The stellar mass fraction and baryon content of galaxy clusters and groups

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Accepted 2010 April 16. Received 2010 April 9; in original form 2009 October 19

ABSTRACT
The analysis of a sample of 52 clusters with precise and hypothesis-parsimonious measurements of mass, derived from caustics based on about 208 member velocities per cluster on average, shows that low-mass clusters and groups are not simple scaled-down versions of their massive cousins in terms of stellar content: lighter clusters have more stars per unit cluster mass. The same analysis also shows that the stellar content of clusters and groups displays an intrinsic spread at a given cluster mass, i.e. clusters are not similar to each other in the amount of stars they contain, not even at a fixed cluster mass. The stellar mass fraction depends on halo mass with (logarithmic) slope $-0.55 \pm 0.08$ and with $0.15 \pm 0.02$ dex of intrinsic scatter at a fixed cluster mass. These results are confirmed by adopting masses derived from velocity dispersion. The intrinsic scatter at a fixed cluster mass we determine for gas mass fractions taken from literature is smaller, $0.06 \pm 0.01$ dex. The intrinsic scatter in both the stellar and gas mass fractions is a distinctive signature that individual regions from which clusters and groups collected matter, a few tens of Mpc wide, are not yet representative of the mean gas and baryon content of the Universe. The observed stellar mass fraction values are in marked disagreement with gasdynamics simulations with cooling and star formation of clusters and groups. Instead, the amplitude and cluster mass dependency of observed stellar mass fractions are those required not to need any active galactic nuclei (AGN) feedback to describe gas and stellar mass fractions and X-ray scale relations in simple semi-analytic cluster models. By adding stellar and gas masses and accounting for the intrinsic variance of both quantities, we found that the baryon fraction is fairly constant for clusters and groups with masses between $10^{13.7}$ and $10^{15.0} M_\odot$ and it is offset from the WMAP-derived value by about $6 \sigma$. The offset is unlikely to be due to an underestimate of the stellar mass fraction, and could be related to the possible non-universality of the baryon fraction, pointed out by our measurements of the intrinsic scatter. Our analysis is the first that does not assume that clusters are identically equal at a given halo mass and it is also more accurate in many aspects. The data and code used for the stochastic computation are distributed with the paper.

Key words: methods: statistical – galaxies: clusters: general – galaxies: luminosity function, mass function – galaxies: stellar content – cosmology: observations – X-rays: galaxies: clusters.

1 INTRODUCTION
Knowledge of the baryon content of clusters and groups is a key ingredient in our understanding of the physics of these objects and in their use as cosmological probes. In fact, clusters have accreted matter from a region of some tens of Mpc, large enough that their content should be representative of the mean matter content of the Universe (White et al. 1993). If this is the case, by measuring the baryon fraction in clusters, $f_b$, and coupling it with an estimate of $\Omega_m$, for example from primordial nucleosynthesis arguments or from CMB anisotropies, gives $\Omega_m = \Omega_b f_b$ (e.g. White et al. 1993; Evrard 1997). Secondly, the study of how baryons are distributed in gas and stars and the way this splitting depends on halo (cluster or group) mass should provide clues to the role played by the various physical mechanisms potentially active in clusters and groups. However, the baryon fraction is far from being fully understood: the WMAP-derived value of the baryon fraction is larger than all values obtained in X-ray analysis (i.e. Vikhlinin et al. 2006) even accounting for baryons in stars (e.g. Gonzalez, Zaritsky & Zabludoff 2007), and gas depletion (e.g. Nagai, Kravtsov & Vikhlinin 2007). X-ray scaling relations (e.g. halo mass versus...
temperature or X-ray luminosity) predicted on the assumption that the thermal energy of the gas comes solely from the gravitational collapse are notoriously in disagreement with observed scalings (e.g. Vikhlinin et al. 2006). Observed and predicted scalings may be brought into agreement by allowing star formation and eventually a further feedback (e.g. Kravtsov, Nagai & Vikhlinin 2005; Nagai et al. 2007; Bode, Ostriker & Vikhlinin 2009; Fabjan et al. 2010). In particular, whether a further feedback, i.e. in addition to the stellar one, is needed is largely unknown because of the uncertainty of the observed stellar mass content of clusters (e.g. Bode et al. 2009).

More generally, recent works on the subject manage to reproduce X-ray derived quantities (e.g. baryon fraction or mass–temperature scaling relations) by basically adding to the cluster model a further degree of freedom associated with star formation (e.g. Nagai et al. 2007; Bode et al. 2009; Fabjan et al. 2010), without adding the corresponding observational constraint, i.e. requiring that the stellar mass produced in the model fit the data. We emphasize that gas properties strongly depend on the amount of stellar mass allowed in the model (e.g. Kravtsov et al. 2005; Nagai & Kravtsov 2005; Nagai et al. 2007) and a constraint on the stellar component has a direct and important consequence on the gas component of the model.

Several observational determinations of the stellar mass fraction have important limitations: published works studied clusters with unmeasured, or very poorly measured, masses and unmeasured reference radii, while these quantities need to be known for the determination of the stellar mass fraction, as discussed in later sections. It is clear, therefore, that an observational measurement of the stellar mass fraction of clusters with known masses and reference radii is valuable.

The caustic method (Diaferio & Geller 1997; Diaferio 1999) offers a robust path to estimating cluster mass and reference radii. It relies on the identification in projected phase space (i.e. in the plane of line-of-sight velocities and projected cluster-centric radii, \(v, R\)) of the envelope defining sharp density contrasts (i.e. caustics) between the cluster and the field region. The amplitude of such an envelope is a measure of the mass inside \(R\). As opposed to masses derived in other ways (e.g. from X-rays, from velocity dispersion, from the virial theorem, from the Jeans method, etc.), caustic masses do not require that the cluster is in dynamical equilibrium (see Rines & Diaferio 2006 for a discussion). There is a good agreement between caustic and lensing masses for the very few clusters where both measurements are available (Diaferio, Geller & Rines 2005). On larger cluster samples, caustic masses also show a good agreement with virial masses (e.g. Rines & Diaferio 2006; Andreon & Hurn 2010) and with the extrapolation to larger radii of dynamical masses derived through a Jeans analysis (Biviano & Girardi 2002). Both virial and Jeans masses require, however, the assumption that the cluster is in dynamical equilibrium.

