior, and Montagner & Natário (1986) linked both together in a common mathematical framework. The theory, initially developed for a flat layered Earth, was later extended to a spherical Earth (Romanowicz & Snieder 1988; Larsen et al. 1998).

The necessity for radial anisotropy in the uppermost mantle has never been questioned in reference models (e.g. Dziewonski & Anderson 1981) or 3-D models (e.g. Natário et al. 1984; Ekström & Dziewonski 1998), while global azimuthal phase velocity maps have not been constructed since earlier efforts (e.g. Tanimoto & Anderson 1984, 1985; Montagner & Tanimoto 1990), despite a tremendous increase in high-quality measurements (Trampert & Woodhouse 1995;Ekström et al. 1997; van Heijst & Woodhouse 1999) from automatic data processing. There are several reasons for this. Azimuthal anisotropy is assumed to be small compared with radial anisotropy and relevant to this assumption is the increased instability of the inverse problem (Zhang & Lay 1996). Indeed, adding azimuthal anisotropy amounts to adding more parameters to an already underdetermined inverse problem and hence the need for stronger regularization. Modelling shows that the amplitude of the azimuthal terms strongly depends upon damping (e.g. Levshin et al. 2001), making it difficult to test the assumption of small azimuthal anisotropy. Furthermore, tests have questioned whether phase data are really sensitive enough to detect azimuthal anisotropy (Larsen et al. 1998; Laske & Masters 1998) and the use of additional polarization data has been proposed.

It is certainly worth mapping anisotropy, which can give insight into the convective flow inside the Earth. This connection has been made as early as the 1980s (Regan & Anderson 1984; Tanimoto & Anderson 1984) and since then has been well accepted and put in a
All other contravariant components are zero. A simple way to determine these terms is to extract this strength prior to constructing the anisotropic phase velocity maps. It is convenient to parametrize the problem in terms of generalized spherical harmonics as shown in the next section. We then explain how we can estimate the strength of the azimuthal terms from the data and discuss the results of our obtained models.

2 PARAMETRIZATION

A plane-layered medium in the presence of a slight general anisotropy gives rise to an azimuthal dependence of the local phase velocity (Smith & Dahlen 1973, 1975). The same azimuthal dependence gives rise to an azimuthal dependence of the local phase velocity. A plane-layered medium in the presence of a slight general anisotropy gives rise to an azimuthal dependence of the local phase velocity. A plane-layered medium in the presence of a slight general anisotropy gives rise to an azimuthal dependence of the local phase velocity. A plane-layered medium in the presence of a slight general anisotropy gives rise to an azimuthal dependence of the local phase velocity.

Path integrals of $dc/c$ are now readily calculated by making use of spherical harmonic rotation matrices to reduce any path to an equatorial path. The advantages of this parametrization are that there are no singularities in the description associated with the indeterminacy of azimuths at the poles, the inverse problem becomes invariant with respect to rotations of the coordinate system and analytic results are available for the path integrals. The forward problem then reduces to the usual linear relation

$$d = Gm,$$  

where $d$ are the path-averaged phase velocity measurements, $m = (m_0, m_2, m_4)^T$ is the model vector of the spherical harmonic coefficients corresponding to the $0\psi$, $2\psi$ and $4\psi$ terms, respectively, and $G = \text{diag}(G_0, G_2, G_4)$ is the block-diagonal matrix of the path-averaged spherical harmonics. $G_0$ contains the ordinary path-averaged spherical harmonics and $G_2$ and $G_4$ correspond to the generalized spherical harmonics defined in eqs. (11) and (12), respectively. The number of unknowns is $(L + 1)^2$ for the $0\psi$ or azimuthally averaged terms, $(2L + 6)(L - 1)$ for the $2\psi$ terms and $(2L + 10)(L - 3)$ for the $4\psi$ terms. In the following, we use $L = 40$ for the isotropic terms and $L = 20$ for the azimuthal terms, resulting in 3405 unknowns.

