A Single Determinant Dominates the Rate of Yeast Protein Evolution

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A gene’s rate of sequence evolution is among the most fundamental evolutionary quantities in common use, but what determines evolutionary rates has remained unclear. Here, we carry out the first combined analysis of seven predictors (gene expression level, dispensability, protein abundance, codon adaptation index, gene length, number of protein-protein interactions, and the gene’s centrality in the interaction network) previously reported to have independent influences on protein evolutionary rates. Strikingly, our analysis reveals a single dominant variable linked to the number of translation events which explains 40-fold more variation in evolutionary rate than any other, suggesting that protein evolutionary rate has a single major determinant among the seven predictors. The dominant variable explains nearly half the variation in the rate of synonymous and protein evolution. We show that the two most commonly used methods to disentangle the determinants of evolutionary rate, partial correlation analysis and ordinary multivariate regression, produce misleading or spurious results when applied to noisy biological data. We overcome these difficulties by employing principal component regression, a multivariate regression of evolutionary rate against the principal components of the predictor variables. Our results support the hypothesis that translational selection governs the rate of synonymous and protein sequence evolution in yeast.

Introduction

A protein’s evolutionary rate, commonly measured by the number of nonsynonymous substitutions per site in its encoding gene, is routinely used to characterize functional importance, detect selection (Nei and Kumar 2000), create phylogenetic trees (Kurtzman and Robnett 2003), identify orthologous genes (Wall, Fraser, and Hirsh 2003), and infer the time of major evolutionary events. However, what determines a protein’s evolutionary rate has remained the subject of active speculation and ongoing research (Pál, Papp, and Hurst 2001; Akashi 2003; Rocha and Danchin 2004).

Recently, studies have found significant influences on evolutionary rate from many disparate variables: proteins have been reported to evolve slower if their encoding genes have a higher expression level in mRNA molecules per cell (Pál, Papp, and Hurst 2001), if they have a higher codon adaptation index (CAI) (Rocha and Danchin 2004; Wall et al. 2005), more protein-protein interactions (higher “degree”) (Fraser et al. 2002), shorter length (Marais and Duret 2001), a smaller fitness effect upon gene knockout (higher “dispensability”) (Hirsh and Fraser 2001; Yang, Gu, and Li 2003; Zhang and He 2005), or a more central role in interaction networks (“betweenness centrality,” or simply “centrality”) (Hahn and Kern 2005).

Here, we first demonstrate that the analytical techniques widely used to establish independent roles for many effects, partial correlation and multiple regression, generate highly significant but entirely spurious effects given noisy data such as those available for evolutionary analyses. Then, using a technique which does not suffer from these problems, we carry out a comprehensive analysis designed to uncover the major independent correlates of evolutionary rate in the model eukaryote Saccharomyces cerevisiae. We determine the number of such correlates, their strength, and their relationship to the biological variables used in previous studies. Finally, we ask what these correlates reveal about the biological constraints on protein sequence evolution.

Materials and Methods

Genomic Data

We obtained CAIs and evolutionary rates (nonsynonymous substitutions per site dN, synonymous substitutions per site dS, adjusted synonymous substitutions dS’ [Hirsh, Fraser, and Wall 2005], and ratios dN/dS and dN/dS’ ) from four-way yeast species alignments for 3,036 S. cerevisiae genes (Wall et al. 2005, supporting information, Table 4). Deletion-strain growth rate data were downloaded from http://chemogenomics.stanford.edu/supplements/01yfh/files/orfgenedata.txt; the average growth rates of the homozygous deletion strains were used as dispensability measurements in our analysis. The filtered yeast interactome data set (Han et al. 2004) provided interaction network hub types for 199 genes and the number of interactions for 1,379 yeast genes. The latter data set was used to compute betweenness-centrality values, which quantify the frequency with which a network node lies on the shortest path between other nodes, as described by Hahn and Kern (2005). Genomic data for Saccharomyces paradoxus and Kluveromyces waltii were obtained exactly as described by Drummond et al. (2005). Genome sequences for Escherichia coli K12 and Salmonella typhimurium LT2 were obtained from the Institute for Genomic Research (Peterson et al. 2001), with orthologs identified and evolutionary rates computed exactly as described (Drummond et al. 2005). Gene expression levels for E. coli measured in mRNAs per cell in Luria-Bertani (LB) and M9 media were obtained from Bernstein et al. (2002).

Statistical Analysis

We used R (Ihaka and Gentleman 1996) for statistical analyses and plotting. The package ‘pls’ was used to perform
principal component regression. We log transformed all variables except dispensability. We decided whether or not to log transform a variable based on whether log transformation led to a higher $R^2$. For those variables that contained zeros, we added a small constant before the log transformation, as previously suggested (Wall et al. 2005). This constant was 0.001 for $dN$, $dS'$, and $dN/dS'$ and $10^{-7}$ for betweenness centrality. We scaled the predictor variables to zero mean and unit variance before carrying out the principal component analysis. In all regression analyses (both against the original predictors and against the principal components), we determined the statistical significance levels by starting with the full model and successively dropping the least significant predictor until only significant predictors ($P < 0.01$) remained.

Results

Correlation and Partial Correlation Analysis

We used the yeast $S. cerevisiae$ to examine the determinants of evolutionary rate because it has been the subject of many previous analyses (e.g., Pál, Papp, and Hurst 2001; Fraser 2005) and has an enormous amount of available genomic, proteomic, and functional data. We first examined the raw correlation of six previously assessed biological variables (expression, CAI, length, dispensability, degree, and centrality) with protein evolutionary rate, as measured by the number of nonsynonymous substitutions per site in the underlying gene. A seventh variable, the number of protein molecules per cell (“abundance”), was also considered. Table 1 shows that all variables except centrality correlated significantly with evolutionary rate, as previously reported.