This paper addresses: (a) the determination of the stellar mass fraction in a sample of clusters and groups with well-determined masses and reference radii derived by the caustic method, using, on average, 208 members per cluster; and (b) the determination of the average baryon content of clusters and groups.

Throughout this paper we assume \(\Omega_M = 0.3, \Omega_{\Lambda} = 0.7\) and \(H_0 = 70\ \text{km} \text{s}^{-1} \text{Mpc}^{-1}\). Magnitudes are quoted in their native system (quasi-AB for SDSS magnitudes).

## 2 Data and Sample

The final cluster (halo) sample consists of the 52 clusters and groups with accurate caustic masses (Rines & Diaferio 2006) fully included in the Sloan Digital Sky Survey (SDSS hereafter) 6th data release (Adelman-McCarthy et al. 2008). Fundamentally, clusters/groups are (a) X-ray flux-selected and (b) with an upper cut at redshift \(z = 0.1\) to allow a good caustic measurement. From the original Rines & Diaferio (2006) larger sample, we removed (in Andreon & Hurn 2010) only clusters at \(z < 0.03\) to avoid shredding problems (large galaxies are split into many smaller sources), two cluster pairs (requiring a deblending algorithm), and one further cluster, the NGC 4325 group, because it is of very low richness. In the present paper, one more group, MWK11, has been removed because the star/galaxy classification of SDSS is poor at this cluster location, as verified by visual inspection (see Section 3.2). It turned out also that MWK11 is the halo with smallest mass in our sample.

We emphasize that only two cluster pairs have been removed from the original sample because of their morphology; all the other excluded clusters have been removed because they are not fully enclosed in the sky area observed by SDSS, or have bad SDSS data, or have suspect masses because the algorithm used to compute the caustic mass converged on a secondary galaxy clump.

The basic data used in our analysis are \(g\) and \(r\) photometry from SDSS, down to \(r = 19\) mag. The latter value is the value where the star/galaxy separation becomes uncertain (e.g. Lupton et al. 2002) and is much brighter than the SDSS completeness limit (e.g. Ivezić et al. 2002). Specifically, we use Petrosian magnitudes for ‘total’ magnitudes, and ‘dered’ magnitudes for colours.

## 3 Analysis of the Individual Clusters

We want to measure the stellar mass fraction and its dependence on cluster mass. To do this, we must (a) measure cluster masses and determine reference radii, (b) determine the total luminosity in galaxies, (c) estimate the luminosity of other components (e.g. the brightest cluster galaxy and intracluster light) and (d) convert the stellar luminosity into stellar mass. In addition to the above, when the total baryon content is of interest, we also need the gas mass fraction.

About point (a), we adopted virial masses, \(M_{200}\), and virial radii, \(r_{200}\), from the caustic analysis of Rines & Diaferio (2006). For the sake of precision, \(r_{200}\) is the radius within which the enclosed average mass density is 200 times the critical density. Let’s consider the remaining points in turn.

### 3.1 Luminosity function and its integral

In order to measure the stellar mass of galaxies, we restrict our attention to red galaxies only: blue galaxies would increase little the stellar mass (e.g. Fukugita, Hogan & Peebles 1998). In fact: (a) blue galaxies have lower mass at a given luminosity in observations (e.g. Hoekstra et al. 2005) and in stellar population synthesis models (e.g. Bruzual & Charlot 2003); and (b) blue galaxies are, on average, fainter than red galaxies and less abundant in clusters. Therefore, their contribution to the total mass is negligible (e.g. Fukugita et al. 1998; Girardi et al. 2000) and thus neglected. Nevertheless, confirmation of the small role played by blue galaxies in the total stellar mass budget, perhaps derived from a better mass tracer such as near-infrared photometry, would be valuable especially for less massive clusters where their contribution is potentially higher in percentage.

In this paper we define red galaxies as those within 0.1 redward and 0.2 blueward in \(g-r\) of the colour–magnitude relation, precisely as in Andreon & Hurn (2010), and in agreement with works mentioned therein. For the colour centre, we took the peak of the colour distribution. For the slope, we adopted the best-fitting value
derived for the richest clusters. This definition of ‘red’ is quite simple because for our cluster sample results hardly depend on the details of the ‘red’ definition: the determination of the precise location of the colour–magnitude relation is irrelevant because the latter is much narrower than the adopted 0.3-mag width and because practically all galaxies brighter than the adopted luminosity cut are red. Colours are corrected for the colour–magnitude slope, but the precise slope determination is not critical given the reduced magnitude range explored (less than ±0.3 mag) and the shallow slope of the colour–magnitude relation.