3 IS AZIMUTHAL ANISOTROPY REQUIRED?

As mentioned in the introduction, several papers have questioned whether phase data are sufficiently sensitive to azimuthal anisotropy. The main reason for these doubts is the strong dependence of the amplitude of anisotropy upon regularization in the inverse problem. Constructing a global isotropic phase velocity map requires solving a linear inverse problem of several tens of thousands of data and 1681 unknowns for a spherical harmonic expansion up to degree 40. Even though the number of data largely exceeds the number of parameters, errors and inconsistencies in the data and inhomogeneous ray coverage make it impossible to retrieve all model parameters. The inverse problem is unstable and needs to be regularized. Recent maps typically solve for 800 independent parameters out of the 1681 (e.g. Trampert & Woodhouse 2001). Adding azimuthal terms as shown in eq. (1) roughly doubles the number of unknowns without changing the data. The inverse problem becomes more unstable and needs stronger damping. There is no objective criterion for choosing the damping and experience shows that the amplitude of the azimuthal terms depends strongly upon it. On the other hand, adding more parameters into the inversion process generally results in a better variance reduction. The question is then whether the improvement in variance reduction is due to the shear fact of increasing the number of parameters or if the data really prefer azimuthal terms. The answer to this question is given by the F-test (e.g. Bevington & Robinson 1992), which states to what level of confidence the difference in variance reduction is significant.

The inverse problem defined in eq. (14) is solved in the usual way by minimizing a cost function

$$C = (d - Gm)^T C_m^{-1}(d - Gm) + G^T C_m^{-1}Gm,$$  

where $C_m$ is the data covariance matrix, which we take to be diagonal and where the data errors have been determined by cluster analyses (Trampert & Woodhouse 2001). $C_m$ is a diagonal matrix, which
we use to impose smoothness upon the model vector. We prefer Laplacian over model damping to reduce spectral leakage (Trampert & Snieder 1996) and the derivation of the smoothness operator can be found in Trampert & Woodhouse (1995). As the model vector, \( \text{C}_m \), is partitioned to emphasize 0, \( w \), and 4\( w \) terms leading to the explicit expressions

\[
(C_{m0})_{jj} = \frac{1}{\lambda} \frac{1}{[l(l+1)]^2}
\]

(15)

\[
(C_{m2})_{jj} = \frac{\theta_2}{\lambda} \frac{1}{[l(l+1)]^2}
\]

(16)

\[
(C_{m4})_{jj} = \frac{\theta_4}{\lambda} \frac{1}{[l(l+1)]^2}
\]

(17)

where \( \lambda \) is an overall damping parameter which controls the trade-off between data misfit and smoothness. The smaller its value, the more the model parameters are allowed to vary and the better the data are explained. \( \theta_2 \) and \( \theta_4 \) control the relative strength of anisotropy. A uniform value of 0.1, for instance, puts 10 times more signal into the isotropic terms relative to the anisotropic ones. To gain an idea of reasonable values for \( \theta_2 \) and \( \theta_4 \), we minimize eq. (14) many times, systematically varying the parameters \( \lambda \), \( \theta_2 \) and \( \theta_4 \) and plot the reduced \( \chi^2 \) as a function of independent parameters in the final model. To compare two different inversions, the total number of unknowns put in the inverse problem is irrelevant, what matters is the number of independent parameters used to construct the estimated model, given by the trace of the resolution matrix. We define the reduced \( \chi^2 \) as

\[
\chi^2 = \frac{1}{N-M} (d - Gm)^T C^{-1}_a (d - Gm)
\]

(18)

where \( N \) is the number of data and \( M = \text{trace}(R) \). The obtained misfit curves show which parametrization explains the data best for a given number of independent parameters. A standard F-test tells us further how significant the differences between two given curves are.

