Storm-Relative Helicity Revealed from Polarimetric Radar Measurements

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ABSTRACT

The dual-polarization radar variables are especially sensitive to the microphysical processes of melting and size sorting of precipitation particles. In deep convective storms, polarimetric measurements of such processes can provide information about the airflow in and around the storm that may be used to elucidate storm behavior and evolution. Size sorting mechanisms include differential sedimentation, vertical transport, strong rotation, and wind shear. In particular, winds that veer with increasing height typical of supercell environments cause size sorting that is manifested as an enhancement of differential reflectivity ($Z_{DR}$) along the right or inflow edge of the forward-flank downdraft precipitation echo, which has been called the $Z_{DR}$ arc signature. In some cases, this shear profile can be augmented by the storm inflow. It is argued that the magnitude of this enhancement is related to the low-level storm-relative environmental helicity (SRH) in the storm inflow.

To test this hypothesis, a simple numerical model is constructed that calculates trajectories for raindrops based on their individual sizes, which allows size sorting to occur. The modeling results indicate a strong positive correlation between the maximum $Z_{DR}$ in the arc signature and the low-level SRH, regardless of the initial drop size distribution aloft. Additional observational evidence in support of the conceptual model is presented. Potential changes in the $Z_{DR}$ arc signature as the supercell evolves and the low-level mesocyclone occludes are described.

1. Introduction

a. Polarimetric variables

Dual-polarization radar observations provide insight into microphysical processes in clouds and precipitation. By receiving signals at orthogonal polarizations, information is gathered about bulk particle properties within the sampling volume, such as size, shape, composition, and diversity (e.g., Herzegh and Jameson 1992; Zrnić and Ryzhkov 1999; Bringi and Chandrasekar 2001). The simultaneous transmission of horizontally and vertically polarized radio waves allows for several polarimetric variables to be estimated, including the differential reflectivity ($Z_{DR}$), differential phase shift ($\Phi_{DP}$), and copolar cross-correlation coefficient ($\rho_{HV}$). These quantities supplement the conventional radar signals of the reflectivity factor at horizontal polarization ($Z_{HH}$) and Doppler velocity ($u_r$). The logarithmic ratio between backscattered power returned to the radar at horizontal polarization and vertical polarization, $Z_{DR}$ (Seliga and Bringi 1976), is sensitive to the shape, orientation, density, and phase composition of hydrometeors in the sampling volume, but not to their concentration. Because raindrop oblateness increases with diameter (Pruppacher and Pitter 1971), $Z_{DR}$ increases with increasing raindrop size. Hydrometeors with isotropic scattering characteristics (e.g., spherical particles or chaotically tumbling particles) have an intrinsic $Z_{DR}$ of 0 dB. For a given shape, higher particle density or higher liquid water content results in higher $Z_{DR}$. The differential phase shift $\Phi_{DP}$ measures the phase difference (in degrees) between the forward-propagating horizontally polarized wave and the vertically polarized wave. As the signals propagate through a medium such as rain, the horizontally polarized wave gradually slows down relative to the vertically polarized wave as it encounters more liquid water because raindrops are oblate. This slowing results in a positive phase difference between the waves. The range derivative of this differential phase shift is the specific differential phase, $K_{DP}$ (given in deg km$^{-1}$), which is sensitive to the concentration of liquid drops but is nearly zero for heavily aggregated snow or dry graupel/hail. As a consequence,
$K_{DP}$ is a good indicator of liquid water content in the resolution volume. The correlation coefficient between the backscattered returns at horizontal and vertical polarization at zero lag time $\rho_{HV}$ is sensitive to the diversity of particle sizes, orientations, shapes, and phase compositions within the sampling volume, being especially sensitive to particles of the size in which resonance scattering effects occur. Such resonance scattering occurs when the ratio

$$\gamma = \frac{D \sqrt{\varepsilon}}{\lambda}$$

is on the order of unity (where $D$ is the particle equivalent diameter, $\varepsilon$ is the dielectric constant of the particle, and $\lambda$ is the radar wavelength).

**b. Microphysical processes**

Polarimetric variables are especially sensitive to microphysical processes characterizing particle phase transitions (e.g., melting) and size sorting of hydrometeors. Signatures from precipitating systems evident in the polarimetric data subsequently provide information about these microphysical processes. The polarimetric signature of a melting layer is an example of the snow-to-rain transition (melting) that appears distinctly in the observed variables (see Ryzhkov and Zrnić 1998; Brandes and Ikeda 2004; Giangrande et al. 2005, 2008).

The trajectories of hydrometeors are dependent on airflow patterns within the storm. Because the terminal fall speed of a raindrop increases monotonically with its diameter (Gunn and Kinzer 1949), drops will be advected throughout the storm at varying rates. A consequence of this is a separation of drops based on their size because smaller drops are advected farther down-stream than larger drops, which fall faster and thus are exposed to air currents for shorter time intervals. This separation of drop sizes due to a combination of air motions in storms and different terminal fall speeds is what we define as size sorting.

**c. Size sorting**

Generally, $Z_{DR}$ increases with $Z_{HH}$ in rain. However, $Z_{DR}$ can vary dramatically for a given $Z_{HH}$ because of strong local drop size distribution (DSD) variability, which is related directly to size sorting. In this subsection we describe several size sorting mechanisms found in convective storms.

Differential sedimentation, the simplest size sorting mechanism, occurs in the absence of any air motion. When a cloud begins to precipitation, the largest drops fall faster than the smaller drops. Before an equilibrium drop size distribution is attained, the median drop size increases with decreasing height. As a result, polarimetric observations of developing convective cells generally display enhanced $Z_{DR}$ beneath the cell, often collocated with very low $Z_{HH}$.