The luminosity function is computed in two different ways: for display purposes we only bin galaxies in magnitude bins and we account for the background (galaxies in the cluster line of sight) computing the difference of counts in the cluster and a reference line of sight (e.g. Zwicky 1957; Oemler 1974, and many papers since these), the latter taken outside the cluster turnaround radius or near to it for clusters near the SDSS sky boundaries. For display purposes only, errors are computed with the usual quadrature sum rule. For our formal analysis, instead, we take a Bayesian approach as done for other clusters (e.g. Andreon 2006; Andreon et al. 2006, 2008b, etc.): we use the likelihood given in Andreon, Punzi & Grado (2005), which is the extension of the Sandage, Tammann & Yahil (1979) likelihood to the case when a background is present. We fit each cluster independently on the other ones and without binning data in magnitude bins. We adopt uniform priors for all parameters, and we note that any other weak prior would have returned a similar result because parameters are well determined by the data. For the same reason, a maximum likelihood analysis, such as the one advocated in Andreon et al. (2005), would have returned identical values for the parameters (but with different meanings). However, the Bayesian approach has a number of advantages, amongst which is that it makes it trivial to compute uncertainties on derived parameters, as the error on the integral of the luminosity function (that we need in order to estimate the stellar mass fraction), fully accounting for the covariance of all error terms and with just one line of code (by typing the about 20 characters in equation 1 below). As usual, all magnitudes are internally zero-pointed to a number near to the average, because this has a number of numerical advantages.

Fig. 1 exemplifies our analysis for two clusters, chosen as those having the third best and worst determination of the stellar mass: top panels show galaxy counts in the cluster (solid dots) and reference (open dots) line of sight. The cluster contribution is the excess over the reference line of sight. The background is modelled with a second-degree power law, the cluster with a Schechter (1976) function with the usual parameters $\alpha$ (faint-end slope), $\phi^*$ (normalization) and $M^*$ (characteristic magnitude). The lines show the fitted model to unbinned data. The bottom panel shows the cluster LF as classically derived (points with the mentioned heuristic error bars) and its Bayesian derivation (mean model with 68 per cent confidence bounds on it, shaded in yellow).

The analysis is repeated for all 52 (plus one, later discarded) studied clusters.

The total luminosity is given by the integral of the luminosity function that, for a Schechter (1976) function, is given by

$$L_{\text{tot}} = \phi^* L^* \Gamma(\alpha + 2).$$  \(1\)

Figs 2 and 3 show the $M^*$ versus $\alpha$ and $M_{\text{tot}}$ versus $\alpha$ of the cluster Abell 954. These figures clarify a number of technical aspects. First, there is a covariance between these quantities. Secondly, as shown for Abell 954 from the comparison of Figs 2 and 3, the error on $M_{\text{tot}}$
is smaller than the quadrature sum of its parts, and also than the $M'_* \alpha$ error alone, owing to the covariance between variables. For our sample of 52 clusters, the average $M'_*$ error is 0.45 mag and the average $M_* \alpha$ error is 0.21 mag. Thirdly, if, following almost all previous literature works (e.g. Lin, Mohr & Stanford 2003; Gonzalez, Zaritsky & Zabludoff 2007; Giodini et al. 2009, etc.), a single value of $\alpha$ is instead taken (justifying the above by stating that $\alpha$ is undetermined from the available data), then the derived error would underestimate the true error on $M_*$, (and even more so the one on $M'_*$). In fact, what literature works measure is the vertical thickness at a given $\alpha$, instead of the overall width, obtained by projecting the likelihood (posterior) on the y-axis (i.e. marginalizing on $\alpha$).

The luminosity we derived thus far is the one emitted from cluster galaxies in a cylinder of radius $r_{200}$. To compute the stellar mass fraction we need instead the luminosity within a sphere, the latter derived from the luminosity in a cylinder assuming a Navarro, Frenk & White (1997) distribution with concentration equal to 3. If, instead, the true value of the concentration would be 5, then we would be underestimating stellar masses by 0.02 dex, a negligible quantity compared to the final stellar mass uncertainty (0.08 dex, on average, Section 3.4).

3.2 The bright and faint ends

The lower panel of Fig. 1 is very useful in detecting the presence of galaxies that might give a large contribution to the total cluster flux, like the brightest cluster galaxy (BCG hereafter) but also bright galaxies unrelated with the cluster or misclassified bright stars. Every galaxy near to, or brighter than, one-fifth of the total flux has been carefully checked. Furthermore, several fainter galaxies, down to the magnitude where the (preliminary computed) LF predicts less than one galaxy, were also checked. First of all, we inspected the SDSS image, and we sometimes found that the checked galaxy is instead a misclassified and saturated star. In such a case, the object is removed from the sample. In such a check, we noted that the SDSS star/galaxy classification is poor at the location of the cluster MKW11 (there are many stars misclassified as galaxies), which has been removed from the sample. Then, we checked if the candidate BCG is a cluster member or a foreground galaxy by searching its redshift in the SDSS and NED archives and comparing it to the cluster redshift. We found that the checked galaxy has either a fairly different redshift ($\Delta v > 4000$ km s$^{-1}$) and, in that case, we removed it from the sample, or very near to it (less than a few hundreds km s$^{-1}$) and we kept it in the sample. At this point we have six BCGs much brighter than the LF, all spectroscopically confirmed as cluster members. We now consider the possibility that BGCs are not drawn from the Schechter (1976) function, in the light of several literature claims that BCGs may be drawn from a different distribution (e.g. Tremaine & Richstone 1977). In order to guard against the risk of missing this source of stellar mass, we (temporarily) remove the object from the sample, or better, we remove a magnitude range largely including the BCG, and we recompute the LF rigorously accounting for missing luminosity range (censored and truncated observations, e.g. in Andreon et al. 2005). We re-integrate the model LF over the full luminosity range, and we add back the temporarily removed BCG flux. We find that the median flux of the six BCGs is 16 per cent of the cluster flux.

It is well known that shallow photometric data miss the flux coming from the galaxy outer regions (e.g. Andreon 2002) or, equivalently, that Petrosian magnitudes listed in the SDSS catalogue underestimate the total galaxy flux (e.g. Blanton et al. 2001). For de Vaucouleurs (1948) profiles, typical of red galaxies of interest here, Petrosian magnitudes underestimate the total flux by about 15 per cent (Blanton et al. 2001) for galaxies with the size of those studied in this paper. Our total flux is corrected for this missed flux.