Before turning to real data, we would like to comment on several synthetic tests. We calculated synthetic data with randomly generated isotropic and anisotropic models using our Love wave data coverage (Fig. 1). We added errors drawn from a Gaussian distribution with a standard deviation of 10 per cent of the values of the synthetic data. First, we inverted data corresponding to a purely random 4\( w \) and Love terms only (Montagner & Nataf 1986). Such reasoning assumes self-coupling and a good candidate to explain the discrepancy would be to evoke strong Love-Rayleigh coupling. Before complicating the theoretical framework, however, we want to make sure that our data coverage can distinguish between 2\( w \) and 4\( w \) models. We thus generated a random 4\( w \)-only degree-20 model (850 model parameters) and calculated various misfit curves (Fig. 2c). Sure enough the misfit curve corresponding to a suppressed 2\( w \) inversion gives the smallest misfit. Allowing 2\( w \) terms in the inversion increases the misfit. The F-test assigns 100 per cent significance to the differences up to the first 850 parameters. Beyond 850 parameters we are running out of 4\( w \) parameters and some signal is explained by 2\( w \) parameters, bringing the misfit curves closer together. Repeating the same test for a purely 2\( w \) input model results in the smallest misfit for a mainly 2\( w \) inversion. These calculations indicate that we have the possibility to determine the strength of azimuthal anisotropy from the data and that the data coverage is sufficient to distinguish between the different azimuthal terms. It should be noted, however, that in these synthetic tests all parameters were completely controlled, particularly, the size and distribution of the uncertainties was perfectly known. In the case of real data this is clearly more difficult.

## 4 Misfit Curves for the Data

We generated as outlined above misfit curves for our data. The most difficult part in the measuring process is to assign errors to the data because many assumptions are implicit in such measurements. We found that a reliable estimate was derived from cluster analyses when we included measurements made with varying assumptions (Trampert & Woodhouse 2001). Errors assigned by cluster analyses assume a Gaussian distribution, which is difficult to check in most cases. Consequently, errors in the data are only approximately known compared with the perfectly determined synthetic tests and make it difficult to distinguish between some misfit curves. Examples of the results are seen in Figs 3 and 4. In general, for small numbers of inverted parameters (long-wavelength or low-spherical harmonic degree inversions), purely isotropic paratemrizations explain the data best. Allowing more parameters in the inversion, eventually anisotropic models become more efficient in explaining the data. Part of the smaller-scale isotropic structure is, in fact, due to long-scale anisotropic structure. This is similar to the textbook example of a finely layered isotropic medium which behaves as a transversely isotropic medium when overall apparent elastic properties are considered. From approximately 500 parameters onwards, we gain at least 5 per cent in \( \chi^2 \) reduction if we allow some azimuthal anisotropy, indicating that the data clearly contain anisotropic information. The F-test shows that this is significant with 100 per cent confidence. Looking closer, there are also differences in the misfit curves between different strengths of anisotropy although much smaller than compared with the isotropic case. The question
Figure 1. Azimuthal coverage of Love wave rays calculated for 20 x 20 deg$^2$ cells. Top: azimuthal coverage for minor arcs. Bottom: azimuthal coverage for major arcs. Note how the major arcs fill important gaps in the azimuthal coverage of the minor arcs. Using minor arcs alone could thus lead to biases in the azimuthal terms. The averaged ray density per cell (not shown) is high and relatively uniform between 1000 and 10 000 rays per cell for a total of 58 506 paths.

is whether or not these differences are significant. The significance varies as a function of inverted parameters and the eigenvalue spectra corresponding to the inverse problem indicate that roughly 800 independently inverted parameters are a reasonable choice for our Love and Rayleigh wave coverage (see also Trampert & Woodhouse 2001).

For Love waves, all anisotropic misfit curves (Fig. 3) are close together and the F-test shows that for 800 free parameters, there is at least a 30 per cent chance (up to 80 per cent depending on period) that the differences are not significant. Note that we included misfit curves for 4ψ azimuthal terms only to test whether or not our data require 2ψ terms. This is an important question because a general
slightly anisotropic Earth should not give a significant $2\psi$ term for love waves in the absence of mode coupling (Montagner & Nataf 1986). In the past, strong $2\psi$ Love terms have been found (Montagner & Tanimoto 1990) and, if confirmed, most likely means that strong Love-Rayleigh coupling is present. Given the results of the F-test mentioned above, we find that with a sufficiently high degree of confidence our data do not require the inclusion of $2\psi$ terms.