Positive vertical velocities in convective updrafts provide additional size sorting to the differential sedimentation mechanism. As hydrometeors encounter upward air motion, their fall velocities are affected. If the updraft vertical velocity is greater than the hydrometeor terminal velocity, the particle is lofted. Only if the terminal velocity of the hydrometeor is greater than the vertical velocity will the particle fall. Size sorting within updrafts is frequently observed in convective storms as a $Z_{DR}$ column (e.g., Caylor and Illingworth 1987; Illingworth et al. 1987; Tuttle et al. 1989; Meischner et al. 1991; Conway and Zrnić 1993; Brandes et al. 1995; Hubbert et al. 1998; Kennedy et al. 2001; Loney et al. 2002; Ryzhkov et al. 2005; Kumjian and Ryzhkov 2008). Only the largest raindrops that have large terminal velocities can fall through the updraft; the other drops are carried farther aloft. If the storm updraft is so intense that no raindrops can fall, the largest drops fall at the periphery of the updraft, where vertical velocities are diminished. In this case, the $Z_{DR}$ column is situated at the edge of the updraft, usually along a gradient of $Z_{HH}$.

Strong rotation on the scale of a tornado can cause size sorting through centrifuging of hydrometeors (e.g., Dowell et al. 2005). In the case of rain, the largest drops are centrifuged outward farther than the smaller drops. A pattern of concentric bands of $Z_{HH}$ and an outer band of enhanced $Z_{DR}$ in a study by Bluestein et al. (2007) are likely a manifestation of this type of size sorting. In a mesocyclone, the length and velocity scales are such that centrifuging of raindrops is less significant; centrifugal accelerations are roughly two orders of magnitude lower for characteristic mesocyclone scales than for characteristic tornado scales.

Size sorting has been attributed to wind speed shear for several decades (e.g., Gunn and Marshall 1955; Hitchens 1960; Jameson and Johnson 1983). Precipitation particles approximately follow the horizontal flow for modest wind speeds. In the event of extremely strong winds such as in a tornado, the raindrops do not follow the air currents. In fact, Dowell et al. (2005) found large differences between the air trajectories and the hydrometeor trajectories in a tornado, which can lead to significant errors in Doppler velocity retrievals. The particles that fall more slowly will experience horizontal advection longer than larger particles falling faster. In linear mesoscale convective systems, an enhancement of $Z_{DR}$ is found frequently along the leading edge. Size sorting due to a combination of quasi-unidirectional...
wind shear and the leading convective updrafts produces this enhancement.

In supercells, Kumjian and Ryzhkov (2008) have found that numerous signatures are consistently observed in the polarimetric data, including the tornadic debris signature, signatures of large hail, low-level inflow and the midlevel updraft, \(Z_{DR}\) and \(K_{DP}\) columns, midlevel \(Z_{DR}\) and \(\rho_H\) rings, and the low-level \(Z_{DR}\) arc. This study examines the last signature in detail, which appears to be caused by the size sorting of raindrops due to speed and directional wind shear. Strong increases in speed and clockwise turning of the winds with height characterize helical environments (i.e., those with helicity; Lilly 1986). Within rotating updrafts, vertical helicity can be quite large. In contrast, vertical helicity is assumed to be negligible when we consider the storm-relative environmental helicity, which is a measure of the streamwise component of the vorticity of the environmental flow in the reference frame of the storm (Davies-Jones 1984). Davies-Jones et al. (1990) define storm-relative environmental helicity (SRH) as

\[
SRH = \int_0^{h'} \left( \nabla \times \mathbf{v}_H \right) \cdot \left( \mathbf{v}_H - \mathbf{v}_r \right) \, dz, \tag{2}
\]

where the integration typically is performed from the ground to some height \(h'\), generally taken to be the level of free convection or about 3 km (e.g., Droegemeier et al. 1993; Markowski et al. 1998). The horizontal velocity vector \(\mathbf{v}_H\) and the storm motion vector \(\mathbf{v}_r\) are used in the integrand. Numerous studies have found that the low-level SRH is a decent indicator of the potential for tornadoes and can be an important prognostic variable for severe storm forecasters (e.g., Lefitch 1990; Davies and Johns 1993; Colquhoun and Riley 1996; Kerr and Darkow 1996; Rasmussen and Blanchard 1998; Thompson et al. 2003, 2007). Thus, it is important to obtain accurate estimates of the low-level SRH, which is known to have significant spatial and temporal variations (e.g., Davies-Jones 1993; Markowski et al. 1998). Because soundings are infrequent and are only meant to capture the synoptic-scale environment, often they are not adequate to resolve the storm-scale variability of SRH. Richardson et al. (2007) found that heterogeneities within the mesoscale environment can also be important, at least in numerical simulations. These mesoscale inhomogeneities would not be captured by sparse and infrequent soundings.

The next section will describe the \(Z_{DR}\) arc and the size sorting that causes it in more detail and presents a hypothesis relating the \(Z_{DR}\) arc and low-level SRH. In section 3, we present a simple numerical model used to test the hypothesis and provide results from several experiments. Observations from tornadic and nontornadic supercells as well as nonsupercell severe storms are discussed in section 4. Section 5 provides a summary of the conclusions from this work.

2. The \(Z_{DR}\) arc

a. Description

The \(Z_{DR}\) arc is a narrow arc-shaped region of very high \(Z_{DR}\) values (>4 dB) found along the \(Z_{HH}\) gradient of the southern (right) or inflow edge of the forward-flank downdraft (FFD) echo in right-moving supercell storms (Kumjian and Ryzhkov 2008). It extends from the updraft region (and thus sometimes connects to the \(Z_{DR}\) column) downstream along the edge of the FFD echo, generally aligned in a direction roughly parallel to the storm motion. This region of the storm is characterized by relatively low \(Z_{HH}\) and high \(Z_{DR}\), which indicate the presence of a sparse population of large (6–8 mm) drops and a relative lack of smaller drops. The signature is generally very shallow, located in the lowest 1–2 km of the storm. For comparison, the typical environmental melting level in the spring cases is about 3–4 km. Such a signature has been observed at S, C, and X bands in many supercells from different geographic regions, including the High Plains (Van Den Broeke 2007, personal communication), the Southern Plains (Kumjian and Ryzhkov 2008; Snyder 2008), the southeastern United States (Kumjian et al. 2008), southern Finland (Outinen and Teittinen 2007, 2008), Canada (Kumjian and Ryzhkov 2007), and Germany (Höller et al. 1994). The \(Z_{DR}\) arc has also been seen in most seasons, as early as 1 March and as late as 10 November. We expect the \(Z_{DR}\) arc to be present in winter supercells when polarimetric observations become more widely available. Several examples of \(Z_{DR}\) arcs observed in central Oklahoma are presented in Fig. 1. In the figure, the data from the original polar radar coordinates have been linearly interpolated onto a Cartesian grid. The \(Z_{DR}\) arc is a consistent feature of supercells and thus may be related to intrinsic processes both within the storms and in their environments.