There is one more component to be accounted for, the intracluster light (ICL). Of course, it should be counted only once in our measurement of the total flux. Therefore, its value should not include the light coming from the galaxy outer haloes, from the BCG, and from faint galaxies (e.g. too faint to be individually detected) because we already accounted for these three terms. Zibetti et al. (2005) measure it by accounting for the three mentioned terms on a stack of clusters and found a small (10 per cent within 500 kpc, about $r_{200}$/2 for their clusters) and decreasing fraction with clustercentric radii. At the radius of interest, $r_{200}$, it is a minor term, and therefore it is neglected. The small spatial extent of the ICL is confirmed by the Gonzalez et al. (2007) analysis: 80 per cent of the BCG+ICL total light is contained in the inner 300 kpc.

We can independently confirm the smallness of the ICL luminosity using measurements from Gonzalez et al. (2007), after accounting for different definitions of ICL among works. These authors measured the intracluster+BCG light and found that 30 per cent of the total light is in the intracluster+BCG light at $r_{200}$. These authors studied clusters that contain a dominant BCG. We estimate the contribution of the BCG light in the Gonzalez et al. (2007) sample as similar to the one in clusters dominated by a BCG in our own sample, about 16 per cent. Gonzalez et al. (2007) quote that a few more per cent of the faint galaxy flux, which we counted with the LF, ends up in their BCG+ICL measurement, and we comment that a few more per cent of the flux from the galaxy halo also likely ends up in their BCG+ICL measurement. In summary, the ICL, defined as in our own paper, measured by Gonzalez et al. (2007) is 10 per cent with large errors, because of the indirect path used to infer it. This estimate confirms the measurement performed by Zibetti et al. (2005): the ICL (as defined in our own and Zibetti et al.’s paper) contribution is negligible at $r_{200}$. We emphasize that some other papers use the term ‘cD halo’ to indicate the flux that is counted with/as ‘intracluster light’.

3.3 The luminosity to stellar mass conversion

For the luminosity to stellar mass conversion, we adopt the $M/L$ value derived by Cappellari et al. (2006). As in previous works, we assume that in the galaxy regions studied by Cappellari et al. (2006) the contribution of non-stellar matter is negligible.

The data of Cappellari et al. (2006) are also consistent with up to 30 per cent non-stellar matter. If it is 15 per cent on average, then stellar masses would be 0.07 dex lower. If stellar masses were instead derived assuming an old single stellar population of solar metallicity and Chabrier initial mass function, we would find only 0.1 dex lower values.

3.4 Results

Table 1 gives the stellar masses found within $r_{200}$ and their errors. Stellar mass errors are small in absolute terms, 0.08 dex on average, and also smaller than halo mass errors (i.e. errors from caustics, 0.14 dex on average).

Fig. 4 plots the stellar mass, derived in the present paper, against the cluster richness $n_{200}$, i.e. the number of red galaxies brighter than $M_g = -20.0$ mag, derived for the very same sample by Andreon & Hurn (2010). There is a good agreement between the two quantities, which are basically two ways to summarize the luminosity content.
Table 1. Stellar masses and errors.

<table>
<thead>
<tr>
<th>id</th>
<th>log $M_\star$ [M$_\odot$]</th>
<th>id</th>
<th>log $M_\star$ [M$_\odot$]</th>
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</table>

Figure 4. Richness versus stellar mass. There is a tight relation between the number of bright red galaxies, $n_{200}$, and the total stellar mass, $M_\star$, in clusters. The line marks a relation with slope one.

of clusters (by counting galaxies or photons):

$$\log M_\star = (\log n_{200} - 2) + 13.04 \pm 0.03.$$

The slope of the regression is fixed to 1.0 (it is not a fit to the data) and the quoted error is just the formal error. For our sample, the two quantities, $\log M_\star$ and $\log n_{200}$, are known with the same amount of precision (0.08 dex).

The good agreement between the two summaries of the cluster luminosity content is a confirmation of the correctness of the two derivations. We note, in fact, that the present derivation uses a more constrained model (a shape for the luminosity function and for background galaxy counts), and more (i.e. also fainter) data than the derivation of $n_{200}$ in Andreon & Hurn (2010). The proportionality of stellar mass and richness is in agreement with the very small, if any, dependency of the faint end slope of the luminosity function with richness (e.g. Garilli, Maccagni & Andreon 1999; Paolillo et al. 2001; Andreon 2004), and with the direct determination of Rines et al. (2004) from a small sample of nine clusters. These authors consider, however, $\log M_\star$ and $\log n_{200}$ integrated down the same limiting magnitude, differently from our choice.

3.5 Comparison with literature

Our stellar mass determination fundamentally differs from previously published works from three major points of view: (a) in the way we choose the clusters to be studied; (b) in the adopted reference radius; and (c) in the performed analysis.

(a) First and foremost, if a precise stellar mass within a reference radius of clusters has to be derived, it is strongly preferable (not to say essential) that the following hold.

(i) The studied clusters are truly existing objects. Our clusters and groups are truly existing objects, with an extended X-ray emission and, on average, 208 spectroscopically confirmed members. Most of the Giodini et al. (2009) systems are noisy X-ray detections which are ambiguous in terms of both detection and extent, ‘cleaned’ by asking a spatial matching with an oversaturation of galaxies to decrease contamination by point sources and blends of point sources misclassified as extended X-ray sources (Finoguenov et al. 2007). Only half of the ‘surviving’ detections have three or more concordant redshifts (Giodini et al. 2009), and only a minority are currently spectroscopically confirmed, according to Gal et al. (2008), which shows that three
concordant redshifts occur frequently by chance in real redshift surveys (a further example is given in section 3.6 of Andreon et al. 2009 using the VVDS survey).

(ii) The reference radius in which stellar masses have to be measured is known and individually measured. All our clusters have individually measured radii (by Rines &Diaferio 2006). Clusters in Gonzalez et al. (2007) and Giodini et al. (2009) have radii inferred from X-ray scaling relations assuming that these are scatter-free, contrary to observations (e.g. Stanek et al. 2006; Vikhlinin et al. 2009; Andreon & Hurn 2010). In other terms, these works assume that the radius appropriate for the studied clusters is that of an average cluster having the same observable (e.g. X-ray flux), ignoring that clusters have a variety of radius values, even restricting attention to those with a given value of the observable (say, X-ray luminosity, it is just enough to consider cool-core and not-cool-core clusters). In passing, the scaling adopted by Gonzalez et al. (2007) is said to be in agreement with Hansen et al. (2005), which is now known to return radii wrong by a factor of 2 (Rykoff et al. 2008; Sheldon et al. 2009).

(iii) The studied clusters are located in a narrow range of redshift, in order not to be obliged to assume an evolution on cluster scaling relation (e.g. how the Lx-mass scaling evolves) or on M/L. All our clusters are in the local Universe (z < 0.1), saving us from making a hypothesis on how to relate parameters (masses, virial radii, etc.) measured at widely different redshifts. Other works (e.g. Giodini et al. 2009) consider objects in a large redshift range (e.g. 0.1 < z < 1) and neglect the uncertainty on evolution.

(b) We believe our adopted radius, r200, is a better choice for the determination of stellar masses than the radius adopted by other authors, r500. First, r500 is small enough that the stellar mass within r500 depends on the precise definition of ‘centre’ (barycentre, BCG location, X-ray peak, etc.). If the centre is measured with a finite degree of accuracy (which is often the case), a small radius leads to a systematic underestimation of the stellar mass because of centroiding errors. If instead one pretends that the cluster centre is coincident with the BCG location, then a systematic overestimate is introduced, because the observationally derived value will be boosted by the presence of the BCG. Systematics are strongly reduced if r200 is used, as it encloses most of the cluster. The r500 radius also makes an underoptimal use of the optical data; stellar masses have smaller error if r200 is used in place of r500, as is fairly obvious (r500 is only a few times the BCG size), and as we verified for our sample. Furthermore, the choice of a larger radius makes the BCG and intracluster light contribution small in percentage, thus making their precise contributions largely irrelevant for the aim of determining the total amount of mass in stars (and in baryons). A larger than r500 radius is also what is needed to compare with theory, because the latter has big difficulties in predicting the stellar mass fraction on such a small scale. On the other hand, the use of a radius larger than r500 makes the computation of the total baryon mass fraction more complicated, the gas mass fraction usually being measured at smaller radii.

(c) Concerning the analysis, the way we derived the integral of the luminosity function is rigorous: the use of the likelihood function for unbinned data is a significant improvement (Cash 1976; Sandage et al. 1979; Andreon et al. 2005; Humphrey, Liu & Buote 2009) over previous approaches that bin data, and even a bigger improvement over those that use simplified schemes, as quadrature sums, to combine errors (see Andreon, Punzi & Grado 2005, for details). Furthermore, differently from previous works, we do not identify the luminosity function, which is a positively defined quantity, with the difference of two galaxy counts, which may be negative. Our choice of marginalizing over the LF parameters is in agreement with axioms of probability and logic. Keeping some of them, e.g. α, fixed as in most literature papers, contradicts them. Finally, and differently from all other works, we allow each cluster to have its own faint end slope and characteristic magnitude, given that the luminosity function differs from cluster to cluster (e.g. Virgo and Coma clusters: Binggeli, Sandage & Tammann 1988).

4 COLLECTIVE ANALYSIS OF THE WHOLE SAMPLE

4.1 Stellar mass versus halo mass

In order to fit the trend between stellar and total mass we use the statistical model (fit) detailed in the Appendix. Essentially, our model assumes that the true stellar mass and true halo mass are linearly related with some intrinsic scatter but rather than having these true values we have noisy measurements of both stellar mass and halo mass, with noise amplitude different from point to point. In the statistics literature, such a model is known as an ‘errors-in-variables regression’ (Dellaportas & Stephens 1995) and has been widely used before, including more complex situations (e.g. Andreon 2006, 2008; Andreon et al. 2006, 2008a,b; Kelly 2007; Andreon & Hurn 2010, etc.). The model is fully specified, and the code listed, in the Appendix.

Using the (fitting) model above, we found, for our sample of 52 clusters,

\[ \log M_* = (0.45 \pm 0.08) (\log M_{200} - 14.5) + 12.68 \pm 0.03. \]  

(2)

(Unless otherwise stated, results of the statistical computations are quoted in the form of \( x \pm y \), where \( x \) is the posterior mean and \( y \) is the posterior standard deviation.)

The left panel of Fig. 5 shows the relation between stellar mass and halo mass, observed data, the mean scaling (solid line) and its 68 per cent uncertainty (shaded yellow region) and the mean intrinsic scatter (dashed lines) around the mean relation. The ±1 intrinsic scatter band is not expected to contain 68 per cent of the data points, because of the presence of measurement errors.

Fig. 6 shows the posterior marginals for the parameters: slope, intercept and intrinsic scatter \( \sigma_{\text{iscat}} \). These marginals are well approximated by Gaussians.

The slope is very different from one, i.e. low-mass clusters are not simple scaled-down version of high-mass clusters: they have more stars per unit halo mass than their more massive cousins, in agreement with Girardi et al. (2000), and other works. Equivalently, the stellar mass fraction decreases with increasing stellar mass, as better shown in Section 4.3.