For Rayleigh waves, all anisotropic misfit curves (Figs 4) are again close together, although there is a slight indication that the data require stronger anisotropy with increasing period. We included a misfit curve with strongly damped $4\psi$ terms because for some petrological models, it is found that the $2\psi$ terms are dominant for Rayleigh waves (Montagner & Tanimoto 1991). If the data could distinguish between cases with or without $4\psi$ terms, this would be a strong petrological discriminant. The F-test shows that the differences between the anisotropic misfit curves are not as significant as the difference with the isotropic case. Nevertheless, at 40 s, the data require with a 95 per cent confidence level a $4\psi$ term from 750 free parameters onwards. It is less certain whether an overall anisotropic weighting of 0.1 or 0.5 is required. At 150 s, the stronger anisotropy explains the data better with 95 per cent confidence and the neglect of the $4\psi$ term clearly gives a higher $\chi^2$ as the number of parameters increases. The data thus require a $4\psi$ term and an increasing strength of anisotropy with period.

5 RESULTS

We constructed azimuthally anisotropic phase velocity maps from our data (58 506 Love wave measurements and 75 515 Rayleigh wave measurements). Although it is clear from the previous paragraph that the data require some degree of anisotropy, the exact strength is difficult to determine. A conservative point of view leads us to choose the smallest significant amount of anisotropy required by the data. Bearing in mind a future depth interpretation, it is most convenient to construct phase velocity models of equal resolution for Love and Rayleigh waves. We finally used $\theta_2 = 10^{-5}$ and $\theta_4 = 0.1$ for Love waves and $\theta_2 = \theta_4 = 0.1$ for Rayleigh waves, although there is an indication that the data need more anisotropy with increasing period. It should be borne in mind that this weighting is put in the cost function but the data still have the possibility to put more anisotropy into longer-period models if needed. $\lambda$ was adjusted to obtain a total of 800 independently inverted parameters out of the 3405.

Before discussing the models, it is instructive to look at the achieved resolution with the given weighting parameters. The full resolution operator consists of a $3405 \times 3405$ matrix, which is difficult to represent. We calculated the full resolution in each case,
but will only comment on two main points of interest, namely the overall lateral resolution and the trade-off between the different azimuthal terms. The overall lateral resolution is calculated from Backus–Gilbert averaging kernels (Trampert & Woodhouse 1995) and is of degree 22 for the isotropic part and degree eight for the azimuthal part. This coincides roughly with values given directly by the trace of the resolution. The important question of whether isotropic structures can give rise to apparent azimuthal anisotropy through inadequate ray coverage is addressed by filtering previously obtained isotropic phase velocity models with the calculated resolution operators. We have chosen the models of Trampert & Woodhouse (2001) because these models and our resolution operators are built from the same number of independent parameters. We calculated the total power of each individual $0\psi$, $2\psi$ and $4\psi$ output model block relative to the total power of the input model. The results are summarized in Table 1. Regardless of the input model, the trade-off with azimuthal terms is negligible due to our excellent and complementary minor and major arc data coverage. The imperfect isotropic recovery is due to a loss of power in the highest degrees, indicating that part of the small-scale structure in purely isotropic inversions is due to unmodelled azimuthal anisotropy. This results in a lower overall lateral resolution ($L = 22$) compared with a simple isotropic inversion ($L = 28$) for the same number of inverted

<table>
<thead>
<tr>
<th>Isotropic input model</th>
<th>$0\psi$</th>
<th>$2\psi$</th>
<th>$4\psi$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Love 40 s</td>
<td>0.88</td>
<td>$2.3 \times 10^{-15}$</td>
<td>$8.6 \times 10^{-4}$</td>
</tr>
<tr>
<td>Love 150 s</td>
<td>0.70</td>
<td>$6.8 \times 10^{-15}$</td>
<td>$2.2 \times 10^{-3}$</td>
</tr>
<tr>
<td>Rayleigh 40 s</td>
<td>0.88</td>
<td>$1.2 \times 10^{-3}$</td>
<td>$5.8 \times 10^{-4}$</td>
</tr>
<tr>
<td>Rayleigh 150 s</td>
<td>0.57</td>
<td>$4.1 \times 10^{-3}$</td>
<td>$2.0 \times 10^{-4}$</td>
</tr>
</tbody>
</table>

The isotropic input models are from Trampert & Woodhouse (2001). $0\psi$ lists the output power of the isotropic model part relative to the input power, $2\psi$ and $4\psi$ correspond to the respective parts of the azimuthal anisotropy.