b. Size sorting hypothesis

Some of the earliest studies of supercell structure noted that the sloping reflectivity echo overhang in the forward flank is a manifestation of precipitation particles being advected toward the left flank of the storm (e.g., Browning and Donaldson 1963; Browning 1964, 1965). Browning (1964) alluded to wind shear as a size sorting mechanism by suggesting that smaller particles...
are transported farther downstream than larger hydrometeors. Additionally, he studied cyclonic “streamers” of precipitation that indicated hydrometeors falling into an environment in which winds veered with height.

In supercell storms, size sorting can be extreme. The strong speed and directional shear that is common in low-level storm-relative hodographs of tornadic supercell environments (e.g., Maddox 1976; Davies-Jones 1984; Thompson and Edwards 2000; Thompson et al. 2003; Esterheld and Giuliano 2008) can cause a significant amount of drop sorting in a relatively shallow layer, resulting in a substantially modified drop size distribution along the edge of the precipitation echo on the inflow side of the storm (i.e., the FFD). This modified DSD contains large drops and a relative lack of smaller drops, which have been advected farther into the FFD. Polarimetric radar observations reveal such skewed DSDs to be strong enhancements of $Z_{DR}$ because the median drop size is quite large. Additional evidence for strong shear affecting supercell precipitation at low levels comes from a recent study by Yu et al. (2009), who found unusual dual-peak signatures in the Doppler spectra from one of the tornadic supercells considered in the current study (10 May 2003). They attributed

\[1\]

The dataset used in this study is the same one used in Kumjian and Ryzhkov (2008). Details of the cases can be found in that paper.
these spectral signatures (which were confined to the lowest elevation angles) to strong shear within the radar sampling volume. Using a simple simulation with vertical shear on the order of 0.01 $s^{-1}$, they were able to reproduce the observed spectra fairly well.

Ryzhkov et al. (2005) first proposed size sorting as a physical explanation for the significant enhancement of $Z_{DR}$ found along the FFD of supercells. Strong low-level shear contained in a shallow layer would promote significant size sorting in that shallow layer. In the Yu et al. (2009) study, the lowest elevation angle scans sampled the storm in the lowest 1 km, consistent with the shallow depth of the $Z_{DR}$ arc signature. We suggest that the $Z_{DR}$ arc location and shape are indicative of a wind shear profile most commonly associated with supercells (Fig. 2).

Previous studies (e.g., Goddard et al. 1982; Wakimoto and Bringi 1988) and T-matrix calculations have shown that the intrinsic $Z_{DR}$ of the largest (6–8 mm) raindrops at S band exceeds 4 dB. Although these large drops are found in convective storms, they are usually associated with much higher concentrations of smaller drops, decreasing their relative contribution to the backscattering characteristics observed by the radar. Thus, in heavy rain $Z_{DR}$ generally does not exceed 2–3 dB. However, if these smaller drops are largely removed from the DSD, the observed $Z_{DR}$ can increase to 4–5 dB (and $Z_{HH}$ and $K_{DP}$ would be relatively low). The resulting DSD is quite exotic, as shown by Schuur et al. (2001) in 2D video disdrometer data collected beneath the $Z_{DR}$ region of a supercell. Vigorous size sorting is necessary for this type of significant separation of drop sizes. We argue that the low-level inflow-enhanced veering wind shear characteristic of supercell environments is the size sorting mechanism that causes the $Z_{DR}$ arc signature to appear and that the degree of size sorting is related to the low-level SRH. The next section develops a simple numerical model to explore this hypothesis and to quantify the impact of size sorting on polarimetric variables for a given DSD.

3. The model

a. Description

To test the hypothesis, a simple model of a precipitating cloud was constructed. The domain has variable horizontal extent, depending on what is necessary to capture the entire precipitation field after it is advected. The domain extends 3 km in the vertical. Horizontal resolution is 500 m and vertical resolution is 200 m. A 3 km $\times$ 3 km cloud is placed at the top of the domain. The cloud is square with truncated corners. A Marshall–Palmer raindrop size distribution is assumed initially in the cloud. The rainfall rate in the cloud is modulated such that the center of the cloud is characterized by a rainfall rate of 50 mm h$^{-1}$; this decreases to 35 mm h$^{-1}$ moving away from the center and is 25 mm h$^{-1}$ at the edges. The DSDs are discretized into 80 size intervals, ranging from 0.05 to 7.95 mm in 0.1-mm increments. Drop sizes are treated independently as “packets” of like drops filled with a concentration prescribed by the initial DSD. The next section develops a simple numerical model to explore this hypothesis and to quantify the impact of size sorting on polarimetric variables for a given DSD.
\[
(y)_n = \begin{cases} 
3.78D_n^{0.67} & \text{for } 0.05 \leq D_n \leq 3.05 \text{ mm} \\
9.65 - 10.3 \exp(-0.6D_n) & \text{for } D_n > 3.05 \text{ mm} 
\end{cases}
\]

(3)

where the subscript \( n \) represents the \( n \)-th drop size interval and \( D \) is in mm. The sensitivity of the model to the initial DSD is discussed in a later subsection.

A new set of packets is placed at the top of the domain at each time step, thus allowing for a continuous flux of drops. The packets of raindrops fall into a horizontally homogeneous wind field. Any vertical profile of wind can be administered. Hodographs displaying the wind profiles will be shown with the results of each experiment. As the packets of drops fall, they are advected with the horizontal flow. The location of each packet and drop size at each time step is calculated. After allowing the precipitation to attain a steady state (approximately 3000 s), constant altitude plan position indicators (CAPPIs) are constructed for various heights. Packets of drops in the corresponding grid boxes are accounted for. This gives the concentration of drops of all sizes, or the modified DSD, at the chosen altitude. From this modified DSD, a T-matrix method (Mishchenko 2000) is employed to calculate the polarimetric variables \( Z_{\text{HH}} \) (dBZ), \( Z_{\text{DR}} \) (dB), and \( K_{\text{DP}} \) (deg km\(^{-1}\)). At the S band in pure rain, \( \rho_{\text{HV}} \) does not differ much from unity and thus is not calculated for these simulations.