The intrinsic stellar mass scatter at a given halo mass, \( \sigma_{\text{iscat}} = \sigma_{\text{iscat}, \log M_{200}} \), is 0.15 ± 0.02 dex. This is the intrinsic scatter, i.e. the term left after accounting for measurement errors. It is clearly non-zero (see right panel of Fig. 6). This is a sort of ‘cosmic variance’: at a given halo mass, clusters are not all equal in terms of the amount of stars they have, but show a spread of stellar masses. Alternatively, the intrinsic scatter is a manifestation of an underestimation of the errors. This is unlikely to be the case, because an intrinsic scatter is seen also in gas masses and in numerical simulations of star and gas masses (discussed later), and therefore we need that errors on four different observables (observed gas and stellar masses, gas and stellar masses predicted in numerical simulations) are underestimated, which is unlikely. The next section addresses in detail a further hypothetical possibility, whether the intrinsic scatter
Stellar mass fraction and baryon content

Figure 5. Stellar mass versus cluster mass scaling. The solid line marks the mean relation between stellar mass and halo mass. Its 68 per cent uncertainty is shaded (in yellow). The dashed lines show the mean relation plus or minus the intrinsic scatter $\sigma_{\text{scat}}$. Error bars on the data points represent observed errors for both variables. The distances between the data and the regression line are due in part to the observational error on the data and in part to the intrinsic scatter. The left panel uses caustic masses; the right panel uses velocity-dispersion based masses fixed by numerical simulations.

Figure 6. Posterior probability distribution for the parameters of the halo mass–stellar mass scaling. The black jagged histogram shows the posterior as computed by MCMC, marginalized over the other parameters. The red curve is a Gauss approximation of it. The shaded (yellow) range shows the 95 per cent highest posterior credible interval.

of stellar masses is due to underestimated errors on caustic masses (an underestimate that, even if present, does not explain anyway why a scatter is also seen in numerical simulations). No matter which is the source of the intrinsic scatter, its presence has a few consequences: first, larger cluster samples are needed to measure the average stellar mass fraction with a given precision. Secondly, and conversely, the existence of a non-zero intrinsic scatter is a technical complication to be accounted for in the determination of the trend of stellar mass (or stellar mass fraction) versus cluster mass. The intrinsic scatter is, as mentioned, rigorously accounted for in our fitting model.

4.2 Checking caustic masses

Because of the relative novelty of caustic masses, and the hypothetical possibility that the intrinsic scatter on stellar masses might be due to an underestimation of caustic mass errors, we now replace caustic mass by a mass, $M_s$, derived from velocity dispersion using a relation calibrated with numerical simulations in Biviano et al. (2006). As shown in Andreon & Hurn (2010), the mass derived using the calibration in Evrard (1997) gives almost indistinguishable numbers, because the two calibrations are almost identical for our clusters. Velocity dispersions are taken from Rines & Diaferio (2006).

To use the masses $M_s$ in place of the caustic ones, we need to only write their values (and their errors) in the data file and run our fitting model, listed in the Appendix. Mass errors are derived by combining in quadrature velocity dispersion errors (converted in mass) and the intrinsic noisiness of $M_s$ (12 per cent, from Biviano et al. 2006). We found:

$$\log M_s = (0.53 \pm 0.08) \left( \log M_s - 14.5 \right) + 12.69 \pm 0.03$$

with an intrinsic scatter of $0.13 \pm 0.03$. By changing the source of halo masses, regression parameters (slope, intercept and intrinsic scatter) do not change. Therefore, the observed intrinsic scatter cannot be due to (unknown) systematics of caustic masses. Data and fit for velocity dispersion derived masses are shown in the right panel of Fig. 5.

The insensitivity of our results to which mass is used is expected, because in Andreon & Hurn (2010) we show the absence of a gross offset or tilt between caustic and velocity-dispersion based masses, and that the error quoted for the caustic mass is as precise as (or as wrong as) the error quoted for the velocity-dispersion based mass.

To summarize, the scatter on the amount of stars that clusters contain at a given halo mass is not due to an unaccounted systematic of the halo mass.
4.3 Stellar mass fraction

Fig. 7 plots the stellar mass fraction versus the cluster mass. The fraction is computed following its definition: it is the logarithmic difference between the stellar mass, $M_\star$, and the halo mass, $M_{200}$. The fit has been performed in the stellar mass versus halo mass plane, and so derived errors are shaded in Fig. 7. In addition to the exact analysis (marked with lines and shadings), we also report approximated errors, marked as error bars, based on just the error on stellar mass, for simplicity. Our fit to the data accounts for the intrinsic scatter, and also simply solves a further problem that affects previous analysis: the fit in the fraction versus halo mass plane performed by other authors (e.g. Gonzalez et al. 2007; Giodini et al. 2009) has the halo mass both on the abscissa and in the ordinate (it is at the denominator of the fraction). As a consequence, the values fitted by other works have correlated errors. However, past works used fitting methods that assume errors to be uncorrelated. Our solution, fitting in the stellar mass versus halo mass, where measurement errors are uncorrelated, solves this problem too.

The decrease in the stellar mass fraction is stunning, with a slope equal to $-1 + 0.45 \pm 0.08 = -0.55 \pm 0.08$. The quality of this result can be better appreciated by noting that the trend above was considered not constrained by data in recent papers: Allen et al. (2008) assume a stellar mass fraction proportional to the gas fraction (when instead the two fractions have opposite dependencies with halo mass, as shown in Fig. 8 and discussed in Section 4.4), whereas Ettori et al. (2009) considered a number of recipes, because of lack of conclusive data. Bode et al. (2009) consider the slope as a free (i.e. not constrained by any stellar fraction observation) parameter.

The value of the slope is robust to systematic errors affecting the conversion factor from luminosity to stellar mass. In fact, to bias the found slope, we need that the $M_\star/L$ value of the galaxies depends on the mass of the cluster. It is difficult to imagine why the initial stellar mass function (which largely regulates the $M_\star/L$ value) should be different in galaxies that are in clusters of different masses. Furthermore, the $M/L$ values in Cappellari et al. (2006) come from galaxies lying in haloes of different masses. Finally, the fundamental plane shows no halo-mass or environmental dependency (Pahre, de Carvalho & Djorgovski 1998).