Figure 4. Misfit curves for (a) 40 s Rayleigh wave data and (b) 150 s Rayleigh wave data.

Figure 5. Relative rms error as a function of the spherical harmonic degree for different isotropic phase velocity models. The curves have been smoothed with a cubic regression.
parameters. For the same strength of anisotropy in the cost function, we note that the longer the period, the more gain there is in variance reduction (Figs 3 and 4) and the more loss of power in the highest degrees (Table 1). This is consistent with the findings from the misfit curves that the data require slightly more anisotropy with increasing period. We checked that the lowest degrees remained unchanged.

Another possible influence on the results could come from irregular topography of the major discontinuities within the Earth. To
test this, we corrected our data with the predictions from CRUST5.1 (Mooney et al. 1998) and the observed surface topography before inversion. As expected the isotropic models changed accordingly, the $2\psi$ and $4\psi$ terms, however, did not change noticeably. Moho depth and topography are the discontinuities with the most pronounced undulations, but we find no significant effects on the azimuthal terms of our models. We interpret this as an indication that undulations in the topography of discontinuities have a first-order effect on the isotropic terms of local phase velocities, but no more than a second-order effect on the azimuthal terms.
We will not show any results for the isotropic part of the models. We have published several models over the past few years with the aim of distinguishing robust features in the models. The construction of the models is data dependent and not unique because of the need for damping. With our currently published models we can address the variability in the models due to uncertainties in the phase velocity measuring process, data coverage, model parametrization and regularization in the inverse problem. As a quick reminder, we first applied our automatic measuring technique with conservative inbuilt protections, resulting in mainly minor arc data (Trampert &
Woodhouse 1995), which required strong damping in the map construction. In Trampert & Woodhouse (1996), we relaxed the inbuilt protections and measured many major arc data. The resulting maps were built using much less damping. We then refined the measuring technique, starting from aspherical reference models (Trampert & Woodhouse 2001). This resulted in a much better control over the $2\pi$ ambiguity. We further cleaned the data set from outliers using cluster analyses. In the present work, we included azimuthal anisotropy in the parametrization having mainly an effect on the higher degrees of the isotropic models. To evaluate the variability in the models thus obtained, we calculate for each spherical harmonic coefficient the mean and variance of the spectral amplitude. In Fig. 5, we plot the ratio of the standard deviation over the mean, giving a relative rms error as a function of the spherical harmonic degree. The relative error increases with increasing period and spherical harmonic degree, indicating that the longer the period and the higher the degree, the more uncertain the models are. As an indication, fixing the acceptable relative model error to 0.3 would mean that models for 40 (150) s become unreliable from degree 25 (15) onwards.