In addition to drop interactions, other physical processes have been omitted from the model, including evaporation and spontaneous breakup. For the values of \( Z_{\text{HH}} \) selected in the model, evaporation is not significant. In general, evaporation occurs most rapidly for smaller drops; when uninhibited, the DSD is narrowed,
favoring the larger drop sizes. This would lead to a larger median drop size in the radar resolution volume, enhancing $Z_{DR}$. Spontaneous breakup of the largest drops would decrease the relative number of large drops and thus decrease $Z_{DR}$. However, very large (6–8 mm) raindrops have been observed in convective storms (Schuur et al. 2001), so spontaneous breakup is probably not a significant factor in this case; or perhaps it is balanced by self-collection, as suggested by Romine et al. (2008). The modeled precipitation is assumed to fall at terminal velocity from the initialization, which neglects the brief acceleration that drops experience if starting from rest. Beard (1976) shows that the response time of a raindrop to changes in drag is on the order of $\frac{y_{t}(D)}{g}$, or about 1 s, where $y_{t}(D)$ is the terminal velocity of a raindrop with diameter $D$ and $g$ is the gravitational acceleration. This assumption results in an error on the order of a few meters, which is negligible compared to the relatively coarse resolution of the model. The drops are assumed to follow the horizontal winds perfectly, which (as mentioned above) is not true in cases of extreme winds. So, for the relatively coarse model resolution and the magnitude of the wind speeds prescribed in the experiments herein, the errors due to the assumption that raindrops instantaneously adjust to the wind field are negligible.

**b. Results**

The results from the simulations are presented in this subsection. First, a control experiment is performed in which the raindrops fall into a domain with no wind. We expect the resulting fields of polarimetric variables to be

![Fig. 4](http://journals.ametsoc.org/doi/pdf/10.1175/2008JAS2815.1)
the echo occurs because more than one packet of drops and contouring (i.e., the enhancement at the center of the cell because of the absence of a size sorting mechanism. The slight difference in appearance is due to the additional smoothing that takes place in the calculations and contouring (i.e., the enhancement at the center of the echo occurs because more than one packet of drops is found in those grid boxes).

A unidirectional shear profile is prescribed in the first experiment. The environmental winds are westerly at all levels, increasing from 1 m s$^{-1}$ at the surface to 15 m s$^{-1}$ at 3 km. The storm is moving toward the east at 15 m s$^{-1}$. As a result, the storm-relative wind profile is unidirectional and from the east, increasing in magnitude with decreasing height. This type of wind profile can be found in environments of mesoscale convective systems in the Great Plains, for example. The results from this experiment show that the precipitation fields have been modified by the wind shear. Raindrops are advected downstream (which is toward the west in the storm reference frame). As a result of the advection, the $Z_{HH}$ echo extends westward. In Fig. 4, a strong enhancement of $Z_{DR}$ is seen along the right edge of the storm, which corresponds to its leading edge. This enhancement is oriented perpendicular to the direction of motion and frequently is augmented by the convective updrafts in real storms. The alignment and location of this enhancement is distinct from that described for the $Z_{DR}$ arc in supercells and thus would not be considered a $Z_{DR}$ arc. Recall that the $Z_{DR}$ arc is located on the front right edge of the FFD precipitation echo and is generally aligned approximately parallel to storm motion. Subsequently, we should not expect any relation between the magnitude of $Z_{DR}$ and the low-level SRH, which is 0 in this experiment.

Next, an idealized veering wind profile is prescribed. The profile is presented using a hodograph, showing the $u$ and $v$ components of the wind field at each level (Fig. 5). At the surface, winds are from the south at 10 m s$^{-1}$ and uniformly veer with height to westerly at 3 km, also at 10 m s$^{-1}$. However, this time the precipitating cloud moves toward the east at 5 m s$^{-1}$, as indicated by the black dot. This introduces speed shear and enhances the veering. The SRH is proportional to the area swept out by the hodograph (Davies-Jones et al. 1990; Droegemeier et al. 1993) and is shaded in gray. The representativeness of such idealized profiles considered herein is discussed in a later subsection. The resulting polarimetric fields are clearly modified by the winds at both 1500 and 400 m (Fig. 6). The precipitation echo from $Z_{HH}$ extends downstream, indicating that drops are being advected by the winds. In the $Z_{DR}$ field, an enhancement is present along the southern edge of the storm, aligned parallel to storm motion. Maximum values of $Z_{DR}$ at 400 m are about 3.6 dB. Note that $K_{DP}$ is largest in the center of the storm, closely associated with the highest $Z_{HH}$. This is expected because rainfall rate is nearly linearly related to $K_{DP}$ (Sachidananda and Zrnić 1987). The $Z_{DR}$ enhancement occurs along the gradient in reflectivity, indicating a sparse population of larger drops with a lack of smaller drops, as observed in real storms.

The wind shear is amplified in experiment 3, with a 15 m s$^{-1}$ flow from the south at the surface veering to westerly at 15 m s$^{-1}$ at 3 km in the idealized quarter-circle hodograph (Fig. 7). The storm motion vector is toward the east at 10 m s$^{-1}$, enhancing the speed and directional shear relative to the previous experiment, thereby also enhancing the SRH. The resulting polarimetric variables show further modification due to advection (Fig. 8). The $Z_{HH}$ echo extends farther downstream, and the $Z_{DR}$ arc at 400 m is quite strong, with maximum values about 4.5 dB. Again, $K_{DP}$ closely follows the $Z_{HH}$ pattern. Also of note is that the enhancement of $Z_{DR}$ is quite shallow; the $Z_{DR}$ field at 1500 m shows only a 0.5-dB increase over the
The greatest enhancement of $Z_{DR}$ occurs below this level, in the lowest 1 km of the domain. This agrees well with the observations of the $Z_{DR}$ arc, in which the enhancement is only found in the lowest 1–2 km above the ground.

