Formation of massive globular clusters with heavy element abundance spread in the Galactic building blocks

Kenji Bekki

ICRAR M468, The University of Western Australia, 35 Stirling Hwy, Crawley, WA 6009, Australia

Accepted 2011 November 30. Received 2011 November 26; in original form 2011 November 10

ABSTRACT
A growing number of recent observations have revealed that the Galactic globular cluster (GC) ω Cen is not the only GC that shows abundance spread in heavy elements (e.g. Fe). In order to understand the origin of the Galactic GCs with heavy element abundance spread (HEAS), we investigate the formation processes of massive GCs (MGCs) with masses larger than $10^6 M_\odot$ in gas-rich dwarf galaxies interacting and merging with the very young Galaxy. We find that massive and compact stellar clumps with masses larger than $10^6 M_\odot$, which can be regarded as progenitors of MGCs, can form from massive gas clumps that are developed through merging of gaseous regions initially at different radii and thus with different metallicities. Therefore, it is inevitable that MGCs formed in dwarfs have HEAS. The abundance spread in each individual MGC depends on the radial metallicity gradient of the host dwarf such that it can be larger for the steeper metallicity gradient. For example, MGCs formed in a dwarf with a central metallicity of $[\text{Fe}/\text{H}]=-1.1$ and the radial gradient of $\sim-0.2 \text{ dex kpc}^{-1}$ can have the abundance spread of $\Delta[\text{Fe}/\text{H}] \sim 0.2$. The simulated MGCs appear to be significantly flattened owing to their dissipative formation from gas discs of their host dwarfs. Based on these results, we discuss possibly diverse formation mechanisms for the Galactic GCs such as M22, M54, NGC 2419, ω Cen and Terzan 5.

Key words: stars: formation – globular clusters: general – galaxies: star clusters: general – galaxies: stellar content.

1 INTRODUCTION

One of the remarkable recent developments in observational studies of the Galactic globular clusters (GCs) is that most of the investigated GCs show varying degrees of chemical abundance spread: helium abundance spread in ω Cen and NGC 2808 (e.g. Bedin et al. 2004; Piotto et al. 2007), a larger dispersion in s-process elements abundances in NGC 1851 (e.g. Yong & Grundahl 2008; Milone et al. 2011), abundance spread in light element in ‘normal’ GCs (e.g. Carretta et al. 2010) and heavy element abundance spread (HEAS) in M22, Terzan 5 and NGC 2419 (e.g. Da Costa et al. 2009; Ferraro et al. 2009; Marino et al. 2009; Cohen et al. 2010). Lee et al. (2009) investigated colour–magnitude diagrams of stars in $hk$ bands for the Galactic GCs and suggested that a significant fraction of the Galactic GCs have two different populations with HEAS (but see also Marino et al. 2009; Carretta et al. 2010, for similar and different claims).

The origin of the HEAS in ω Cen has been discussed by theoretical models in the context of formation and evolution of stellar galactic nuclei in dwarfs (‘the stripped nucleus scenario’; e.g. Bekki & Freeman 2003; Romano et al. 2010). Since stellar populations of stellar galactic nuclei can have different metallicities and ages owing to their possible formation by merging of different stellar and gaseous clumps (e.g. Bekki 2007), it would not be so surprising that ω Cen is observed to have HEAS owing to its possible origin from the stellar nucleus of its host dwarf. Also, it would be possible that the formation process of other GCs with HEAS (e.g. Terzan 5) can be different from that of ω Cen (e.g. GC mergers; Bekki & Yong 2011, hereafter BY11; Brüns & Kroupa 2011). Ideally speaking, chemodynamical simulations of GC formation based on a theoretical model are essential for discussing both the formation processes of GCs from gas and the resultant internal chemical abundance spread within GCs in a fully self-consistent manner. However, no chemodynamical simulations on the origin of GCs with HEAS (other than ω Cen) have been done so far.

The purpose of this Letter is to clearly show whether and how GCs with HEAS can be formed by using chemodynamical simulations of GC formation processes based on a GC formation scenario. We here consider that most of the Galactic GCs were formed in galactic building blocks (e.g. Searle & Zinn 1978), in particular when they were interacting and merging with the very young Galaxy (> 10 Gyr...
ago). We focus exclusively on $\text{[Fe/H]}$ spread ($\Delta\text{[Fe/H]}$) in massive GCs (MGCs) with masses as large as or larger than $10^6 \, M_\odot$ formed within their host dwarfs (i.e. galactic building blocks).

2 THE MODEL

We numerically investigate star formation and chemical evolution processes of a gas-rich dwarf interacting and merging with the Galaxy in order to investigate whether MGCs composed of many stellar particles can be formed. In order to simulate chemodynamical evolution of the gas-rich dwarf in the young Galaxy, we use both the latest version of GRAPE (GRAVity PipE, GRAPE-DR), which is the special-purpose computer for gravitational dynamics (Sugimoto et al. 1990), and high-end PCs with GPU cards (GTX 580) and CUDA G5/G6 software package being installed for calculations of gravitational dynamics. We adopt our original GRAPE-SPH code (Bekki 2009) which combines the method of smoothed particle hydrodynamics with GRAPE for calculations of three-dimensional self-gravitating fluids in astrophysics.

The dwarf galaxy is assumed to be strongly influenced by the fixed gravitational potential of the Galaxy in the present study. We adopt a model of the Galaxy similar to that used in BY11 in which the Galaxy is assumed to have three components: a dark matter halo, a disc and a bulge. We consider that (i) dwarfs forming and hosting GCs interact or merge with the Galaxy in the very early history of the Galaxy formation (>10 Gyr ago) and thus (ii) the Galaxy has not yet fully developed its halo, disc and bulge components at the epoch of dwarf merging.

We assume the following logarithmic dark matter halo potential for the Galaxy:

$$\Phi_{\text{halo}} = v_{\text{halo}}^2 \ln(r^2 + d^2),$$

where $d = 12$ kpc, $v_{\text{halo}} = 131.5$ km s$^{-1}$ and $r$ is the distance from the centre of the Galaxy. The gravitational potential of the Galactic disc is represented by a Miyamoto & Nagai (1975) potential:

$$\Phi_{\text{disc}} = -\frac{GM_{\text{disc}}}{\sqrt{R^2 + (a + \sqrt{z^2 + R^2})^2}},$$

where $M_{\text{disc}} = 1.0 \times 10^10 \, M_\odot$, $a = 6.5$ kpc, $b = 0.26$ kpc and $R = \sqrt{x^2 + y^2}$. The disc mass is much smaller than the one adopted in BY11, because we consider that only the first generation of the thin disc is being built when the dwarf starts interacting/merging with the Galaxy (>10 Gyr ago). We do not include the bulge in the young Galaxy, because we consider that the bulge can be formed much later from bar instability of disc stars.

The centre of the Galaxy is always set to be $(x, y, z) = (0, 0, 0)$, whereas the initial location and velocity of the dwarf are free parameters that can control the orbital evolution of the dwarf. The initial distance of the dwarf from the Galactic Centre and the velocity are represented by $R_i$ and $v_i$, respectively, where $v_i$ is the circular velocity at $R_i$. The inclination angle between the initial orbital plane and the $x$-$z$ plane (= Galactic disc plane) is denoted as $\theta$. The initial spin of the dwarf is specified by two angles, $\theta_0$ and $\phi_0$, where $\theta$ is the angle between the $z$-axis and the vector of the angular momentum of a disc and $\phi$ is the azimuthal angle measured from $x$-axis to the projection of the angular momentum vector of a disc on to the $x$-$y$ plane. In the present study, we show the results of the models with $R_i = 35$ kpc, $f_i = 0.5$, $\theta = 30^\circ$, $\theta_0 = 15^\circ$ and $\phi_0 = 45^\circ$.

We adopt the same dwarf galaxy model as that in BY11: the dwarf has a ‘cored’ dark matter halo (Salucci & Burkert 2000) and an exponential stellar disc. We describe the result of the models with the total stellar disc masses ($M_{d, \text{tw}}$) being $10^7 \, M_\odot$ in the present study: other models with different $M_{d, \text{tw}}$ will be discussed in our forthcoming papers. The mass ratio of dark matter halo to stellar disc in the dwarf is set to be 9 and thus the core radius ($a_{\text{core}}$) of the dark matter halo is 1.5 kpc. The stellar disc has the total mass of $M_{d, \text{tw}}$ and the size of $R_{d, \text{tw}}$, and the radial ($R$) and vertical ($Z$) density profiles of the stellar disc are assumed to be proportional to $\exp(-R/R_0)$ with scale length $R_0 = 0.2R_{d, \text{tw}}$ and to $\text{sech}^2(Z/Z_0)$ with vertical scale height $Z_0 = 0.04R_{d, \text{tw}}$, respectively. In addition to the rotational velocity caused by the gravitational field of disc and dark halo components, the initial radial and azimuthal velocity dispersions are assigned to the disc component according to the epicyclic theory with Toomre’s parameter $Q = 1.5$. The vertical velocity dispersion at a given radius is set to be 0.5 times as large as the radial velocity dispersion at that point.

In the present study, the dwarf also has an extended gas disc with the total mass of $M_{d, \text{tw}}$ and the size of $R_{d, \text{tw}}$ ($=2.5R_{d, \text{tw}}$). The disc is assumed to have an exponential profile with scale length $0.4R_{d, \text{tw}}$ and vertical scale height $0.04R_{d, \text{tw}}$. The mass ratio of gas disc to stellar one ($f_g$) is an important free parameter that can control the formation processes of MGCs in the present study. We consider that the dwarf disc initially has a plenty of cold gas and accordingly an isothermal equation of state is adopted for the gas with a temperature ($T_g$) of 160 K. Star formation is modelled by converting the collisional gas particles into collisionless new stellar particles according to the algorithm of star formation described below. We adopt the Schmidt law with exponent $y = 1.5$ ($1.0 < y < 2.0$; Kennicutt 1989) as the controlling parameter of the rate of star formation.

We allocate metallicity to each gas particle according to its initial position: at $r = R$, where $r$ is the projected distance (in units of kpc) from the centre of the disc, and thus the metallicity of the gas is given as

$$\text{[Fe/H]}_{\text{gas}} = \text{[Fe/H]}_{\text{d, tw}} + \alpha_d \times R.$$  

We consider that (i) the slope $\alpha_d$ is a free parameter and (ii) $\text{[Fe/H]}_{\text{d, tw}}$ is determined by the total stellar mass of the dwarf. Accordingly, we adopt $\text{[Fe/H]} = -1.1$ as a reasonable value for the adopted $M_{d, \text{tw}}$, and the observed value of $\alpha_d$ $\sim$ –0.2 for dwarf spirals (Hidalgo-Gámez, Ramirez-Fuentes & Gonzalez 2010) should be a reference value for the radial metallicity gradient. The chemical yield $\eta_{\text{met}}$ and the return parameter $R_{\text{ret}}$ are key parameters that control chemical evolution of dwarfs. We investigate models with (i.e. $\eta_{\text{met}} > 0$ and a fixed $R_{\text{ret}} = 0.3$) and without ($\eta_{\text{met}} = 0$) chemical enrichment by supernovae.

In order to find massive stellar clumps with masses ($m_{\text{clump}}$) as large as or larger than $10^6 \, M_\odot$, we investigate the total number of new stellar particles ($N_{\text{new}}$) within 200 pc around each new stellar particle. If $N_{\text{new}}$ around a new stellar particle is larger than a threshold value $n_{\text{thresh}}$, then we regard the particle as being within a massive and compact stellar clump. Since the particle is not necessarily at the centre of the clump, we newly determine the centre of the clump using the position data of the neighbouring particles around the particle. For the newly determined centre of the clump, we estimate the total mass of the clump within the central 200 pc. We consider that $n_{\text{thresh}} = 1000$ is reasonable, first because only massive clumps ($m_{\text{clump}} \geq 5 \times 10^5 \, M_\odot$ for $f_g = 0.5$) can be selected and secondly because the selected clumps also show high stellar densities.

The selected massive clumps are significantly larger and more massive than the present GCs and thus should be regarded as progenitors of GCs (i.e. not literally genuine GCs). Recent numerical
in the present Letter. We mainly describe the results of the ‘standard’ model (M1) in which $f_g = 0.5$, $\alpha_d = -0.2$ and chemical enrichment is not included (i.e. $\gamma_{\text{met}} = 0$). This is mainly because we need to more clearly demonstrate the origin of HEAS in GCs. The total particle numbers for the dark matter ($N_{\text{dm}}$), the stellar disc ($N_s$) and the gas one ($N_g$) used in most of the present models are 200,000, 200,000 and 100,000, respectively. The gravitational softening lengths ($\epsilon$) for the dark matter particles, the stellar ones and the gaseous ones are 128, 20 and 20 pc, respectively. In order to confirm that the present results do not depend on the adopted numerical resolution, we also run a high-resolution model (H1) in which $N_{\text{dm}} = 400,000$, $N_s = 400,000$ and $N_g = 200,000$.

### 3 RESULTS

Fig. 1 shows the orbital evolution of the dwarf and the time evolution of the mass distributions of gas and new stars in the standard model (M1). During the first pericentre passage ($R_p \sim 14$ kpc) at $T \sim 0.3$ Gyr, the gas disc is strongly compressed by the tidal field of the Galaxy to form high-density gaseous regions. As a result of this, a number of massive clumps composed mostly of gas and new stars can be formed within the central $\sim 1$ kpc of the dwarf and the star formation rate becomes higher ($\sim 0.08$ $M_\odot$ yr$^{-1}$). After the pericentre passage, a significant fraction of gas and new stars are tidally stripped and the stripped matter can form leading and trailing streams along the orbit of the dwarf ($T = 0.7$ Gyr). Some of the more massive clumps can sink into the central region of the dwarf owing to dynamical friction so that they can become stellar galactic nucleus. At the final time step ($T = 1.7$ Gyr), only one massive and compact clump (identified as MGC3) with $m_\text{ms} = 1.2 \times 10^8$ $M_\odot$ (originally $1.6 \times 10^8$ $M_\odot$ at $T = 1.0$ Gyr) can be clearly seen within the central 1 kpc of the dwarf. We confirm that this MGC3 can sink into the dwarf’s centre within the next $\sim 1$ Gyr to become nucleus: it can be identified as an isolated GC only after

---

**Table 1. Description of the model parameters for the representative models.**

<table>
<thead>
<tr>
<th>Model no.$^a$</th>
<th>$M_{s,\text{dw}}$</th>
<th>$R_{s,\text{dw}}$</th>
<th>$f_g$</th>
<th>$\alpha_d$</th>
<th>$\gamma_{\text{met}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.2</td>
<td>-</td>
</tr>
<tr>
<td>M2</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.1</td>
<td>-</td>
</tr>
<tr>
<td>M3</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.05</td>
<td>-</td>
</tr>
<tr>
<td>M4</td>
<td>1.0</td>
<td>1.8</td>
<td>0.1</td>
<td>-0.2</td>
<td>-</td>
</tr>
<tr>
<td>M5</td>
<td>1.0</td>
<td>1.8</td>
<td>0.2</td>
<td>-0.2</td>
<td>-</td>
</tr>
<tr>
<td>M6</td>
<td>1.0</td>
<td>2.8</td>
<td>0.5</td>
<td>-0.2</td>
<td>0.0005</td>
</tr>
<tr>
<td>M7</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.2</td>
<td>0.002</td>
</tr>
<tr>
<td>M8</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.2</td>
<td>-</td>
</tr>
<tr>
<td>H1</td>
<td>1.0</td>
<td>1.8</td>
<td>0.5</td>
<td>-0.2</td>
<td>-</td>
</tr>
</tbody>
</table>

*a* Only the model H1 is the higher resolution model with $N = 10^6$.

*b* The total mass of a stellar disc in a dwarf in units of $10^8$ $M_\odot$.

*c* The initial size of a stellar disc in a dwarf in units of kpc.

*d* The radial metallicity gradient of the gas disc in a dwarf (dex kpc$^{-1}$).

*e* The value of a chemical yield ($\gamma_{\text{met}}$) is not shown for models without chemical evolution.

---

**Figure 1.** The time evolution of the mass distribution of the dwarf with respect to the Galactic Centre (left four) and to the dwarf’s centre (right four) projected on to the $x$–$y$ plane for the standard model (M1). Gas and new stars are shown by cyan and magenta, respectively, and $T$, which is the time that has elapsed since the simulation started, is shown in the upper left corner in units of Gyr for each panel. The green lines in the four left-hand panels represent the orbit of the dwarf. The locations of MGC1, 2 and 3 are indicated by blue, red and green circles at $T = 1.7$ Gyr, respectively.

---

*K. Bekki*
They can be finally regarded as ‘isolated’ GCs owing to such that 

The orbits of the dwarf (left three) and the mass distributions of MGC2 (right three) projected on to the $x$–$y$ (top), $x$–$z$ (middle) and $y$–$z$ planes (bottom) in the standard model (M1). For comparison, the locations of the dwarf and MGC2 at $T = 1.7$ Gyr are shown by green and magenta circles, respectively. Only new stars formed from gas are plotted in the three right-hand panels.

the complete destruction of its host by the (older) Galaxy with the much larger mass.

Two stellar clumps can be developed from gaseous tidal tails (or outer spiral arms) during the tidal interaction of the dwarf with the Galaxy. Fig. 1 shows that the two clumps (i.e. MGC progenitors) can be stripped from their host dwarf and consequently located within the gaseous tails ($T = 1.7$ Gyr). These two clumps are identified as MGC1 with $m_{ns} = 7.5 \times 10^5$ $M_{\odot}$ and MGC2 with $m_{ns} = 1.3 \times 10^5$ $M_{\odot}$. They can be finally regarded as ‘isolated’ GCs owing to their large distances (>40 kpc) from the dwarf. Fig. 2 shows that owing to its formation from the outer gas disc through gaseous dissipation, MGC2 has a significantly flattened shape in the $x$–$y$ projection. This flattened shape can be seen in most of the simulated MGCs in the present study.

The formation of MGCs can be severely suppressed in models (M4 and 5) with lower $f_{z} (\leq 0.2)$, which implies that MGC formation is possible only when their host dwarfs have a plenty of cold gas. Therefore, the formation processes of MGCs in gas-rich discs and tidal tails described above can be essentially the same as those of massive stellar and gaseous clumps discussed in previous papers (e.g. Noguchi 1999; Bournaud, Elmegreen & Elmegreen 2007) in which $f_{z}$ is a fundamentally important parameter for dynamical evolution of gas-rich galactic discs. MGCs can be formed even in the low surface brightness model M6 with larger $R_{dw} (= 2.8$ kpc), which implies that mass densities of stellar discs in dwarfs are not so important as $f_{z}$ for MGC formation.

Fig. 3 clearly shows that new stars of MGC2 originate from gaseous regions at different locations within the dwarf and thus with different [Fe/H] owing to the adopted metallicity gradient of the gas disc. This result demonstrates that some Galactic GCs have HEAS because they formed from massive gaseous clumps developed from merging of different gaseous regions with different initial [Fe/H]. However, Fig. 4 shows that the degree of HEAS ($\Delta$[Fe/H]) depends strongly on $\alpha_d$ such that $\Delta$[Fe/H] is larger ($\sim 0.2$ dex) for the steeper metallicity gradient (i.e. the larger absolute magnitude of $\alpha_d$).

Fig. 5 shows that a younger population can have [Fe/H] $\sim −1$ in MGC2 in the model with chemical evolution (M7), though the mass fraction of the population with the age less than 0.2 Gyr is only $\sim 0.05$. Although the prolonged star formation can be seen, the vast majority of stars are formed in a burst at the epoch of massive clump formation. Furthermore, there appears to be an age–metallicity relation that younger stars are more metal rich in MGC2. It should be stressed that the relation can depend on how the supernova ejecta can influence the later star formation within cluster-forming massive gas clumps, which needs to be investigated by more sophisticated
models in our future works. The [Fe/H] spread could be overestimated owing to the adopted instantaneous recycling approximation. The mean metallicities and internal [Fe/H] spread of MGCs are larger in models with larger $y_{\text{met}}$ (e.g. M8) in the present study. The physical properties of MGCs (e.g. masses and locations) are not different between models with different numerical resolutions (M1 and H1).

4 DISCUSSION AND CONCLUSIONS

The present chemodynamical study has first demonstrated that MGCs with HEAS can be formed from massive gas clumps developed from merging of different gaseous regions with different metallicities. Therefore, MGCs with HEAS can be formed even without chemical enrichment by supernovae during their formation. The present study suggests that more MGCs are more likely to have a larger degree of HEAS owing to their formation from gas clouds developed from merging between a larger number of different gaseous regions with different metallicities. The low-mass GCs can be formed from single gas clouds so that they are likely to have no/little HEAS. The present study thus suggests that the origin of HEAS in some Galactic GCs can be closely associated with HEAS of interstellar medium in their host dwarfs.

The large metallicity spread of various elements and possible age variation in $\omega$ Cen (e.g. Sollima et al. 2005) can be consistent with the stripped nucleus scenario. However, this does not necessarily mean that all of the Galactic GCs with HEAS (e.g. NGC 2419, M22 and Terzan 5) were formed from stripped nuclei of dwarfs. A GC with two distinct peaks in the [Fe/H] distributions of the stars might well be consistent with GC merging with different [Fe/H] (e.g. BY11; Brüns & Kroupa 2011). A GC with a smaller degree of HEAS yet no clear bimodal [Fe/H] distribution might well form from massive gas clumps of the host dwarf and then be stripped from the dwarf without sinking into the centre (i.e. without becoming the stellar nucleus) to finally become the Galactic halo GC. We lastly suggest that nucleation, GC merging and merging of gas clouds with different [Fe/H] can be all promising mechanisms for the formation of the Galactic GCs with different degrees of HEAD.

ACKNOWLEDGMENTS

I am grateful to the anonymous referee for constructive and useful comments that improved this Letter.

REFERENCES

Bekki K., 2007, PASA, 24, 77
Ferraro F. R. et al., 2009, Nat, 462, 483
Lee J.-W., Kang Y.-W., Lee J., Lee Y.-W., 2009, Nat, 462, 480
Miyamoto M., Nagai R., 1975, PASJ, 27, 533
Sugimoto D., Chikada Y., Makino J., Ito T., Ebisuzaki T., Umemura M., 1990, Nat, 345, 33

This paper has been typeset from a TeX/LATEX file prepared by the author.