Expression level strongly correlates with evolutionary rate, and higher expressed genes have higher CAIs (Akashi 2001), are less dispensable (Gu et al. 2003), more abundant (Ghaemmaghami et al. 2003), and more likely to be found in protein-protein interaction experiments (Bloom and Adami 2003) than lower expressed genes. No inverse relationships have been posited by which these variables alter the expression level. Thus, it is imperative to establish whether these variables play a role independent of expression level. Following previous analyses (Pál, Papp, and Hurst 2003; Lemos et al. 2005; Wall et al. 2005), we computed the partial correlation of our seven variables with evolutionary rate, controlling for expression level. Table 1 shows that CAI, dispensability, and degree all showed reduced but highly significant partial correlations, consistent with previous studies (Hirsh and Fraser 2003; Wall et al. 2005), as did abundance.

Partial Correlations and Noisy Data

What can we conclude from highly significant partial correlations? Yeast expression-level measurements from multiple groups, even two using the same commercial oligonucleotide array, correlated with coefficients of only 0.39–0.68 (Coghlan and Wolfe 2000), demonstrating that expression-level measurements are inaccurate and/or simply reflect the variability of gene expression across growth conditions and strains. We refer to all such variability as noise, regardless of its source. Noisy data are the rule in genome-wide molecular studies, leading us to explore what effect noise has on partial correlation analyses. As a concrete example, CAI is so tightly bound to expression level that a recent analysis used CAI as its preferred expression-level measurement (Wall et al. 2005). Might CAI’s significant partial correlation only reflect our inability to control for the true (i.e., evolutionarily relevant) underlying expression level? More generally, we can ask: what is the expected partial correlation of two variables, controlling for a third, when (1) the two variables relate only through dependence on the third “master” variable and (2) all measurements contain noise?

Given these conditions, we derive explicit formulas for the expected partial correlation, its statistical significance, and its behavior under various limiting cases in the Appendix. The expected partial correlation is, in general, larger than zero because the full correlation reflects the true underlying master variable’s influence, while partial correlations can only remove the portion of this influence that is visible through a noisy measurement (box 1). We show that, surprisingly, if measurements of an underlying causal variable (e.g., expression level) are noisy, highly significant partial correlations of virtually any strength between the dependent predictors can be obtained.

As a case in point, dispensability’s role has been vigorously debated (Hirsh and Fraser 2003; Pál, Papp, and Hurst 2003; Wall et al. 2005) with correlation and partial correlations acting as key analytical tools. Given a model in which expression level $X$ and noise completely determine dispensability $D$ and evolutionary rate $K$ (see box 1), what is the observed partial correlation $r_{DKX}$ if we fit variables to approximately match the observed correlations between $X$, $D$, and $K$? As a concrete example, previous reports show that, using parametric Pearson’s correlations, $r_{Y|K} \approx -0.6$ (Pál, Papp, and Hurst 2001; Wall et al. 2005), $r_{DX} \approx 0.25$ (Wall et al. 2005), $r_{DX} \approx 0.2$ (Pál, Papp, and Hurst 2003), and $r_{DKX} \approx 0.24$ (Wall et al. 2005). We can obtain roughly the reported full correlations and $r_{DKX} \approx 0.23 \pm 0.02, P \ll 10^{-9}$ with 3,000 observations if the true expression level $X$ is normally distributed with mean 0.5 and standard deviation (SD) 0.25, and the observable predictors $X$, $D$, and $K$ are equal to $X$ plus zero mean normally distributed noise with SDs of 0.3, 0.7 and 0.1, respectively. This highly significant partial correlation is entirely

| Variable X | Correlation $r_{X|DN}$ | Partial Correlation $r_{X|DN|gene expression}$ | VIF |
|------------|-------------------------|-----------------------------------------------|-----|
| Gene expression | $-0.537***$ | $0$ | $2.72$ |
| CAI | $-0.565***$ | $-0.338***$ | $2.46$ |
| Protein abundance | $-0.478***$ | $-0.232***$ | $2.05$ |
| Gene length | $0.136***$ | $0.010$ | $1.25$ |
| Gene dispensability | $0.265***$ | $0.183***$ | $1.08$ |
| Degree (number of protein-protein interactions) | $0.246***$ | $-0.127*$ | $1.70$ |
| Protein centrality (frequency on node-node shortest paths) | $-0.098$ | $-0.082$ | $1.64$ |

Note.—$^*P < 0.01$; $^{**}P < 10^{-5}$; $^{***}P < 10^{-9}$. 

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spurious: in this model, expression level and random noise completely determine dispensability. Thus, the observed statistical relationship between dispensability and evolutionary rate, established by correlation and partial correlation, would arise even if no actual relationship existed except mutual dependence on noisily measured expression level.

Multivariate Regression Analysis

Because partial correlation analysis is not applicable to the problem at hand, what other methods can we use to determine the relative influence of different predictors on the rate of evolution? One obvious choice is multivariate regression analysis, a method with the added benefit that we can look at the influence of all potential predictor variables at the same time and can eliminate step by step those predictors that contribute the least to the regression model. Indeed, several authors have followed this route (Rocha and Danchin 2004; Agrafioti et al. 2005). Regressing dN simultaneously against the seven predictors we consider here, we find that all but centrality make a significant contribution to the response’s variance, R². However, for our toy model (box 1) in which the two predictors reflect the same underlying variable plus noise, the VIFs are only 1.21 in both cases, yet the analysis demonstrates that multivariate regression and partial correlation break down any way. Collinearity and noise work together to undermine these techniques.