The next experiment (4) uses the low-level wind profile from 9 May 2003, as observed by the 0000 UTC sounding from Norman, Oklahoma (KOUN). This sounding has large SRH and characterizes the environment of a tornadic supercell that produced a violent F-4 tornado in central Oklahoma. A detailed case study of this event can be found in Romine et al. (2008). Polariometric observations from this storm display a strong $Z_{DR}$ arc (Fig. 1a). The initialization uses linearly interpolated winds between the actual sounding observations to provide enough data points below 3 km. The hodograph is essentially unchanged by this interpolation, aside from minor smoothing (Fig. 9). Storm motion was determined by Esterheld and Giuliano (2008), who averaged the translational velocity of the precipitation echo in the volume scans leading up to and just after tornadogenesis, encompassing the time of the polarimetric data from this storm shown above. The resulting polarimetric fields are modified by the shear, again producing an enhancement of $Z_{DR}$ along the southern and eastern edges of the $Z_{HH}$ echo (Fig. 10). The maximum $Z_{DR}$ in the simulation is 4.5 dB, which agrees fairly well with the observed values in the $Z_{DR}$ arc from this storm (4–5 dB). The orientation of the simulated enhancement is also in agreement with the observed signature.

c. Impact of the initial DSD

To some extent, the modeling results depend on the type of initial DSD aloft. Initially we assumed that the DSD aloft is a Marshall–Palmer distribution. The three-parameter gamma distribution

\[ f(x; a, b, c) = \frac{1}{\Gamma(a) b^a} x^{a-1} e^{-b x/c} \]

where $\Gamma$ is the gamma function, $a$, $b$, and $c$ are the shape, scale, and location parameters, respectively. This distribution is commonly used to model radar reflectivity factors and is characterized by its flexibility in fitting various shapes of distribution functions. The shape parameter $a$ controls the skewness of the distribution, the scale parameter $b$ controls the spread, and the location parameter $c$ shifts the distribution along the $x$-axis. In polarimetric radar observations, $Z_{DR}$ is often used as a diagnostic for the presence of hydrometeors, with higher values indicating a larger scatter strength and potentially larger reflectivity factors. The simulation results shown in Fig. 6 illustrate the impact of the initial DSD on the resulting polarimetric fields.
describes a larger variety of DSDs in rain (e.g., Ulbrich 1983). The intercept of the gamma DSD \( N_0 \) for the raindrops aloft does not affect \( Z_{\text{DR}} \) because it is a relative measurement. Hence, additional variability of \( Z_{\text{DR}} \) is caused by variations of the parameters \( \Lambda \) and \( \mu \). Brandes et al. (2004) found that \( \Lambda \) and \( \mu \) are generally well correlated and introduced the constrained gamma DSD in rain. Cao et al. (2008) established that in Oklahoma storms the relation between \( \Lambda \) and \( \mu \) has the form

\[
\mu = -0.0201\Lambda^2 + 0.902\Lambda - 1.718, \tag{5}
\]

where \( \Lambda \) is expressed in mm\(^{-1}\).

In convective storms, the parameter \( \Lambda \) is primarily defined by \( Z_{\text{HH}} \), which usually varies from about 40 to 50 dBZ in the downstream forward-flank precipitation region of supercells. It can be shown that \( \Lambda \) for these values of \( Z_{\text{HH}} \) changes within the interval between 1.7 and 2.9 mm\(^{-1}\). Correspondingly, the parameter \( \mu \) varies from \(-0.24\) to 0.73, according to Eq. (5). To assess the impact of the initial DSD on the spatial distribution of \( Z_{\text{DR}} \) and its maximal value at the 400-m level, we performed simulations for these two combinations of the parameters \( \Lambda \) and \( \mu \).

We compare the simulated \( Z_{\text{DR}} \) maxima to the SRH for each of the experiments by plotting the maximum \( Z_{\text{DR}} \) against the low-level SRH calculated from the simulated hodographs. The 0.4–3-km SRH is used rather than the traditional 0–3-km SRH. This is because the lowest level where the polarimetric variables were calculated was 400 m, and in some cases considerable SRH existed below this level. Except for experiment 4, all simulations were prescribed with idealized quarter-circle hodographs of varying magnitudes, as in experiments 2 and 3 above. A summary of these numerical experiments is provided in Table 1. The scatterplot of maximum \( Z_{\text{DR}} \) versus 0.4–3.0-km SRH for these experiments is shown in Fig. 11. The small diamonds represent the simulations using an initial Marshall–Palmer DSD, the asterisks indicate results of simulations using the first gamma DSD (i.e., \( \Lambda \) = 1.7 mm\(^{-1}\); \( \mu = -0.24 \)), and the triangles correspond to the second gamma DSD (\( \Lambda = 2.9 \) mm\(^{-1}\); \( \mu = 0.73 \)). As Fig. 11 indicates, there is a strong correlation between the maximal \( Z_{\text{DR}} \) and low-level SRH regardless of the type of DSD aloft. For low-level SRH exceeding about 150 m\(^2\) s\(^{-2}\), the largest modeled \( Z_{\text{DR}} \) values are attained. Minimum SRH thresholds for mesocyclones have been reported at 157 m\(^2\) s\(^{-2}\) in observed storms (Davies-Jones et al. 1990) and 250 m\(^2\) s\(^{-2}\) for simulated supercells (Droegemeier et al. 1993). Despite the limitations of our simplistic model, the results indicate that most (if not all) supercells should exhibit a fairly strong \( Z_{\text{DR}} \) arc.

The DSD formed near the ground is primarily determined by the size sorting due to wind shear rather than the initial DSD aloft. Note that the variability of the DSD in convective storms is usually less than in most stratiform rain cases (Bringi et al. 2003). In convective cores, most of the rain is generated from the melting of graupel and hail with relatively high density, which does not vary much. Stratiform rain originates from snow with very high diversity in its density, depending on the degree of riming or aggregation. As a result, size distributions of rain melted from snow more often exhibit larger variability compared to convective rain.

d. Representativeness of the modeled wind profiles

Although the quarter-circle hodographs used in our simulations are idealized, we feel that these wind profiles are representative of the general type of directional and speed shear found in supercell environments. Such simplified hodographs are not without precedent; previous modeling studies have used such quarter-circle and half-circle profiles (e.g., Weisman and Klemp 1984; Droegemeier et al. 1993; Weisman and Rotunno 2000). Additionally, the observed sounding used in experiment 4 yielded similar results.

Unfortunately, some uncertainty exists as to how well even the observed soundings capture the near-storm environment, especially because the strong low-level inflow from the storm can alter the local wind profiles.
In some cases, the inflow may intensify the low-level shear and SRH, which should increase the amount of size sorting. Observations within the near-storm environment are relatively sparse, so further studies are necessary to quantify the impact of the storm itself on its environment. This issue is further explored in the discussion section.

4. Observations

In this section we will describe observations of the $Z_{DR}$ arc in tornadic and nontornadic supercells as it appears before the low-level mesocyclone occludes and once the occlusion takes place. Observations from left-moving supercells (resulting from the splitting of the parent storm) are presented. Additionally, the appearance of the signature in developing supercells and in nonsupercell storms preceding the development of severe weather is discussed briefly.

a. Supercell storms

1) PRE-OCCLUSION VERSUS OCCLUSION

The rear-flank downdraft (RFD) has long been implicated with tornadogenesis (e.g., Lemon and Doswell 1979). In fact, Davies-Jones (2008) has shown that the hook echo precipitation associated with the RFD can actually instigate tornadogenesis through the downward transport of air rich in angular momentum, which is subsequently converged under the updraft. Of particular interest in many modeling and observational studies is the occlusion of the low-level mesocyclone by the RFD, which is believed to be intricately tied to the development of a tornado (Lemon and Doswell 1979; Klemp and Rotunno 1983; Klemp 1987; Wicker and

FIG. 8. As in Fig. 4, but for experiment 3 (the hodograph in Fig. 7). A substantial enhancement of $Z_{DR}$ is present at 400 m, with maximum values about 4.5 dB.
Wilhelmson 1995). Thus, any indication that the occlusion process is beginning may allow forecasters to give more advanced warnings. It should be noted, however, that the occlusion of the low-level mesocyclone is not a sufficient condition for tornadogenesis; recent research has shown that low-level thermodynamic characteristics of the RFD can be important (see Markowski 2002; Markowski et al. 2002, 2003).

A recent observational study by Van Den Broeke et al. (2008) suggests that the $Z_{DR}$ arc tends to extend back toward the updraft at times leading up to tornadogenesis, sometimes wrapping around the inside of the hook echo (Kumjian et al. 2008). Observations of non-tornadic supercells from the Kumjian and Ryzhkov (2008) dataset show this extension of the $Z_{DR}$ arc preceding the occlusion of the low-level mesocyclone. Thus, it is unlikely that the $Z_{DR}$ arc is a manifestation of
Table 1. Summary of numerical experiments. The initial DSD aloft is given: MP (Marshall–Palmer), \( \Gamma \) – 1 (first gamma distribution with \( \Lambda = 1.7 \text{ mm}^{-1}, \mu = -0.24 \)), and \( \Gamma \) – 2 (second gamma distribution with \( \Lambda = 2.9 \text{ mm}^{-1}, \mu = 0.73 \)). The idealized wind profiles are indicated (the amplitudes of the quarter-circle hodographs are listed) along with the storm motion \( u \) and \( v \) components. The 0.4–3.0-km SRH calculated from the idealized hodographs and the maximum simulated \( Z_{DR} \) (dB) for each experiment are listed.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>DSD</th>
<th>Environmental shear profile</th>
<th>Storm motion ((u, v)) in m s(^{-1})</th>
<th>0.4–3.0-km SRH</th>
<th>Maximum (Z_{DR}) (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>MP</td>
<td>No wind</td>
<td>(0, 0)</td>
<td>0</td>
<td>1.9</td>
</tr>
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<td>1</td>
<td>MP</td>
<td>Unidirectional shear</td>
<td>(15, 0)</td>
<td>0</td>
<td>4.2</td>
</tr>
<tr>
<td>2</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(5, 0)</td>
<td>87.2</td>
<td>3.6</td>
</tr>
<tr>
<td>3</td>
<td>MP</td>
<td>Quarter circle, 15 m s(^{-1})</td>
<td>(10, 0)</td>
<td>159.4</td>
<td>4.5</td>
</tr>
<tr>
<td>4</td>
<td>MP</td>
<td>9 May 2003</td>
<td>(18.2, 7.0)</td>
<td>197.7</td>
<td>4.5</td>
</tr>
<tr>
<td>5</td>
<td>MP</td>
<td>Quarter circle, 2 m s(^{-1})</td>
<td>(0, 0)</td>
<td>5.4</td>
<td>2.3</td>
</tr>
<tr>
<td>6</td>
<td>MP</td>
<td>Quarter circle, 3 m s(^{-1})</td>
<td>(0, 0)</td>
<td>12.2</td>
<td>2.5</td>
</tr>
<tr>
<td>7</td>
<td>MP</td>
<td>Quarter circle, 6 m s(^{-1})</td>
<td>(3, 0)</td>
<td>31.4</td>
<td>2.8</td>
</tr>
<tr>
<td>8</td>
<td>MP</td>
<td>Quarter circle, 7 m s(^{-1})</td>
<td>(3, 0)</td>
<td>46.1</td>
<td>2.8</td>
</tr>
<tr>
<td>9</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(7, 0)</td>
<td>67.6</td>
<td>2.9</td>
</tr>
<tr>
<td>10</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(6, 0)</td>
<td>77.4</td>
<td>3.8</td>
</tr>
<tr>
<td>11</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(4, 0)</td>
<td>96.9</td>
<td>3.8</td>
</tr>
<tr>
<td>12</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(3, 0)</td>
<td>106.7</td>
<td>3.4</td>
</tr>
<tr>
<td>13</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(2, 0)</td>
<td>116.5</td>
<td>4.5</td>
</tr>
<tr>
<td>14</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(1, 0)</td>
<td>126.3</td>
<td>4.1</td>
</tr>
<tr>
<td>15</td>
<td>MP</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(0, 0)</td>
<td>136.1</td>
<td>4.5</td>
</tr>
<tr>
<td>16</td>
<td>MP</td>
<td>Quarter circle, 15 m s(^{-1})</td>
<td>(5, 0)</td>
<td>232.0</td>
<td>4.5</td>
</tr>
<tr>
<td>17</td>
<td>( \Gamma ) – 1</td>
<td>No wind</td>
<td>(0, 0)</td>
<td>0.0</td>
<td>2.0</td>
</tr>
<tr>
<td>18</td>
<td>( \Gamma ) – 1</td>
<td>Quarter circle, 7 m s(^{-1})</td>
<td>(3, 0)</td>
<td>46.1</td>
<td>3.1</td>
</tr>
<tr>
<td>19</td>
<td>( \Gamma ) – 1</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(5, 0)</td>
<td>87.2</td>
<td>3.7</td>
</tr>
<tr>
<td>20</td>
<td>( \Gamma ) – 1</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(1, 0)</td>
<td>126.3</td>
<td>4.2</td>
</tr>
<tr>
<td>21</td>
<td>( \Gamma ) – 1</td>
<td>Quarter circle, 15 m s(^{-1})</td>
<td>(10, 0)</td>
<td>159.4</td>
<td>4.5</td>
</tr>
<tr>
<td>22</td>
<td>( \Gamma ) – 2</td>
<td>No wind</td>
<td>(0, 0)</td>
<td>0</td>
<td>1.1</td>
</tr>
<tr>
<td>23</td>
<td>( \Gamma ) – 2</td>
<td>Quarter circle, 7 m s(^{-1})</td>
<td>(3, 0)</td>
<td>46.1</td>
<td>3.2</td>
</tr>
<tr>
<td>24</td>
<td>( \Gamma ) – 2</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(5, 0)</td>
<td>87.2</td>
<td>4.0</td>
</tr>
<tr>
<td>25</td>
<td>( \Gamma ) – 2</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(1, 0)</td>
<td>126.3</td>
<td>4.0</td>
</tr>
<tr>
<td>26</td>
<td>( \Gamma ) – 2</td>
<td>Quarter circle, 10 m s(^{-1})</td>
<td>(0, 0)</td>
<td>136.1</td>
<td>4.0</td>
</tr>
</tbody>
</table>

Processes that instigate tornado genesis. Instead, the extension toward the updraft may mark increased low-level inflow that augments the wind shear, coincident with increasing low-level vorticity that precedes the occlusion.

In contrast, the \( Z_{DR} \) arc often becomes “disrupted” by the hail signature, defined here as \( Z_{DR} \) values near 0 dB associated with \( Z_{HH} \) greater than 50 dBZ, once the occlusion takes place. The hail signature is a manifestation of large hailstones with statistically isotropic scattering properties that dominate the contributions from raindrops and smaller wet hailstones within the radar sampling volume (Fig. 12). Such hail signatures are quite common in the FFD core, especially in nontornadic supercells (Kumjian and Ryzhkov 2008). It appears as if the weakening of the updraft associated with the occlusion may diminish the low-level inflow, perhaps disrupting the size sorting that produces the \( Z_{DR} \) arc near the updraft.

Both tornadic and nontornadic supercells exhibit the \( Z_{DR} \) arc. However, there is some indication based on observations from KOUN that the \( Z_{DR} \) arc signature is disrupted more consistently in nontornadic supercells.

It is possible that the consistent disruption of the \( Z_{DR} \) arc by a hail signature indicates that FFD outflow may be partially “undercutting” the updraft in a manner similar to that described by Brooks et al. (1993). This is because the hail signature marks a heavy precipitation core that has substantial amounts of liquid water inferred from very large \( K_{DP} \) values. Precipitation-induced drag, melting of hail and graupel, and evaporation of raindrops contribute to downward velocities, so these cores are generally associated with surface divergence. More observations are required to confirm or refute this suggestion, however; at present it remains speculative.

2) LEFT-MOVING SUPERCELLS

As convective storms develop midlevel rotation, dynamic effects due to the presence of vertical vorticity aloft promote updraft growth on the flanks of the storm, elongating and eventually splitting the main updraft (see Klemp and Wilhelmson 1978; Rotunno and Klemp 1982, 1985; Klemp 1987). This preferential growth on the flanks of the storm may lead the observed storm...
echoes to “split” into left-moving and right-moving members in which the storm motion for each member deviates from the mean tropospheric wind. In instances of such storm splitting, the size sorting hypothesis predicts that an enhancement should be found on the north flank (inflow side) of the left split. In these cases, the left-moving storm motion vector can be found on the opposite side of the hodograph from the right moving member, such that the storm-relative winds have a northerly component and back with height (Fig. 13). The hodograph in Fig. 13 has been modified from the observed 20 May 2003 KOUN sounding from 0000 UTC. The observed sounding was taken approximately 1 h after a cold front passage and thus was not representative of the environment in which the supercells formed. The KOUN surface wind just before the cold front arrival was used instead, and the lowest-level wind observations that were contaminated by the front were omitted. The hodograph is used for illustrative purposes only; because of these subjective modifications, no quantitative calculations were performed.

The expected size sorting would result in an enhancement of $Z_{DR}$ on the north side of the storm. The storm-relative hodograph indicates negative SRH, and we anticipate an analogous relation between negative SRH and the strength of the $Z_{DR}$ arc. In fact, a $Z_{DR}$ arc is observed on the north flank of the anticyclonic storm (Fig. 14). This has been seen in data from 8 May 2003, 19 May 2003, 24 May 2004, 10–11 April 2005, and 10–11 April 2007. We speculate that a left mover with a strong $Z_{DR}$ arc, which indicates a substantial amount of negative SRH, may be long-lived and more conducive to large hail formation because of the sustenance of the mesoanticyclone. Lilly (1986) showed for idealized conditions that supercells may promote their own longevity. According to Lilly, the flow within supercell updrafts is characterized by high helicity, which may inhibit turbulent energy dissipation. For purely helical (Beltrami) flow, this turbulent energy cascade is
completely blocked. By analogy, a strong mesoanticyclone in a left mover may promote the storm’s longevity.

b. Developing supercell and nonsupercell storms

The $Z_{DR}$ arc is a signature intrinsic to supercell storms, but it can be useful in diagnosing nonsupercell storms that are transitioning into a supercellular mode or for identifying nonsupercell severe storms that take on supercell characteristics. On 8 May 2003 the $Z_{DR}$ arc was observed for the first time in one of the storms as it began to transition into a supercell; this storm later went on to produce a damaging F-4 tornado in the Oklahoma City area (Romine et al. 2008). In at least three storms analyzed for this study (8 May 2003; 10 November 2004; 23 April 2008), the $Z_{DR}$ arc appears before the development of the hook echo. Off-hodograph propagation of storms or storms that develop in helical environments should encounter wind shear conducive to the appearance of the $Z_{DR}$ arc prior to the development of strong low-level rotation and the hook echo.

The signature has been observed in a few nonsupercell storms that went on to produce tornadoes (19 August 2005 near King City, Canada; 9 May 2007 in El Reno, Oklahoma; 15 November 2006 in southeastern Alabama). Data from these events are presented in Kumjian and Ryzhkov (2007, 2008), and Schenkman et al. (2008a,b) investigated the evolution of the El Reno event in detail. In each case, a particular cell embedded within a larger mesoscale convective system developed a $Z_{DR}$ arc, indicating locally enhanced shear and SRH. This could be due to local variations in the environmental winds or some change in motion of the particular storm cell such that the storm-relative flow is enhanced. The cells that developed the signature produced the most significant reported severe weather in the mesoscale convective system.

5. Discussion and conclusions

It is documented that supercells can alter their nearby environment, especially the low-level winds (e.g., Browning 1964; Bluestein et al. 1988; Dowell and Bluestein 1997). Using observations from an instrumented tower, Dowell...
and Bluestein (1997) show strong vertical wind shear in the lowest 500 m that increased as a supercell approached. Their measurements from the edge of the FFD where the $Z_{DR}$ arc is normally found indicated shear on the order of 0.01 s$^{-1}$. Such measurements of strong low-level shear have also been made by mobile Doppler radars (e.g., Bluestein and Pazmany 2000).

Because the storms can influence their environments, the low-level shear and SRH could be potentially enhanced because of strong inflow. Because synoptic observations rarely sample the environment very near the storm, and because of the aforementioned significant variability in SRH, it is imperative for forecasters to assess any changes in the local environment due to the storm itself. The $Z_{DR}$ arc may be a way to estimate local enhancements of shear and SRH.

From the alignment of the $Z_{DR}$ arc, one can roughly approximate the mean storm-relative wind direction of the 1–2-km layer just above the observed signature, which should be more or less perpendicular to the major axis of the $Z_{DR}$ arc. In a qualitative sense, the wind speed can be inferred as well (stronger winds cause more size sorting and thus a greater enhancement of $Z_{DR}$). By using this information in addition to the storm motion and surface wind speed, one can piece together a conceptual schematic of how the low-level hodograph, and thus SRH, is related to the $Z_{DR}$ arc signature (Fig. 15). This conceptual framework could be used to make a qualitative estimate of the SRH at low levels. The storm motion can be estimated by tracking radar echoes from previous volume scans. Observations of the surface wind from stations near the storm inflow environment should be used to estimate the surface wind vector. Thus, the low-level SRH can be roughly estimated by combining the surface wind vector, storm motion vector, and estimated storm-relative winds in the layer immediately above the $Z_{DR}$ arc. This method is similar to the one advocated in Davies-Jones et al. (1990) and may be particularly useful in situations in which the radiosonde observations are spatially and/or temporally unrepresentative of the storm inflow environment.

The results from this paper indicate that a positive relation exists between the magnitude of the $Z_{DR}$ values in the arc signature and the low-level SRH. Increasing wind shear will increase the amount of size sorting that occurs, which subsequently manifests itself as an increase in $Z_{DR}$. Because SRH takes wind shear into account with other factors, generally there should be a positive relation for supercells or storms with motion off the hodograph. Obviously one can envision situations of large shear but low SRH in which the relation may not hold, so the relation is not perfect. Nonetheless, the relation between a radar observation and strong wind shear (and subsequently SRH) is potentially important, especially when the measurement...
is made at the storm location. We are not claiming that all $Z_{\text{DR}}$ enhancements are related to SRH; in fact, the $Z_{\text{DR}}$ arc signature appears to be unique in that such a relation evidently exists.

In summary,

1) Size sorting due to speed and directional wind shear, which can be augmented by low-level inflow, results in an enhancement of $Z_{\text{DR}}$ along the edge of the storm’s FFD precipitation echo, generally along a gradient in $Z_{\text{HH}}$. The location, shape, shallowness, and alignment of this signature, called the $Z_{\text{DR}}$ arc, are distinct among other size-sorting induced enhancements of $Z_{\text{DR}}$.

2) Increased storm-relative wind speed and directional shear tend to increase the area swept out by the hodograph, enhancing the SRH. As low-level SRH values increase, the size sorting due to the enhanced storm-relative wind shear generally increases. This results in larger $Z_{\text{DR}}$ values in the arc signature. The conceptual model presented here suggests a positive relation between low-level SRH values and the magnitude of the $Z_{\text{DR}}$ in the signature. Idealized numerical simulations have verified this positive relation, and observational evidence supporting the conceptual model is discussed.

3) In both tornadic and nontornadic supercells, the $Z_{\text{DR}}$ arc tends to extend to the updraft region in times leading up to the occlusion of the low-level mesocyclone. Once the occlusion takes place, the $Z_{\text{DR}}$ arc appears to be disrupted by a hail signature. There is some indication that in nontornadic supercells the $Z_{\text{DR}}$ arc signature is disrupted more persistently, possibly indicating that outflow from the FFD is interfering with processes necessary for tornadogenesis.

4) Because the $Z_{\text{DR}}$ arc is measured within the storm, it characterizes the immediate inflow environment well and could potentially be employed to refine estimates of low-level SRH.

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