The models for azimuthal anisotropy are plotted in Figs 6–8. In general, for Rayleigh waves, the 2$\psi$ term is stronger (rms amplitude of 0.5 per cent) than the 4$\psi$ term (rms amplitude of 0.25 per cent). The 4$\psi$ term for Love waves is stronger (rms amplitude of 0.5 per cent) than the corresponding Rayleigh wave term. The correlation of 2$\psi$ and 4$\psi$ models at different periods is relatively high (Fig. 9), indicating that the source of anisotropy is shallow, probably lithospheric, but a detailed depth inversion will have to clarify this. For instance, the overall high correlation of the 2$\psi$ Rayleigh terms is dominated by the oceanic part (0.60) compared with a correlation of only 0.16 for continents, suggesting a deeper source of anisotropy beneath continents at least. The dominant degrees in the 2$\psi$ Rayleigh models are two to four. For the 4$\psi$ models the maximum power is found for degree six, slightly shorter wavelength. It is generally observed that the fast directions of the 2$\psi$ Rayleigh terms agree well with directions of plate motions in the oceans (Tanimoto & Anderson 1985; Montagner & Tanimoto 1990). Qualitatively we also see such a correlation, especially fast directions perpendicular to mid-oceanic ridges. While relative plate motions are well constrained, their absolute motion with respect to the underlying mantle is still a matter of debate (Gordon 1995). We considered absolute plate motions in the two most common reference frames: the hotspot reference frame (HS2-NUVEL1 from Gripp & Gordon 1990) and the no-net-rotation reference frame (NNR-NUVEL1 from Argus & Gordon 1991). It has also been suggested that fossil seafloor spreading directions could be important (Nishimura & Forsyth 1989). We obtained these fossil directions from the mapped magnetic anomalies in the oceans. At each point, we calculated the angular difference between the fast direction of the 2$\psi$ Rayleigh term and the local direction of absolute plate motion. Since we are considering directions only, the differences are represented between $0^\circ$ and $90^\circ$. To show the significance of the correlation most clearly, we plotted cumulative distributions and compared them with a set of random angles (Fig. 10). In the oceans, there is no clear overall correlation using the no-net-rotation reference frame or the fossil directions. The corresponding distributions plot close to that of random angles. The hotspot reference shows a clear correlation and we note again the similarity between directions at 40 and 150 s. In continents, the no-net-rotation reference frame again gives no significant correlation, but the hotspot reference frame works remarkably well, especially at 150 s where two-thirds of all directions agree to better than $25^\circ$ concurring with a recent study beneath Australia (Simons & van der Hilst 2003). This is an interesting observation, because most studies of anisotropy beneath continents rely on shear wave splitting measurements (Silver 1996). It will now be interesting to construct models of azimuthal anisotropy as a function of depth and test several hypothesis concerning the role of plates in the overall mantle flow. The models presented here can be downloaded from ftp://terra.geo.uu.nl/pub/jeannot/twgji02aniso.tar.gz.

6 CONCLUDING REMARKS

We constructed global anisotropic phase velocity maps from more than 100 000 automatically measured phase differences of surface waves between 40 and 150 s. The azimuthal anisotropy is expanded in terms of generalized spherical harmonics, which allows path-averaged phase velocities to be calculated with great ease. This parametrization makes the inverse problem invariant with respect to rotations of the coordinate frame and eliminates singularities associated with the indeterminacy of azimuths at the poles. Great care is taken to determine the strength of anisotropy required by the data. To achieve this we propose a technique based on relative weighting of the different model terms in the cost function associated with the inverse problem. The results show that phase data clearly require azimuthal anisotropy. Including azimuthal anisotropy into phase velocity map constructions reduces the overall lateral resolution of the isotropic part by reducing the power of the highest degrees. This indicates that short-wavelength structure seen in purely isotropic inversion could result from unmodelled azimuthal anisotropy. Concerning azimuthal anisotropy itself, we observe that Love wave data do not require 2$\psi$ terms, whereas Rayleigh wave data need both, 2$\psi$ and 4$\psi$ terms, although the 2$\psi$ term is stronger. Based on correlations, the sources of the observed azimuthal anisotropy are shallow. Only absolute plate motions in the hotspot reference frame show a significant correlation with the fast 2$\psi$ Rayleigh directions.

ACKNOWLEDGMENTS

This research was partly financed by a joint scientific research grant from the Dutch National Science Foundation (NWO) and the British Council. Yanick Ricard provided the fossil sea floor directions based on magnetic anomalies.
Figure 10. Cumulative distribution of the angular difference between the absolute plate motion and the fast $2\psi$ Rayleigh directions at 40 and 150 s (a) for continents and (b) for oceans. The plate motions correspond to the models HS2-NUVEL1, NNR-NUVEL1 and the fossil directions deduced from magnetic anomalies. Random angles plot as a straight line in the cumulative graph.

REFERENCES

Relevant references include: