

# Modelling the degradation of endogenous residue and 'unbiodegradable' influent organic suspended solids to predict sludge production

Mathieu Spérandio, Marc-André Labelle, Abdellah Ramdani, Alain Gadbois, Etienne Paul, Yves Comeau and Peter L. Dold

## ABSTRACT

Activated sludge models have assumed that a portion of organic solids in municipal wastewater influent is unbiodegradable. Also, it is assumed that solids from biomass decay cannot be degraded further. The paper evaluates these assumptions based on data from systems operating at higher than typical sludge retention times (SRTs), including membrane bioreactor systems with total solids retention (no intentional sludge wastage). Data from over 30 references and with SRTs of up to 400 d were analysed. A modified model that considers the possible degradation of the two components is proposed. First order degradation rates of approximately  $0.007\text{ d}^{-1}$  for both components appear to improve sludge production estimates. Factors possibly influencing these degradation rates such as wastewater characteristics and bioavailability are discussed.

**Key words** | endogenous residue, long SRT, membrane bioreactor, modelling, sludge production, total solids retention

**Mathieu Spérandio** (corresponding author)  
**Etienne Paul**  
Université de Toulouse; INSA, UPS, INP; LISBP,  
135 Avenue de Rangueil, F-31077 Toulouse,  
France;  
INRA, UMR792 Ingénierie des Systèmes  
Biologiques et des Procédés, F-31400 Toulouse,  
France;  
CNRS, UMR5504, F-31400 Toulouse,  
France  
E-mail: [Spérandio@insa-toulouse.fr](mailto:Spérandio@insa-toulouse.fr)

**Marc-André Labelle**  
**Abdellah Ramdani**  
**Yves Comeau**  
Department of Civil, Geological and Mining  
Engineering,  
Ecole Polytechnique of Montreal, P.O. Box 6079,  
Station Centre-ville, Montreal, Quebec, H3C 3A7,  
Canada

**Alain Gadbois**  
John Meunier Inc., 4105 Sartelon Street,  
Saint-Laurent, Quebec, H4S 2B3,  
Canada

**Peter L. Dold**  
EnviroSim Associates Ltd, McMaster Innovation  
Park, 175 Longwood Rd South, Suite 114A,  
Hamilton, Ontario, L8P 0A1,  
Canada

## INTRODUCTION

Prediction of sludge production is an important issue for wastewater treatment plant (WWTP) modelling, and it is considered a crucial step in calibration of activated sludge models (ASMs). In the theoretical framework of these models (ASM1, ASM2, ASM3) the mixed liquor suspended solids is composed mainly of active microorganisms ( $X_H$ ), inactive/inert particulate organic matter ( $X_U$ ) and inorganic matter ( $X_{I,g}$ ) (Henze *et al.* 2000; symbols according to Corominas *et al.* 2010). Storage compounds are also considered in ASM2, ASM2d and ASM3, and slowly biodegradable organics are also present to a lesser extent. The inert organic matter ( $X_U$ ) originates from the influent ( $X_{U,Inf}$ ) and the accumulation of endogenous residue ( $X_E$ ) from biomass decay. This concept was

initially developed by Marais & Ekama (1976) and Dold *et al.* (1980) for conventional activated sludge processes operating at typical sludge retention times (SRTs), i.e. < 30 d. The terms 'inactive' or 'inert' organic matter are replaced in this paper by the more specific term 'unbiodegradable'.

Several articles deal with the operation of membrane bioreactors (MBRs) at very long SRTs and the concept of MBRs with 'total solids retention', i.e. nearly no solids wastage (Rosenberger *et al.* 2002; Laera *et al.* 2005; Lubello *et al.* 2009). In some of these studies authors reported a zero observed mixed liquor volatile suspended solids (MLVSS) production, suggesting that biomass (active and endogenous residue) production was equilibrated by

biomass decay (or that influent substrate was completely oxidised for cell maintenance). If such systems were stable in terms of MLVSS concentration, it would imply that a significant degradation of  $X_{U,Inf}$  and  $X_E$  occurs. This concept is clearly still controversial, and in opposition to the actual ASM framework. Adaptation of ASM models for MBRs was recently reviewed and the need to include a slow 'hydrolysis' process was pointed out (Spérandio & Espinosa 2008; Fenu *et al.* 2010).

Recent research indicates that sludge production at long SRTs is slightly lower than expected based on models calibrated at conventional SRTs. Several studies point out a need to introduce the degradation of endogenous products ( $X_E$ ) and influent 'unbiodegradable' particulate organics ( $X_{U,Inf}$ ) (Spérandio & Espinosa 2008; Lubello *et al.* 2009; Fenu *et al.* 2010; Ramdani *et al.* 2012). The objective of this article is to discuss these recent findings and to evaluate the predictions of a modified ASM with datasets obtained from MBRs operated over a large range of SRTs.

## THEORETICAL BACKGROUND

Simulated sludge production in conventional activated sludge or MBRs depends *inter alia* on influent organic and inorganic loads and on some core model parameters (mainly  $Y_H$ ,  $f_{XE}$  and  $b_H$ ; Table 1). As SRT increases, the predicted mass of volatile solids in the system (and the observed sludge production) becomes dominated by the unbiodegradable particulate COD (chemical oxygen demand) components  $X_{U,Inf}$  and  $X_E$ .

The expression of sludge production yield (kg VSS/kg COD removed) at steady state based on conventional ASMs (ASM-based model with endogenous respiration concept) is:

$$Y_{OBS} = \left( (1 - f_{XU} - f_{SU}) \cdot \left( \frac{Y_H}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XH}} \right) + \frac{Y_H \cdot b_H \cdot f_{XE} \cdot SRT}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XE}} + \frac{f_{XU}}{f_{cv,XU,Inf}} \right) / (1 - f_{SU}) \quad (1)$$

Parameters definition and typical values are given in Table 1. Equation (1) is developed for aerobic conditions and a single value for the  $Y_H$  coefficient is assumed. Considering different  $Y_H$  values depending on electron acceptor would be more accurate for systems with anaerobic and anoxic conditions.

Table 1 | Typical parameters values

Symbol	Parameter description	Value	Units
$Y_H$	Heterotrophic biomass yield (aerobic)	0.666	g COD/g COD
$b_H$	Decay rate of heterotrophic biomass	0.24	d <sup>-1</sup>
$b_{XE}$	Degradation rate of endogenous particulate 'residue'	0.007	d <sup>-1</sup>
$b_{XU}$	Degradation rate of influent particulate unbiodegradable organics	0.007	d <sup>-1</sup>
$f_{SU}$	Soluble unbiodegradable organics fraction of wastewater COD	0.05 <sup>a</sup>	g COD/g COD
$f_{XU}$	Particulate unbiodegradable organics fraction of wastewater COD	0.08–0.20 <sup>a</sup>	g COD/g COD
$f_{XE}$	Endogenous fraction of biomass (endogenous respiration concept)	0.20	g COD/g COD
$f_{cv,XH}$	Conversion factor for heterotrophic biomass	1.42	g COD/g VSS
$f_{cv,XU,Inf}$	Conversion factor for influent unbiodegradable particulate COD	1.55 <sup>a</sup>	g COD/g VSS
$f_{cv,XE}$	Conversion factor for endogenous residue	1.55	g COD/g VSS

<sup>a</sup>Wastewater dependent.

In the case of synthetic soluble substrates, as  $f_{XU} = 0$  and  $f_{SU} = 0$ , Equation (1) is simplified to:

$$Y_{OBS} = \frac{Y_H}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XH}} + \frac{Y_H \cdot b_H \cdot f_{XE} \cdot SRT}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XE}} \quad (2)$$

If the degradation of endogenous residue is considered as a first order kinetic, the mass balance for  $X_E$  gives:

$$V \frac{dX_E}{dt} = V \cdot f_{XE} \cdot b_H \cdot X_H - V \cdot b_{XE} \cdot X_E - P X_E = 0 \quad (3)$$

where  $V$  is the reactor volume and  $P X_E$  is the wasted endogenous suspended solids.

Then Equation (1) becomes:

$$Y_{OBS} = \left( (1 - f_{XU} - f_{SU}) \cdot \left( \frac{Y_H}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XH}} + \frac{Y_H \cdot b_H \cdot f_{XE} \cdot SRT}{(1 + b_H \cdot SRT)(1 + b_{XE} \cdot SRT)} \frac{1}{f_{cv,XE}} \right) + \frac{f_{XU}}{f_{cv,XU,Inf}} \right) / (1 - f_{SU}) \quad (4)$$

If the degradation of  $X_{U,Inf}$  is introduced, also as a first order kinetics, the mass balance on  $X_{U,Inf}$  is:

$$V \frac{dX_{U,Inf}}{dt} = Q \cdot f_{XU} \cdot T_{Inf,COD} - V \cdot b_{XU,Inf} \cdot X_{U,Inf} - P X_{U,Inf} = 0 \quad (5)$$

where  $T_{Inf,COD}$  is the total influent COD concentration.

Consequently, the observed sludge production yield, considering the degradation of  $X_{U,Inf}$  and  $X_E$ , is expressed (modified ASM model) as:

$$Y_{OBS} = \left( (1 - f_{XU} - f_{SU}) \cdot \left( \frac{Y_H}{(1 + b_H \cdot SRT)} \frac{1}{f_{cv,XH}} + \frac{Y_H \cdot b_H \cdot f_{XE} \cdot SRT}{(1 + b_H \cdot SRT)(1 + b_{XE} \cdot SRT)} \frac{1}{f_{cv,XE}} \right) + \frac{f_{XU}}{(1 + b_{XU,Inf} \cdot SRT)} \frac{1}{f_{cv,XU,Inf}} \right) / (1 - f_{SU}) \quad (6)$$

In this first order kinetic approach, it is implicitly assumed that both  $X_E$  and  $X_{U,Inf}$  can eventually be degraded completely. However, there may be a portion that cannot be degraded at all.

## RESULTS

### Identifying degradation rate of $X_E$ or $X_{U,Inf}$ in batch tests

The degradation rates of  $X_E$  or  $X_{U,Inf}$  were estimated either during long-term digestion (anaerobic or aerobic) or in MBRs (Table 2). A first order kinetic reaction was proposed for these processes for the specific parameters  $b_{XE}$  or  $b_{XU}$ . It is considered essential to accurately evaluate the value of the 'core' parameters  $Y_H$ ,  $f_{XE}$  and  $b_H$  in ASM models (Ramdani 2011).

### Model-based evaluation of sludge yield measurements in MBR literature

Based on a literature review from 30 references covering the last 30 years (Table 3), the excess sludge production in

MBRs was evaluated in terms of both model concepts: with or without the degradation of  $X_E$  and  $X_{U,Inf}$  (Figure 1). Data are provided for MBRs treating both synthetic soluble substrate ( $f_{XU} = 0$ ) and real wastewater (Figure 1(a) and 1(b), respectively). The x axis shows SRT and duration for MBRs operated with solids wastage and with total solids retention, respectively. For MBRs operated at SRTs longer than 50 d, the modified ASM model better predicted sludge production, using a mean degradation rate value of  $0.007 \text{ d}^{-1}$  for both  $b_{XE}$  and  $b_{XU}$ . This result is in agreement with the degradation rate for  $b_{XE}$  determined by Ramdani *et al.* (2012).

Obviously a significant variability is observed in the data from literature and this should not be considered as a definitive rate value. Variability can be related to the wastewater characteristics (or type of synthetic carbon source), the presence of anoxic and anaerobic conditions and the temperature variations in the case of full-scale data. Analysis of available data obtained at long SRT or total solids retention indicates that applying degradation rates for endogenous residue ( $b_{XE}$ ) in the range  $0.0035\text{--}0.017 \text{ d}^{-1}$  may improve predictions of sludge production depending on the data (cross-flow filtration versus submerged membrane filtration; laboratory-scale versus full-scale systems). Higher degradation rates were obtained mostly from the cross-flow mode of operation, which could be explained by a higher shear stress resulting in some sludge disintegration.

The values of  $f_{XU}$  which give exactly the same sludge production yield with Equation (1) (ASM based) and Equation (6) (modified ASM) are shown in Figure 2. For example at an SRT of 20 d, the same  $Y_{OBS}$  is predicted with  $f_{XU} = 0.16$  for the conventional model (Equation (6)) and with  $f_{XU} = 0.20$  for the model which includes degradation of  $X_{U,Inf}$  and  $X_E$  (Equation (6)). With the conventional model,  $f_{XU}$  should be reduced to less than 0.10 at an SRT of 60 d, and  $f_{XU}$  should tend theoretically towards zero at SRTs greater than 200 d in order to predict the same sludge production as by the modified model. In contrast, this last model, including the degradation of

**Table 2** | Degradation rate constants estimated for  $X_E$  or  $X_{U,Inf}$

Parameter	$b_{XE}$	$b_{XE}$	$b_{XE} + b_{XU}$	$b_{XE} + b_{XU}$
References	Ramdani <i>et al.</i> (2010)	Ramdani <i>et al.</i> (2012)	Lubello <i>et al.</i> (2009)	Jones <i>et al.</i> (2007)
Conditions	Batch, 35 °C	MBR, 20 °C	MBR, 20 °C	Batch, 35 °C
Aerobic	–	$0.006\text{--}0.007 \text{ d}^{-1}$	$0.012\text{--}0.014 \text{ d}^{-1}$	–
Aerobic/anaerobic	$0.012 \text{ d}^{-1}$	–	–	–
Anaerobic	$0.005 \text{ d}^{-1}$	–	–	$0.0075 \text{ d}^{-1}$

**Table 3** | Effect of influent type, MBR type and conditions, sludge utilisation rate (SUR) and SRT/duration on observed sludge production yield

Influent	MBR type & conditions	SUR	SRT*/ Duration**	Y <sub>Obs</sub>	Authors	Country	
		g COD/ (g VSS · d)	d	g VSS/g COD			
<b>Synthetic soluble wastewater, with solids wastage*</b>							
Acetate, corn starch, yeast extract	Submerged	9.670	0.25	0.414	Ng & Hermanowicz (2005)	USA	
		6.070	0.5	0.329			
		5.220	0.5	0.383			
		1.430	2.5	0.280			
		0.790	5	0.253			
Glucose, peptone	Submerged	0.104	90	0.107	Bhatta <i>et al.</i> (2004)	Japan	
		0.083	120	0.100			
		0.072	160	0.087			
Not detailed	Submerged	0.250	200	0.022	Hay <i>et al.</i> (2006)	Singapore	
Meat extract, propionate, peptone, ethanol	Submerged	0.392	12	0.205	Spérandio <i>et al.</i> (2004)	France	
Meat extract, propionate, tryptone	Submerged	0.333	12.5	0.240			
Meat extract, tryptone, ethanol	Submerged	0.245	20	0.204	Lesage <i>et al.</i> (2005)	France	
		0.278	20	0.180			
		0.192	40	0.130			
Ethanol, methanol, acetate	Submerged	0.353	20	0.142	Mozo <i>et al.</i> (2011)	France	
		0.322	20	0.155			
		0.418	16	0.150			
Synthetic complex	Crossflow	0.187	100	0.063	Chaize & Huyard (1991)	France	
			100	0.070			
Ethanol, methanol, acetate	Crossflow	0.554	20	0.090	Mozo <i>et al.</i> (2011)	France	
			0.536	20			0.093
			0.724	10			0.138
<b>Synthetic soluble wastewater, total solids retention**</b>							
Acetate	Submerged	0.091	233	0.047	Heran <i>et al.</i> (2008)	France	
		0.137	160	0.042			
		0.062	393	0.041			
Acetate, peptone, yeast extract, paper	Submerged		133	0.050	Chiemchaisri <i>et al.</i> (1992)	Japan	
			330	0.048			
Glucose, peptone	Submerged	0.060	200	0.033	Bhatta <i>et al.</i> (2004)	Japan	
			0.100	200			0.020
			0.043	200			0.047
<b>Domestic wastewater, with solids wastage*</b>							
Raw wastewater + acetate (20%)	Submerged, AN/AX/OX	0.171	20	0.292	du Toit <i>et al.</i> (2007)	South Africa	
Screened wastewater	Submerged	0.109	50	0.183	Buisson <i>et al.</i> (1998)	France	
Screened wastewater	Submerged, AX/OX	0.123	56.7	0.143	Coté <i>et al.</i> (1998)	France	
			62.3	0.140			
			67.5	0.148			

(Continued)

Table 3 | Continued

Influent	MBR type & conditions	SUR	SRT*/ Duration**	Y <sub>obs</sub>	Authors	Country
		g COD/ (g VSS · d)	d	g VSS/g COD		
Screened wastewater	Submerged, AX/OX	0.175	23	0.248	Al-Halbouni <i>et al.</i> (2008)	Germany
		0.112	40	0.222		
Screened wastewater	Submerged, AX/OX	0.0797	60	0.209	Delrue <i>et al.</i> (2010)	France
Screened wastewater	Submerged, AX/OX Full scale	0.117	35	0.243	de Wever <i>et al.</i> (2008)	Belgium
Screened wastewater	Submerged, AX/OX	0.303	15	0.22	Jimenez <i>et al.</i> (2010)	France
		0.166	40	0.15		
Screened wastewater	Crossflow	0.1	100	0.10	Chaize & Huyard (1991)	France
Screened wastewater	Crossflow	0.242	20	0.206	Urbain <i>et al.</i> (1998)	France
		0.243	20	0.205		
Screened wastewater	Crossflow	0.201	30	0.165	Wen <i>et al.</i> (1999)	China
		0.239	15	0.278		
		0.53	5	0.377		
<b>Domestic wastewater, total solids retention**</b>						
Domestic primary effluent	Submerged		150	0.106	Rosenberger <i>et al.</i> (2002)	Germany
Domestic primary effluent	Submerged		120	0.120	Pollice <i>et al.</i> (2004)	Italy
Primary effluent, peptone, apple juice	Submerged		300	0.021	Wagner and Rosenwinkel (2000)	Germany

Note: AN: anaerobic; AX: anoxic; OX: aerobic. \*SRT is indicated for studies with solids wastage. \*\*Duration is indicated for studies with full solids retention.

$X_{U,Inf}$  and  $X_E$ , allows the prediction of the  $Y_{OBS}$  over a large range of SRTs with a constant  $f_{XU}$  value. This example shows that the conventional ASM-based model requires an undesirable adjustment to the parameter  $f_{XU}$  as a function of the SRT in order to obtain a good prediction of the sludge production yield over a large range of SRTs.

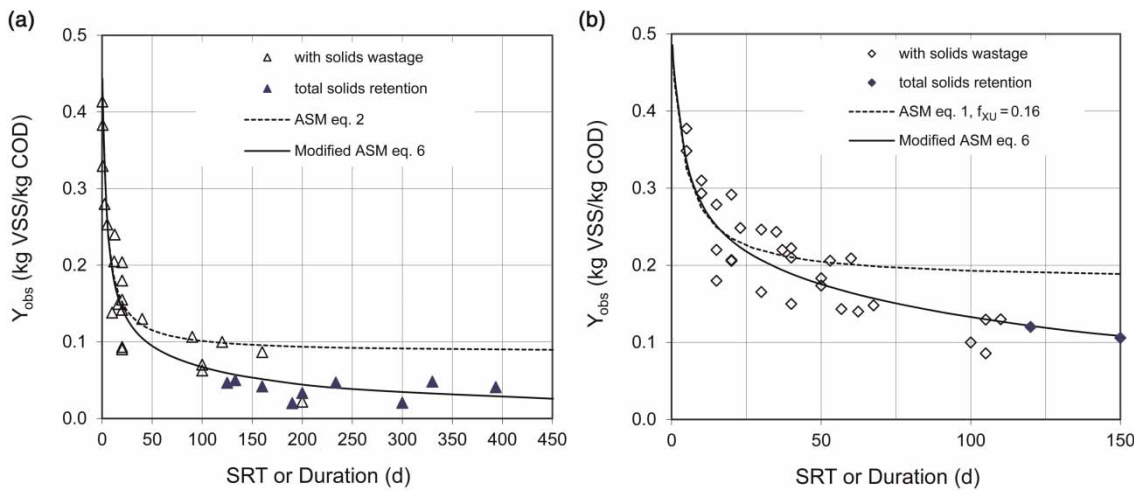
## DISCUSSION

Sludge production measured in systems operated at very long SRTs or in long-term digestion tests could be predicted by modifying ASMs to include the degradation of  $X_{U,Inf}$  ( $b_{XU}$ ) and of  $X_E$  ( $b_{XE}$ ). The fundamental mechanisms underlying this degradation and its kinetics (especially for  $X_{U,Inf}$ ) are still under review. The value of  $0.007 \text{ d}^{-1}$  appears to be a good estimate for  $b_{XE}$  at  $20^\circ\text{C}$  under aerobic conditions. The factors influencing these degradation rates are not yet fully understood. Both the physical accessibility and the chemical nature of these materials should be considered as well as their bioavailability. Hydrolysis of particles is, for example,

controlled by extracellular enzymes and is a surface-limited process that depends on substrate availability and aggregate size (Dimock & Morgenroth 2006). For these reasons it can be expected that increasing mass transfer by high mixing or provoking physical disaggregation by mechanical or hydrodynamic constraints should both lead to higher hydrolysis rates. It seems realistic to think that processes that can destabilise the chemical bonds between bio-aggregates can also increase the hydrolysis rate of particulate organic matter. Conversely, coagulation with multivalent ions (iron, aluminium, calcium and magnesium) is known to modify the accessibility of extracellular polymeric substances, influencing the digestibility of sludge in aerobic and anaerobic conditions (Park *et al.* 2006).

Whereas recent works allow the estimation of the degradation rate of endogenous compounds, less investigated and more complex is the determination of degradation rates for influent solids which were modelled as 'inerts' until now ( $X_{U,Inf}$ ). The degradation depends both on their chemical properties (Sophonsiri & Morgenroth 2004) and their size (Dimock & Morgenroth 2006). Based on respirometric



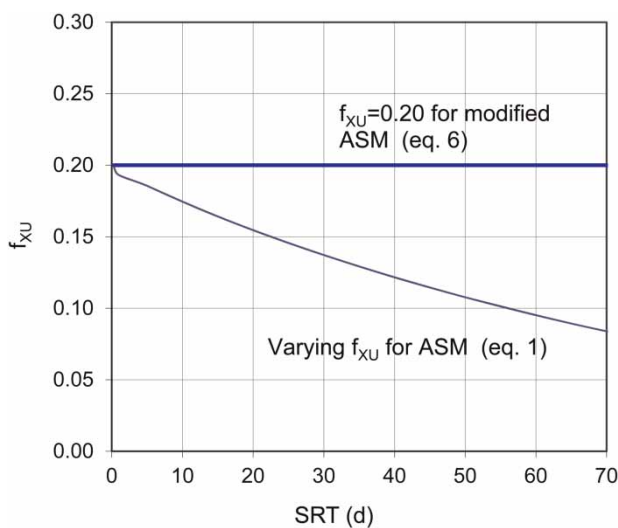


**Figure 1** | Observed sludge production ( $Y_{obs}$ ) for the ASM (Equations (1) and (2)) and the modified ASM (including degradation of  $X_{U,Inf}$  and  $X_E$ ; Equation (6); with  $b_{XE} = b_{XU} = 0.007 \text{ d}^{-1}$ ). (a) MBR fed with synthetic soluble substrate, (b) MBR treating real wastewater.

tests (long term), [Ginestet \*et al.\* \(2002\)](#) found that the hydrolysis rate of a fraction of settleable solids (mostly the cellulosic fraction) can be simulated with a hydrolysis rate of  $0.2$  to  $0.6 \text{ d}^{-1}$ , which is a relatively low value compared to those used in conventional ASM models, but a much higher value than those estimated for ‘unbiodegradable’ compounds ( $X_{U,Inf}$  and  $X_E$ ). It seems reasonable to think that some organic solids in the influent have a very low hydrolysis rate, but more work would be necessary to estimate this kinetic rate. In the absence of such information, a similar hydrolysis rate, for  $X_E$  and  $X_{U,Inf}$  can be used when dealing with systems working at very long sludge

age as this assumption seems to give acceptable predictions ([Figure 1](#)).

The experimental determination of  $b_{XE}$  and  $b_{XU}$  values could be performed by specifically tailored long-term continuous or batch tests, with both synthetic sludges ( $X_{U,Inf} = 0$ ) and real sludges (known  $f_{XU}$ ), respectively, by fitting the simulated suspended solids and oxygen uptake rate to measured data. A similar experiment was completed for the determination of  $b_{XE}$  by [Ramdani \*et al.\* \(2012\)](#). The determination of  $b_{XU}$  is, however, more complex, requiring the determination of the feed  $f_{XU}$  value (often obtained by model calibration for sludge production) and a stable feed wastewater composition during a long-term experiment.



**Figure 2** |  $f_{XU}$  values for a given sludge production yield with Equation (1) (conventional ASM model) and Equation (6) (with degradation of  $X_E$  and  $X_{U,Inf}$ ).  $b_{XE}$  and  $b_{XU}$  were fixed at  $0.007 \text{ d}^{-1}$ .

## CONCLUSIONS

Based on a literature review of MBRs treating synthetic or real wastewater, assuming an average degradation rate value of  $0.007 \text{ d}^{-1}$  for both,  $X_E$  or  $X_{U,Inf}$  was found to improve the estimation of sludge production yields measured with MBRs operated at SRTs from 1 to 400 d. This result is in accordance with the estimation of degradation rate of endogenous residue from long-term batch experiments.

Including a degradation rate for components that traditionally were considered unbiodegradable ( $X_E$  and  $X_{U,Inf}$ ) may require a change to some wastewater fractionation parameters and/or model kinetic and stoichiometric parameters. Finally the use of a modified ASM should allow the prediction of sludge production over a large range of SRTs with a

constant value for  $f_{XU}$ . This modification should improve modelling of different technologies that aim to reduce sludge production, e.g. extended sludge aeration in MBRs, activated sludge processes with parallel sludge disintegration, oxidation or hypoxic digestion.

## ACKNOWLEDGEMENTS

This work was part funded by a Collaborative Research and Development (CRD) grant from the Natural Sciences and Engineering Research Council of Canada (NSERC). This paper was presented at the 3rd IWA-WEF Wastewater Treatment Modelling Seminar (WWTmod), and the fruitful ensuing discussions with a number of researchers are kindly acknowledged.

## REFERENCES

- Al-Halbouni, D., Traber, J., Lyko, S., Wintgens, T., Melin, T., Tacke, D., Janot, A., Dott, W. & Hollender, J. 2008 Correlation of EPS content in activated sludge at different sludge retention times with membrane fouling phenomena. *Water Research* **42** (6–7), 1475–1488.
- Bhatta, C. P., Matsuda, A., Kawasaki, K. & Omori, D. 2004 Minimization of sludge production and stable operational condition of a submerged membrane activated sludge process. *Water Science and Technology* **50** (9), 121–128.
- Buisson, H., Cote, P., Praderie, M. & Paillard, H. 1998 The use of immersed membranes for upgrading wastewater treatment plants. *Water Science and Technology* **37** (9), 89–95.
- Chaize, S. & Huyard, A. 1991 Membrane bioreactor on domestic wastewater treatment sludge production and modelling approach. *Water Science and Technology* **23** (7–9), 1591–1600.
- Chiemchaisri, C., Wong, Y. K., Urase, T. & Yamamoto, K. 1992 Organic stabilization and nitrogen removal in membrane separation bioreactor for domestic wastewater treatment. *Water Science and Technology* **25** (10), 231–240.
- Corominas, L., Rieger, L., Takács, I., Ekama, G., Hauduc, H., Vanrolleghem, P. A., Oehmen, A., Gernaey, K. V., van Loosdrecht, M. C. M. & Comeau, Y. 2010 New framework for standardized notation in wastewater treatment modelling. *Water Science and Technology* **61** (4), 841–857.
- Coté, P., Buisson, H. & Praderie, M. 1998 Immersed membranes activated sludge process applied to the treatment of municipal wastewater. *Water Science and Technology* **38** (4–5), 437–442.
- de Wever, H., Brannock, M., Leslie, G. & Brepols, C. 2008 Inside or outside submerged MBR: which one is better? Membranes in Drinking Water Production and Wastewater Treatment. IWA conference, 20–22 October, Toulouse, France.
- Delrue, F., Choubert, J. M., Stricker, A. E., Spérandio, M., Mietton-Peuchot, M. & Racault, Y. 2010 Modelling a full scale membrane bioreactor using activated sludge Model n°1: challenges and solutions. *Water Science and Technology* **62** (10), 2205–2217.
- Dimock, R. & Morgenroth, E. 2006 The influence of particle size on microbial hydrolysis of protein particles in activated sludge. *Water Research* **40** (10), 2064–2074.
- Dold, P. L., Ekama, G. A. & Marais, G. v. R. 1980 A general model for the activated sludge process. *Progress in Water Technology* **12** (6), 47–77.
- du Toit, G. J. G., Ramphao, M. C., Parco, V., Wentzel, M. C. & Ekama, G. A. 2007 Design and performance of BNR activated sludge systems with flat sheet membranes for solid-liquid separation. *Water Science and Technology* **56** (6), 105–113.
- Fenu, A., Guglielmi, G., Jimenez, J., Spérandio, M., Saroj, D., Lesjean, B., Brepols, C., Thoeve, C. & Nopens, I. 2010 Activated sludge model (ASM) based modelling of membrane bioreactor (MBR) processes: a critical review with special regard to MBR specificities. *Water Research* **44** (15), 4272–4294.
- Ginestet, P., Maisonnier, A. & Spérandio, M. 2002 Wastewater COD characterization: biodegradability of physico-chemical fractions. *Water Science and Technology* **45** (6), 89–97.
- Hay, C. T., Sun, D. D., Khor, S. L. & Leckie, J. O. 2006 Effect of 200 days' sludge retention time on performance of a pilot scale submerged membrane bioreactor for high strength industrial wastewater treatment. *Water Science and Technology* **53** (11), 269–276.
- Henze, M., Gujer, W., Mino, T. & Van Loosdrecht, M. 2000 *Activated Sludge Models ASM1, ASM2, ASM2d and ASM3*. IWA Publishing, London, UK.
- Heran, M., Wisniewski, C., Orantes, J. & Grasmick, A. 2008 Measurement of kinetic parameters in a submerged aerobic membrane bioreactor fed on acetate and operated without biomass discharge. *Biochemical Engineering Journal* **38** (1), 70–77.
- Jimenez, J., Grelier, P., Meinhold, J. & Tazi-Pain, A. 2010 Biological modelling of MBR and impact of primary sedimentation. *Desalination* **250** (2), 562–567.
- Jones, R., Parker, W., Khan, Z., Murthy, S. & Rupke, M. 2007 A study of the biodegradable fraction of sludges in aerobic and anaerobic systems. In: *Proceedings of the WEF Specialty Conference on Residuals and Biosolids Management*, Denver, CO.
- Laera, G., Pollice, A., Saturno, D., Giordano, C. & Lopez, A. 2005 Zero net growth in a membrane bioreactor with complete sludge retention. *Water Research* **39** (20), 5241–5249.
- Lesage, N., Spérandio, M. & Cabassud, C. 2005 Performances of a hybrid adsorption/submerged membrane biological process for toxic waste removal. *Water Science and Technology* **51** (6–7), 173–180.
- Lubello, C., Caffaz, S., Gori, R. & Munz, G. 2009 A modified activated sludge model to estimate solids production at low and high solids retention time. *Water Research* **43** (18), 4539–4548.

- Marais, G. v. R. & Ekama, G. A. 1976 The activated sludge process – part I: Steady state behaviour. *Water S.A.* **2** (4), 163–200.
- Mozo, I., Stricot, M., Lesage, N. & Spérandio, M. 2011 Fate of hazardous aromatic substances in membrane bioreactors. *Water Research* **45** (15), 4551–4561.
- Ng, H. Y. & Hermanowicz, S. W. 2005 Membrane bioreactor operation at short solids retention times: performance and biomass characteristics. *Water Research* **39** (6), 981–992.
- Park, C., Abu-Orf, M. M. & Novak, J. Y. 2006 The digestibility of waste activated sludges. *Water Environment Research* **78** (1), 59–68.
- Pollice, A., Laera, G. & Blonda, M. 2004 Biomass growth and activity in a membrane bioreactor with complete sludge retention. *Water Research* **38** (7), 1799–1808.
- Ramdani, A., Dold, P. L., Déléris, S., Lamarre, D., Gadbois, A. & Comeau, Y. 2010 Biodegradation of the endogenous residue of activated sludge. *Water Research* **44** (7), 2179–2188.
- Ramdani, A. 2011 Biodégradation du résidu endogène de boues activées. PhD thesis, Université de Montréal, Montréal, Canada.
- Ramdani, A., Dold, P. L., Gadbois, A., Déléris, S., Houweling, D. & Comeau, Y. 2012 Biodegradation of the endogenous residue of activated sludge in a membrane bioreactor with continuous or on-off aeration. *Water Research* **46** (9), 2837–2850.
- Rosenberger, S., Krüger, U., Witzig, R., Manz, W., Szewzyk, U. & Kraume, M. 2002 Performance of a bioreactor with submerged membranes for aerobic treatment of municipal waste water. *Water Research* **36** (2), 413–420.
- Sophonsiri, C. & Morgenroth, E. 2004 Chemical composition associated with different particle size fractions in municipal, industrial, and agricultural wastewaters. *Chemosphere* **55** (5), 691–703.
- Spérandio, M. & Espinosa, M. C. 2008 Modelling an aerobic submerged membrane bioreactor with ASM models on a large range of sludge retention time. *Desalination* **231** (1–3), 82–90.
- Spérandio, M., Lebreton, M. H. & Lesage, N. 2004 Lab-scale MBR performances analysis. Internal LISBP-INSA report.
- Urbain, V., Mobarry, B., de Silva, V., Stahl, D. A., Rittmann, B. E. & Manem, J. 1998 Integration of performance, molecular biology and modelling to describe the activated sludge process. *Water Science and Technology* **37** (4–5), 223–229.
- Wagner, J. & Rosenwinkel, K. H. 2000 Sludge production in membrane bioreactors under different conditions. *Water Science and Technology* **41** (10–11), 251–258.
- Wen, X., Xing, C. & Qian, Y. 1999 A kinetic model for the prediction of sludge formation in a membrane bioreactor. *Process Biochemistry* **35** (3–4), 249–254.

First received 15 June 2012; accepted in revised form 26 September 2012