After binning, the decrease in the stellar mass fraction becomes clearer, due to the smaller error bars of our cluster stacks. The horizontal lines in Figs 7 and 8 mark the Universe baryon fraction from the five-year WMAP results in Dunkley et al. (2009). 68 per cent credible intervals are shaded. This has to be taken as
an upper limit to the stellar mass fraction, because there are other baryons in clusters. Stars account for only about one-third at most of all baryons.

Table 2 lists derived stellar mass fractions and their errors.

### 4.4 Gas mass fractions

Vikhlinin et al. (2006) and Sun et al. (2009) data on the fraction of matter in the hot intergalactic gas are plotted in the right panel of Fig. 8, after converting them for minor differences in the adopted cosmological parameters.

Mases and gas mass fractions are measured within \( r_{500} \). Because of asymmetrical errors on \( f_{\text{gas}} \), we assume Gaussian errors on \( \log f_{\text{gas}} \) so that our previous fitting model can be applied without any change (apart for reading ‘gas fraction’ where ‘stellar mass’ is written). We found

\[
\log f_{\text{gas}} = (0.15 \pm 0.03) \left( \log M_{500} - 14.5 \right) - 0.97 \pm 0.02
\]

with an intrinsic scatter of 0.06 ± 0.01 dex. The right panel of Fig. 8 shows the derived mean \( f_{\text{gas}} \) versus halo mass fit (slanted solid line) and its 68 per cent uncertainty (shaded yellow region) and the mean intrinsic scatter (dashed lines) around the mean relation.

Intercept and slope posteriors are Gaussian shaped, whereas the intrinsic scatter posterior is a bit skewed, as a Gamma function (figure not shown). Our mean relation is similar to Sun et al.’s (2009) best fit. Their work, however, uses a similar, but not identical, cluster sample and a different fitting model. Our intrinsic scatter value cannot be compared with theirs, because these authors, even though they note a scatter, do not report its value, if measured at all.

Similarly to stellar masses and stellar mass fractions, gas fractions display an intrinsic variance, i.e. intrinsic differences from cluster to cluster. The scatter is not bounded to low-mass systems, but is apparent to all masses (see Fig. 8, and Vikhlinin et al. 2006, fig. 21), differently from some past claims of a spread at group (low) mass only. We emphasize that Vikhlinin et al. (2006) and Sun et al. (2009) selected and studied a sample of clusters and groups that, from X-ray images, appeared relaxed. Therefore, the observed spread of gas fractions at a given cluster mass is not due to the presence in the sample of clusters manifestly out of equilibrium (e.g. merging).

Table 2 lists derived gas mass fractions and their errors.

Given the importance of our claim that intrinsic scatter is not restricted to low-mass systems only, let’s look for an independent, although not equally precise, measurement.

The existence of an intrinsic scatter at high masses is confirmed by our analysis of gas fractions in Ettori et al. (2009). We took their \( f_{\text{gas}} \) values and errors, quoted at 68.3 per cent level of confidence, from their table 1. Their quoted errors are symmetric, and Gaussian distributed, because equation (7) in Ettori et al. (2009) only holds in this case. A Gaussian likelihood for \( f_{\text{gas}} \) is mathematically impossible, because a Gaussian is strictly positive everywhere on all the real axes, including impossible values for a fraction, those outside the [0, 1] range. It is therefore unsurprising that several of their quoted 68.3 per cent confidence intervals include unphysical (negative) values for a fraction. In order to select, from among their measurements, those for which the Gaussian approximation is an acceptable approximation, we select from their sample only the best measurements, defined as those having an \( f_{\text{gas}} \) determination with an S/N (\( = f_{\text{gas}}/\sigma_{f_{\text{gas}}} \)) larger than 3. This operation removes 31 out of the 52 of their clusters. We then carry out the gas fraction versus cluster temperature (the mass proxy listed in their paper) fits for the remaining 21 clusters, accounting for errors on both variables and a possible intrinsic scatter. Here, we reuse the fitting model given in the Appendix; we only need to read \( f_{\text{gas}} \) and \( kT \), where log stellar mass and log halo mass is written. We find

\[
f_{\text{gas}} = (0.000 \pm 0.004) (kT - 8) + 0.14 \pm 0.01
\]

with an intrinsic scatter of 0.03 ± 0.01 on \( f_{\text{gas}} \). Fig. 9 shows the derived mean \( f_{\text{gas}} \) versus cluster temperature fit (solid line) and its 68 per cent uncertainty (shaded yellow region) and the mean intrinsic scatter (dashed lines) around the mean relation. All clusters have \( kT > 5 \text{ keV} \), i.e. are very massive. Yet the intrinsic scatter is not zero, confirming that the intrinsic scatter in the gas mass fraction is not reserved to low-mass clusters only. The large majority (17 out of 21) of the fitted clusters have an observational error smaller than the intrinsic scatter. Therefore, by far the largest source of uncertainty in the determination of the average gas mass fraction of clusters (and of the baryon fraction of the universe, derived from these measurements) is the intrinsic scatter, and not the measurement error.