Principal Component Regression Analysis

An alternative approach is to first identify the independent sources of variation in the data, and then determine the contribution of each biological predictor to each source. The technique of principal component regression offers a standard way to carry out such an analysis.

In principal component regression (Mandel 1982), multiple linear predictors (e.g., expression level and dispensability) are scaled to zero mean and unit variance, inserted in a matrix, and rotated such that the new coordinate axes point in the directions of greatest predictor variation. The new axes define variables, called principal components, which are linear combinations of the original predictors. Subsequent linear regression of the response (e.g., dN) on the rotated predictor data yields several pieces of information per principal component: the proportion of the response’s variance, R², explained by the component, the significance of this R², and the fractional contribution of each original predictor to the component. Because all principal components are orthogonal and independent, the total proportion of response variance explained by the data is the sum of the component R² values. Principal component regression thus circumvents the debilitating problems of partial correlation and multivariate regression analyses (box 1) while yielding results which are, in some ways, easier to interpret.

We carried out principal component regression on the seven predictors analyzed above. Because the determination of principal components involves only the predictors and not the response (i.e., dN or dS), there is only one set of components and contributions from biological predictors. The regression analysis generates response-specific results, in particular, the proportions of variance in dN, dS, and so on, which each component explains. Table 2 shows numerical data from the analysis of dN and dS using the seven predictors of expression, CAI, abundance, length,
dispensability, degree, and centrality; figures 1a and 2a show these data graphically.

Strikingly, for the rate of protein evolution, dN, one principal component explained 43% of the variance with high significance, while all other components explained less than 1% (fig. 1). The single dominant component was almost entirely (>90%) determined by roughly equal contributions from three predictors: expression level, abundance, and CAI.

While the causes of dNs variation have remained unclear, dS is constrained by translational selection: selection for preferred codons, which correspond to abundant tRNAs and are translated faster and more accurately (Akashi 1994, 2001), makes many synonymous changes unfavorable and thus reduces dS (Hirsh, Fraser, and Wall 2005). Figure 2 shows that the dS results mirror those using dN: the first component, which is determined almost entirely by expression, abundance and CAI, is overwhelmingly dominant (50.8% of dS variation). A second highly significant component of modest size (6.6% of dS variation) appears but is 88.4% determined by abundance and CAI. Astonishingly, the seven biological predictors explain a cumulative 61.9% of the total variance in dS, with three predictors (expression, abundance, and CAI) contributing roughly equal amounts and accounting for 87% of the total variance explained. Because synonymous sites are thought to be under relatively weak selection, we would expect random fluctuations (noise) to contribute a large proportion of variation in dS, yet our analysis suggests that selective pressures, even those revealed using noisy data, account for almost two-thirds of the dS variation among these genes.

The size of the seven-component data set (568 genes) was severely limited by the requirement for genes having measures for all seven predictors. In particular, we used high-quality interactions measurements (Han et al. 2004) for degree and betweenness centrality; eliminating these measurements, which apparently contribute negligible amounts to evolutionary rate, more than triples the data set size to 1,939 genes. We performed the same analysis on this expanded set and obtained similar results (table 3, and figs. 1b and 2b).

To examine the possible effects of assuming a linear model in the regression, we repeated our analyses using only data ranks for the predictors and each response. The results of this nonparametric analysis were virtually unchanged from the parametric case (data not shown), indicating that little information is contained in the relative magnitudes of the variables.

It is common practice to interpret dS as the rate of selectively neutral divergence and the ratio dN/dS as the deviation of protein evolutionary rate from neutral, putatively allowing detection of purifying selection or adaptive evolution. We analyzed dN/dS and found trends that were similar to those observed in dN and dS alone (tables 2 and 3). The dominant principal component explained only half the variation in dN/dS compared to dN or dS, but the reason seems obvious in light of our results: dN and dS appear to reflect the same underlying selective force, so dividing one by the other removes much of the shared influence. In yeast, as in many other organisms, dS does not reflect neutral divergence but rather divergence constrained by translational selection for preferred codons, as previous authors have noted (Hirsh, Fraser, and Wall 2005). These authors proposed an adjusted measure of dS, denoted dS', from which the influence of codon preference has been extracted (Hirsh, Fraser, and Wall 2005). We thus analyzed dS' and dN/dS' (tables 2 and 3), and found that for dS' the dominance of the first principal component was obliterated. While two components (component 1, mostly CAI, expression and abundance; and component 2, mostly dispensability) appeared to make small but possibly meaningful contributions ($R^2 > 6\%$) in the smaller seven-predictor data set, these contributions were effectively eliminated in the

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Fig. 1.—Principal components regression on the rate of protein evolution (dN) in 568 yeast genes reveals a single dominant underlying component. (a) Of the seven principal components only one (starred) explained a statistically significant proportion of the variation in dN. This component explained 43% of the variance, while no other component explained more than 1%. Expression level, CAI, and protein abundance determined most of this dominant component (labeled), while the remaining predictors (in order from top to bottom: length, dispensability, degree, and centrality) determined <10% of the component’s $R^2$. See table 2 for numerical data. (b) A larger data set (1,939 genes) excluding protein-protein interaction predictors showed the same patterns as in (a).

Fig. 2.—Principal components regression on the rate of synonymous site evolution (dS) in 568 yeast genes reveals a single dominant underlying component. (a) Seven-predictor variables (see text) yielded seven principal components, of which six (starred) explained a statistically significant proportion of the variation in dS. The dominant component explained 51% of the variance, while no other component explained more than 7%. See figure 1 caption for the breakdown of predictor contributions. (b) A larger data set (1,939 genes) excluding protein-protein interaction predictors showed the same patterns as in (a).
larger five-predictor data set ($R^2 < 3\%$), even though the major contributing predictors were still present. This sample size dependence suggests that the contributions of components 1 and 2 are artifacts. Overall, our results are consistent with the previous claim that $dS^1$ has been purged of the influence of selection on synonymous sites (Hirsh, Fraser, and Wall 2005). As additional support, the $dN/dS$ ratio for $dS^1$ was $2.58$ ($P < 10^{-6}$) in contrast to $0.73$ ($P < 10^{-6}$) for $dS^2$, contrary to previous reports (Hirsh and Fraser 2001; Fraser et al. 2002; Fraser et al. 2004; Wall et al. 2005). Perhaps these measures, as continuous predictors describing complex and poorly understood phenomena, display false precision, i.e., they reflect real underlying effects but quantify them in overly precise ways that introduce noise. We reasoned that simpler

### Table 3

Results of Principal Component Regression Analysis on Five Predictors and Five Measures of Evolutionary Rate for 1,939 Saccharomyces cerevisiae genes

<table>
<thead>
<tr>
<th>Percent variance explained</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>All</th>
</tr>
</thead>
<tbody>
<tr>
<td>dN</td>
<td>36.94***</td>
<td>0.05</td>
<td>0.03</td>
<td>0.22</td>
<td>0.60***</td>
<td>37.85***</td>
</tr>
<tr>
<td>dS</td>
<td>39.33***</td>
<td>0.73***</td>
<td>0.09</td>
<td>1.93***</td>
<td>1.92***</td>
<td>44.01***</td>
</tr>
<tr>
<td>$dN/dS$</td>
<td>22.39***</td>
<td>0.28</td>
<td>0.21</td>
<td>0.00</td>
<td>0.21</td>
<td>23.10***</td>
</tr>
<tr>
<td>$dS^1$</td>
<td>1.26</td>
<td>2.52***</td>
<td>2.58***</td>
<td>0.00</td>
<td>1.54***</td>
<td>7.91***</td>
</tr>
<tr>
<td>$dN/dS^1$</td>
<td>37.61***</td>
<td>0.28</td>
<td>0.00</td>
<td>0.14</td>
<td>1.16**</td>
<td>39.20***</td>
</tr>
</tbody>
</table>

**Percent contributions**

| Expression | 33.2 | 1.7 | 0.1 | 24.2 | 40.8 |
| CAI        | 31.4 | 1.0 | 9.4 | 9.0  | 49.2 |
| Abundance  | 31.3 | 0.6 | 0.4 | 65.8 | 1.9  |
| Length     | 2.0  | 61.0 | 29.6 | 0.4  | 7.0 |
| Dispensability | 2.1  | 35.7 | 60.5 | 0.6  | 1.1 |

**Note:** $^P < 0.01$; $^{**}P < 10^{-6}$; $^{***}P < 10^{-9}$. Bold indicates that the indicated predictor contributes at least 20% to the indicated component.

In all the above analyses, we found that protein-protein interactions and gene dispensability showed little or no apparent influence on the rate of protein evolution ($dN$) and synonymous site evolution ($dS$), contrary to previous reports (Hirsh and Fraser 2001; Fraser et al. 2002; Fraser and Hirsh 2004; Wall et al. 2005). Perhaps these measures, as continuous predictors describing complex and poorly understood phenomena, display false precision, i.e., they reflect real underlying effects but quantify them in overly precise ways that introduce noise. We reasoned that simpler per synonymous site, far beyond the range of reliable estimation. These high $dS$ values may result from a combination of the large amount of time separating the species, changes in synonymous pressures, and difficulties in ortholog identification and alignment. The robust $dN$ results lend weight to the first two explanations. We expect that as even more distant relatives are analyzed, the $dN$ results will be attenuated by noise, alignment degradation, and phenotypic changes that must, in some cases, be linked to changes in relative gene expression levels.

To assess whether the trends we identified for yeast extend to other species, we examined evolutionary rates in 2,605 E. coli genes relative to S. typhimurium. Lacking global protein abundance, interaction, and dispensability data for E. coli, we used length, two measures of expression level, reflecting growth in minimal M9 and rich LB media, and two measures of codon optimization, CAI and the frequency of optimal codons $F_{op}$ (Ikemura 1985), as predictors. Again, a dominant component emerged which explained 36% of the $dN$ variance (16-fold more than any other) and 25% of the $dS$ variance (38-fold more than any other). Because most of the included predictors are translation oriented in some way, our results offer no conclusion as to the possible influence of other predictors in E. coli. However, the remarkable similarity to the yeast results, including the large portion of variance explained, suggests that similar selective forces have shaped evolutionary rates in this prokaryotic organism.

Analysis of Binary Variables Using Analysis of Covariance

In all the above analyses, we found that protein-protein interactions and gene dispensability showed little or no apparent influence on the rate of protein evolution ($dN$) and synonymous site evolution ($dS$), contrary to previous reports (Hirsh and Fraser 2001; Fraser et al. 2002; Fraser and Hirsh 2004; Wall et al. 2005). Perhaps these measures, as continuous predictors describing complex and poorly understood phenomena, display false precision, i.e., they reflect real underlying effects but quantify them in overly precise ways that introduce noise. We reasoned that simpler
measures, such as essentiality (the limiting case of dispensability, where essential genes are indispensable and nonessential genes include all those with dispensability >0) and type of network interaction hub ("date" hubs interact with many partners individually, while "party" hubs do so simultaneously) (Han et al. 2004; Fraser 2005), subjected to a category-based analysis, might reveal relationships obscured by their noisy continuous counterparts.

Because expression level, CAI, and abundance have such an important effect on evolutionary rate, we have to carry out the category-based analysis controlling for the effect of these three predictors. We chose to perform an analysis of covariance ("ANCOVA"). As the continuous variable we used the principal component of the three quantities expression level, CAI, and abundance, while we encoded the category (gene is or is not a party hub, is or is not a date hub, is or is not essential) as a binary variable. We found that party hubs evolve on average at 60% of the rate of genes with known interactions (P < 10^{-5}), date hubs at 92% of the rate (not significant) for genes with measured interactions, and essential genes at 84% of the speed of all genes (P < 10^{-5}) (fig. 3). The effect of gene essentiality is significant but small in magnitude, and date hubs show no significant rate constraint. As previously reported (Fraser 2005), party hubs do indeed experience a notable 40% reduction in evolutionary rate. However, evolutionary rates in yeast span three orders of magnitude; interactions play at best a minor role in constraining rates.

Discussion

We have carried out the most comprehensive comparative analysis to date of potential determinants of nonsynonymous (dN) and synonymous (dS) yeast gene evolutionary rates. We used a published data set of evolutionary rates, previously used to establish an independent role for dispensability (Wall et al. 2005) and to correct dS for translational selection (Hirsh, Fraser, and Wall 2005), to highlight the methodological improvements introduced here. We find that a single underlying component explains roughly half the variation in both dN and dS, and that this dominant component is almost entirely determined by the gene expression level, protein abundance, and codon bias as measured by the CAI. Our results generalize to E. coli despite use of a reduced set of predictors.

The predictors we included in our analysis appear to explain roughly half the variation in dN and dS. Some other predictors could explain the remaining half, but this seems quite unlikely for a variety of reasons. First, a significant portion of evolutionary rate variations are probably random because the evolutionary process is inherently stochastic. Second, our R^2 estimates constitute a lower bound because the R^2 values we find are attenuated by measurement noise, for example, on microarray readings of gene expression (Coghlan and Wolfe 2000), by systematic error, e.g., in some protein-protein interactions data (Bloom and Adami 2003), and by time variation, for example, in expression over the cell cycle (Cho et al. 1998). Finally, the true relationship between any of the predictors we examine and dN or dS is unlikely to be perfectly linear, and deviations from linearity reduce parametric R^2.

Our results point to a single dominant cause for most of the 1,000-fold variation in evolutionary rates among yeast genes, and the dominant component’s three biological contributors suggest that the cause is translational selection. We hypothesize that the number of translation events a gene experiences determines its evolutionary rate and that expression, abundance, and CAI are all roughly equally good predictors of the number of translation events. Translation is remarkably error prone, with roughly 19% of average length yeast proteins carrying a missense error (Drummond et al. 2005), and these errors can cause protein misfolding that imposes a well-known burden on the cell (Goldberg 2003) which scales with the number of translation events. Selection to reduce the number of error-induced misfolded proteins could constrain both synonymous site evolution
(dS), e.g., through pressure for preferred codons which reduce mistranslation of proteins (increased translational accuracy) (Akashi 1994), and protein sequence evolution (dN), e.g., through pressure for protein sequences that fold properly despite mistranslation (increased translational robustness) (Drummond et al. 2005). In this way, a single underlying cost can govern both synonymous and nonsynonymous evolutionary rates, consistent with our findings.

We used principal component regression for our analysis because, as we demonstrate, the more commonly employed techniques of partial correlation analysis and multivariate regression are inapplicable by assumption (in the latter case) and prone to produce spurious effects in the presence of noisy correlated data (in both cases). By contrast, under principal component regression, the transformed predictors are orthogonal and uncorrelated, so that their relative contributions to the overall regression model can be evaluated independently and reliably. Moreover, we can extend this method to assess the influence of additional binary predictors, by carrying out an ANCOVA in which the covariable is given by the principal component that explains the majority of the response-variable variance.

Wall et al. (2005) use a structural equation model to examine the influence of measurement inaccuracy on their partial correlation analysis of the effects of expression level and dispensability on dN. Given their analysis, they admit an inability to determine the relative importance of these two predictors but conclude that dispensability has an independent effect on dN. We claim to be able to determine relative importance and come to an opposite conclusion for two reasons. First, a general advantage of principal component regression over partial correlation is the ability to find predictors not originally included in the analysis. We were fortunate in this case that the dominant predictor is not expression level, CAI, or abundance, but rather a variable (likely the frequency of translation) that these three predictors measure with roughly equal accuracy. Partial correlation can never find such underlying variables. Second, the structural equation model of Wall et al. (2005) attempts to quantify how much the predictors could explain given the hypothetical levels of measurement accuracy, but with principal component regression, we are asking how much the given predictors can explain, whatever their accuracy. Here we were doubly fortunate. Three of our predictors (CAI, abundance, and expression) triangulate on the same underlying variable, increasing accuracy essentially by measuring it in triplicate; this variable happens to explain a large portion, perhaps most, of dN’s explainable variance.

How much dispensability and degree influence evolutionary rate has been a contentious issue. Regarding the former, the literature reflects disagreement over whether dispensability has any effect whatsoever on the rate of evolution, with partial correlation analyses playing a prominent evidentiary role (Hirsh and Fraser 2003; Páll, Papp, and Hurst 2003; Wall et al. 2005). Our analysis, which avoids problematic partial correlations but uses the same data as in previous analyses that appeared to confirm a significant role for dispensability (Wall et al. 2005), is quite clear: dispensability neither constitutes an independent source of variation in dN nor contributes meaningfully to the dominant component that does influence dN. In the case of degree, the disagreement has pivoted on whether experimental surveys are biased toward detecting interactions more often in highly expressed proteins (Bloom and Adami 2003, 2004; Fraser and Hirsh 2004), leading to a true but biologically irrelevant degree-dN relationship. Our analysis shows that degree does not contribute independently, but makes a small, significant contribution to the variable dominated by expression, abundance, and CAI, as expected under the expression-bias hypothesis and inconsistent with a true constraint from the number of interactions. In short, our results suggest neither degree nor dispensability make much difference in dN and point out precisely why previous authors have been led to the opposite conclusion.

By contrast, our ANCOVA offers support for the observation that proteins that interact with multiple partners simultaneously, so-called party hubs, evolve slower (Fraser 2005), even after accounting for the translational effect we identify here. Party hubs epitomize the intuition behind the interactions hypothesis: while interactions presumably constrain residues, it appears that in order to slow a protein’s overall rate of evolution, interactions must involve a significant proportion of the protein’s residues, as expected for party hubs. Date hubs, which would include proteins that interact with many partners serially at the same site, appeared significantly slower evolving in the previous analysis (Fraser 2005), but our results suggest this finding reflected a failure to properly control for expression-linked effects (again, partial correlation was used). (Note that ANCOVA enjoys a crucial and useful advantage over partial correlation aside from its greater reliability, namely the ability to control simultaneously for multiple intercorrelated variables such as expression and CAI.)

The rates dN and dS are routinely used to carry out analyses on selection, often under the assumption that dN/dS > 1 indicates adaptive protein evolution and dN/dS < 1 indicates purifying selection, and generally with the intent of quantifying functional pressures. Our results suggest that both evolutionary rates are determined by translational selection and are therefore likely poor predictors of functional selection because translational selection by definition operates before a protein becomes functional. In yeast, dS does not measure neutral divergence, and thus, in the absence of a quantitative description of the relative strengths of selection on nonsynonymous and synonymous sites, the measure dN/dS is meaningless. Recently, a method for correcting dS for synonymous site selection was proposed (Hirsh, Fraser, and Wall 2005), and we found that the adjusted measure of neutral divergence, dS', indeed appears free of the influence of the dominant variable we link to translational selection. Our dominant variable shows virtually identical predictive power for dN and dN/dS', indicating that dividing out the neutral divergence, which for example might be due to variable mutation rates, makes little difference when analyzing the rate of protein evolution. Our results suggest that using overall gene evolutionary rates to characterize functional selection is unwise; examining dN and dS at particular sites remains a powerful and important tool in evolutionary analyses of genes.

We have found that yeast coding sequences accumulate substitutions according to a surprisingly simple formula: more predicted translation events mean slower
evolution. In recent years, evidence has accumulated that translation-linked variables, in particular expression levels, govern the evolutionary rate of proteins across all life, from bacteria (Rocha and Danchin 2004) to fungi (Pál, Papp, and Hurst 2001), plants (Wright et al. 2004) and animals (Duret and Mouchiroud 2000) including humans (Subramanian and Kumar 2004), but translational selection has only recently been proposed as an explanation for this puzzling trend (Akashi 2003; Drummond et al. 2005). Our results suggest that translational selection dominates the rate of protein evolution, and by extension suggest that translational selection operates across the tree of life, from prokaryotes to humans. Future work must illuminate the precise biophysical effects that constrain molecular evolution, but we have shown that, at least in yeast, the answers may be found in translation.

**Box 1**
Comparing Partial Correlation, Multivariate Regression, and Principal Component Regression

How do the three analytical techniques considered here fare given a case where only one variable determines evolutionary rate? For each technique, what would we conclude about the number and strength of the rate determinants? Consider a simple model in which a variable $X$ (e.g., expression level) determines two other variables, a putative determinant $D$ (e.g., dispensability) and a response $K$ (evolutionary rate), so that $D = X + e_D$ and $K = X + e_K$, where $e_D$ and $e_K$ are noise terms with mean 0 and variances $\sigma_D^2$ and $\sigma_K^2$. Further, assume that we cannot measure $X$ but only a noisy correlate, $X' = X + e_{X'}$. In this model, $X$ is responsible for all the correlation between $D$ and $K$. We let $X$ be normally distributed with mean 0.5 and SD 0.25 (so that $X$ values span the unit interval) with the observable predictors $X'$, $D$, and $K$ equal to $X$ plus zero mean normally distributed noise with SD of 0.3. We ran each analysis 100 times with 3,000 measurements each.

Partial correlation analysis suggests that both $D$ and $X'$ contribute to the rate $K$ independently and with equal strength:

<table>
<thead>
<tr>
<th>Partial Correlation with $K$</th>
<th>$P$ Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_{DK</td>
<td>X} = 0.296 \pm 0.03$</td>
</tr>
<tr>
<td>$r_{X</td>
<td>K,D} = 0.291 \pm 0.02$</td>
</tr>
</tbody>
</table>

Multivariate regression similarly suggests that both $D$ and $X'$ independently influence the rate $K$:

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Percent Variance in $K$ Explained ($R^2$)</th>
<th>$P$ Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$X'$</td>
<td>16.9 $\pm$ 2</td>
<td>$&lt;10^{-9}$</td>
</tr>
<tr>
<td>$D$</td>
<td>17.3 $\pm$ 2</td>
<td>$&lt;10^{-9}$</td>
</tr>
</tbody>
</table>

Principal component regression, however, properly identifies only one component which contributes significantly to the rate $K$. The two components identified are $X' + D$, which measures mostly $X$, and $X' - D$, which measures mostly noise. Component 1 alone carries predictive value for $K$.

We may proceed with the confidence that we have properly identified the number and strength of the underlying determinants of $K$.

In general, the underlying variable represented by the dominant component is not known a priori and its identification requires additional insight. In this case, we know it is $X$, which is accurately captured by the principal component regression method, but not by the other methods. Other methods are therefore likely to lead to erroneous results when faced with the problem of trying to find true predictors within noisy data. Principal component regression, as shown here, is unlikely to do so.

Our toy model underscores a key observation: in the presence of noisy and correlated data, nonzero partial correlations and $R^2$ values from multivariate regression, even those with very high statistical significance, must not be taken as evidence for independent effects, contrary to previous studies (Lemos et al. 2005; Wall et al. 2005).

**Supplementary Material**

All data and scripts used to perform our analyses are available as supplementary material at *Molecular Biology and Evolution* online (http://www.mbe.oxfordjournals.org/).

**Acknowledgments**

We are grateful to Frances H. Arnold for insightful comments on the manuscript. C.O.W. was supported by National Institutes of Health (NIH) grant AI 065960 and D.A.D. was supported by NIH National Research Service Award 5 T32 MH19138.

**Appendix**

Spurious Partial Correlations from Noisy Data

Consider a model in which a variable $X$ determines two other variables $D$ and $K$ in a linear fashion. Then we can write, without loss of generality,

$$D = X + e_D, \quad K = X + e_K,$$

where $e_D$ and $e_K$ are noise terms with mean 0 and variances $\sigma_D^2$ and $\sigma_K^2$, respectively. We assume that these noise terms are each independent of $X$ and of each other. In the following analysis, we also assume for convenience that $X$ has variance 1; results for the case when $X$ has an arbitrary variance $\sigma_X^2$ follow by dividing all other variances in the problem by $\sigma_X^2$ in the equations below.

The partial correlation between $D$ and $K$ given $X$ is defined as

$$r_{DK|X} = \frac{r_{OK} - r_{DX}r_{KX}}{\sqrt{(1 - r_{DX}^2)(1 - r_{KX}^2)}},$$

where $r_{ij}$ is the standard Pearson correlation between variables $i$ and $j$. Given the model (1), it is intuitively obvious
that $r_{DKX}$ should be 0 because $e_D$ and $e_K$ are independent noise sources. Indeed, we find in this case

$$r_{DK} = \frac{E(DK) - E(DE)E(K)}{\sigma_D\sigma_K} = [(1 + \sigma_D^2)(1 + \sigma_K^2)]^{-1/2},$$

$$r_{DX} = (1 + \sigma_D^2)^{-1/2}, \quad r_{KX} = (1 + \sigma_K^2)^{-1/2},$$

(3)
giving $r_{DKX} = 0$. In the above, $E(\cdot)$ denotes expected value.

We now consider the question of whether it is possible that we observe a spurious partial correlation between $D$ and $K$ if we are given a somewhat noisy version of $X$ instead of $X$ itself. Thus, we introduce the new variable $X = X + e_X$, where the noise $e_X$ is assumed to have mean 0 and variance $\sigma_X^2$, and now compute the partial correlation $r_{DKX}$ because this is the actual partial correlation we would observe if we were given noisy samples of $X$. We find that $r_{DK}$ remains the same as in equation (3), while $r_{DX}$ and $r_{KX}$ are now given by

$$r_{DX} = [(1 + \sigma_D^2)(1 + \sigma_X^2)]^{-1/2},$$

$$r_{KX} = [(1 + \sigma_K^2)(1 + \sigma_X^2)]^{-1/2},$$

(4)

and the new partial correlation is

$$r_{DKX} = \frac{\sigma_X^2}{\sqrt{(\sigma_D^2 + \sigma_X^2 + \sigma_D\sigma_X)(\sigma_K^2 + \sigma_X^2 + \sigma_K\sigma_X)^2}}.$$  

(5)

Thus, the presence of noise in the samples of $X$, characterized by the variance $\sigma_X^2$, leads to a nonzero spurious partial correlation between $D$ and $K$. Because equation (5) is quadratic in $\sigma_X^2$, we can also write it in terms of the amount of noise on $X$ that would result in a given spurious partial correlation:

$$\sigma_X^2 = \frac{\sigma_X^2(1 + \sigma_D^2) + \sigma_D^2(1 + \sigma_X^2) + \sqrt{(\sigma_X^2 - \sigma_D^2)^2 + 4r_{DKX}^2\sigma_X^2\sigma_D^2}}{2(r_{DKX}^2 - (1 + \sigma_D^2)(1 + \sigma_X^2))}.$$  

(6)

We may alternatively specify a significance level as a $P$ value $P$, for the desired spurious correlation and the number of data points $n$, and ask what noise level in $X$ is required to achieve the given significance. Based on asymptotic (large $n$) results, the $P$ value for testing significance of the partial correlation is given (Wall et al. 2005) as

$$P = 2[1 - \Phi(t)], \quad t = r\sqrt{\frac{n - 3}{1 - r^2}},$$  

(7)

where $\Phi(\cdot)$ denotes the standard normal cumulative distribution function, and $t$ is a partial correlation. Solving for the partial correlation in terms of $P$ and $n$, we obtain

$$t^2 = 1 + \frac{n - 3}{\sigma_X^2 - 1 - P/2},$$  

(8)

where $z_{0.05}$ is the 100 × $\gamma$th percentile of the standard normal distribution. Given a $P$ value $P$ and the number of data points $n$, we may therefore use equation (8) to find the corresponding partial correlation $r$ and then substitute this partial correlation in equation (6) to find the noise level in $X$ that would produce that partial correlation to the desired significance.

There are a number of important consequences and special cases of equations (5) and (6):

(i) For fixed $\sigma_D$ and $\sigma_K$, $r_{DKX}$ is maximized when $\sigma_X^2 \to \infty$. This maximum achievable partial correlation is given by

$$r_{DKX} \to [(1 + \sigma_D^2)(1 + \sigma_K^2)]^{-1/2}.$$  

(9)

(ii) As expected, $r_{DKX}$ increases as the noise level on $X$ increases. Perhaps, less intuitive is the fact that the partial correlation also increases as the noise levels on $D$ and $K$ become smaller. In the limit that $D$ and $K$ are perfectly clean ($\sigma_{DX} = 0$), we find a perfect but spurious partial correlation of 1 with an arbitrary, nonzero $\sigma_X$. Thus, if we are given noisy samples of $X$, we would be falsely led to conclude that $D$ and $K$ are well-correlated even if we control for $X$.

(iii) When $\sigma_K$ and $\sigma_D$ are comparable, i.e., $\sigma_K \approx \sigma_D = \sigma_C$, equation (6) simplifies to yield

$$\sigma_X^2 = \frac{\sigma_X^2}{r_{DK}^2 - (1 + \sigma_D^2)(1 + \sigma_X^2)}.$$  

(10)

With $\sigma_C = 1$ (almost a worst-case scenario: in most realistic situations, $\sigma_C$ will be much smaller than the variation in $X$, and we would then need a much smaller noise level in $X$ in order to obtain a significant $r_{DKX}$) we find, using equation (8) with $P = 0.05$ (95% significance) and equation (10), that $\sigma_X^2 = 0.11$ for $n = 500$ and $\sigma_X^2 = 0.07$ for $n = 1,000$. Thus, for 1,000 data points, and assuming a large noise on $D$ and $K$, we only need a modest (~7% of the variance in $X$) amount of noise to achieve a 95% significant partial correlation. This noise level would, of course, be much lower if $D$ and $K$ were less noisy.

(iv) When $n$ is large, equation (8) implies that a small partial correlation is needed to achieve significance. We may therefore assume that the $r^{-2}$ terms dominate in equation (6), which may then be combined with equation (8) to yield, for large $n$,

$$\sigma_X^2 \approx \frac{\sigma_K\sigma_D^2 z_{0.05}/2}{\sqrt{n}},$$  

(11)

which directly expresses the noise level $\sigma_X$ required to achieve significant partial correlation in terms of $n$ and $P$. This shows that for fixed $\sigma_D$, $\sigma_K$, and $P$ the amount of noise on $X$ that is required to achieve significance decreases as $1/\sqrt{n}$ for large $n$.

Partial Correlations in Terms of Measurable Quantities

Because all variances in equations (5) and (6) are really ratios with respect to the true variance of $X$, it may appear that we need to know the true variance of $X$, an unmeasurable quantity, in order to find $r_{DKX}$. This is, however, not the case. Suppose we make two measurements of a variable $Y = X + e_Y$ (here, $Y$ could stand for any of $X$, $D$, or $K$), where $e_Y$ is a noise source with mean 0 and variance $\sigma_{e_Y}^2$. 


These two measurements, say, $Y_1$ and $Y_2$, can be expressed as $Y_1 = X + e_1$, $Y_2 = X + e_2$, where $e_1$ and $e_2$ are independent, identically distributed noise sources with the same distribution as $e_Y$. The Pearson correlation between the two measurements $Y_1$ and $Y_2$ is then given by

$$r_Y = \frac{E(Y_1Y_2) - E(Y_1)E(Y_2)}{\sqrt{\text{Var}(Y_1)\text{Var}(Y_2)}} = (1 + \sigma^2_Y)^{-1},$$

where we have assumed, as before, that the variance of $X$ itself is set to 1. We can therefore use equation (12) to express the variances of $X$, $D$, and $K$ in equations (5) and (6) in terms of the two-measurement correlations $r_{X',D}$, $r_{D,K}$, respectively, as

$$\sigma^2_{X',D,K} = (r_{X',D})^{-1} - 1.$$

Such a substitution ensures that the true variance of $X$ does not appear in equations (5) and (9) and that these equations are expressed directly in terms of measurable quantities. In particular, equation (9) takes the particularly simple form $r_{DK|X} \to \sqrt{r_{D/K}^2 \sigma_X^2} \to \infty$ (or $r_{X'} \to 0$), and equation (10) becomes, with $r_c = r_{D/K}$ or $r_c = r_{D/K}$:

$$r_X = \frac{1 - r_{DK|X}^2}{1 - r_{D/K}}.$$

**Literature Cited**


Edward Holmes, Associate Editor

Accepted October 10, 2005