![Figure 9](https://academic.oup.com/mnras/article-abstract/407/1/263/984834/The-stellar-mass-fraction-and-baryon-content-of/clusters/92x300)
The value of the intrinsic scatter determined for the Ettori et al. (2009) subsample cannot be easily compared with the one derived for Vikhlinin et al. (2006) and Sun et al. (2009) for three reasons at least: first, the intrinsic scatter is the part of the scatter not due to observational errors. Therefore, its amplitude relies on the assumption that observational errors are precisely measured. As mentioned, the errors reported by Ettori et al. (2009) are noisy estimates of the true errors (see Andreon & Hurn 2010 for how to deal with noisy errors). Secondly, the scatter derived for the Ettori et al. (2009) sample is measured on a linear gas fraction scale, whereas the one for Vikhlinin et al. (2006) and Sun et al. (2009) is on a logarithmic scale (compare the left-hand sides of equations 4 and 5), and a Gaussian scatter on one scale cannot be translated to a Gaussian scatter on another scale. Finally, the scatter measured with the Ettori et al. (2009) data is for a given temperature, not for a given mass, as the ones measured with Vikhlinin et al. (2006) and Sun et al. (2009) data. If the above caveats are ignored, then one finds a good qualitative agreement between the two determinations of the intrinsic scatter after an approximate conversion to a common scale.

The existence of an intrinsic scatter in $f_{\text{gas}}$ (both at a given mass and at a given temperature) must surprise all those who believe that, having clusters from material collected from a large region, their content should be representative of the mean matter content of the Universe (White et al. 1993). The measured intrinsic scatter implies that individual regions from which clusters and groups collected matter, a few tens of Mpc wide, are not yet representative of the mean gas and baryon content (at large masses $f_{\text{gas}}$ is the largest baryon contributor) of the Universe, i.e. each region has a gas, and thus baryon, content that differs from the average by more than the observational error. The existence of an intrinsic scatter on $f_{\text{gas}}$ does not preclude the use of the gas or baryon mass fraction as determined in clusters for cosmological tests; it only decreases its efficiency (a larger sample is required to achieve the same precision), and obliges us to address selection effects, i.e. to enquire if studied clusters are representative, in terms of $f_{\text{gas}}$, of the population present in the Universe, or are a biased subsample. Therefore, cosmological constraints derived from $f_{\text{gas}}$ ignoring intrinsic scatter and $f_{\text{gas}}$ selection function (e.g. Ettori et al. 2009) are optimistically estimated, and, perhaps, biased.

4.5 Stellar and gas mass fractions

A comparison of the right and left panels of Fig. 8 shows that the halo mass at which stars and gas contribute equally to the total halo baryonic content is nearly $10^{13.5} M_\odot$ (roughly, $M_{200} \approx 1.5 M_{500}$).

Fig. 10 compares our observational constraints and theoretical predictions on the stellar (left panel) and gas (right panel) mass fraction. We consider gasdynamic simulations of Kravtsov et al. (2005) and Nagai et al. (2007). These simulations were performed in a (simulated) universe with a too low (compared to WMAP5) baryon fraction (0.14 versus 0.17). Therefore, we revise upward fractions derived in simulations by 0.17/0.14. Stellar mass fractions (Kravtsov 2009, private communication) are measured at $r_{200}$ in the simulations, as for data. Gas mass fractions for the very same simulations are taken from Nagai, Kravtsov & Vikhlinin (2007), and are measured within $r_{500}$, as for data. Gas fractions have been revised upward by 0.17/0.14, for the same reason as stellar fractions. The predicted fraction of matter in gas (open points, right panel) is near to the observed gas mass fraction, as commented in Kravtsov et al. (2009) and Nagai et al. (2007). Note in particular that simulated clusters also display a spread of gas and stellar mass fractions at a given halo mass, as real clusters.

As remarked by Kravtsov et al. (2009) and Gonzalez et al. (2007), the predicted stellar mass fraction (closed points, left panel) is off from the observed one (slanted solid line), and more evidently so in our paper than in previous works, given our more precise observational determination. Both the slope and the intercept of the simulations are in flagrant disagreement with the observed values. The gasdynamic simulations with star formation of Fabjan et al. (2010) show a very similar behaviour to the Kravtsov et al. (2009) and Nagai et al. (2007) simulations: the temperature–mass scaling and the gas mass fraction can only be reproduced if star formation is allowed, but in such a case the predicted stellar mass fraction (similar in the two sets of simulations) is off.

The mismatch between predicted and observed stellar mass fractions is not of secondary importance in the cluster model because of the strict interplay of the stellar and gas components. First, if fewer stars need to be formed, then more gas is left, and thus the current agreement between predicted and observed gas mass fractions is
corrupted. Secondly, the gas component responds to the feedback of the stellar component (e.g. Nagai et al. 2007; Fabjan et al. 2010). If the stellar part of the model has to be altered, changes in the gas predictions (e.g. X-ray scaling relations) occur. Unfortunately, the agreement between gas-related quantities, at the temperature–mass scaling, holds in current models for wrong stellar content predictions. Therefore, observations on the stellar mass fraction presented in this paper give a challenging constraint to theories of cluster formation.

Bode et al. (2009) presented a semi-analytical cluster model, i.e. they inserted a number of recipes in an N-body simulation. They concluded that if the stellar mass fraction has a logarithmic slope of $-0.49$, then there is no need of a supplementary feedback, i.e. in addition to the stellar one, to match the gas mass fraction and X-ray scale relations (temperature–mass, $Y_e$–mass). Our observed stellar mass fraction has a logarithmic slope of $-0.55 \pm 0.08$, which is consistent with the slope required to avoid supplementary feedback in the Bode et al. (2009) model.

In the Bode et al. (2009) model, this is a real model prediction; it has not been adjusted to match previous observational data on the stellar mass fraction slope. In contrast, the remaining model parameters commented on below have been adjusted to fit observations, diminishing the significance of the agreement between ‘predicted’ and observed values. The intercept of the model stellar mass fraction versus mass, kept fixed by Bode et al. (2009) to the Lin et al. (2003) value, also agrees with our observational determination: the Bode et al. (2009) model stellar mass fraction (dotted red line, left panel) is fully enclosed in the 68 per cent confidence band of our observational determination, i.e. it is in remarkable agreement. Similarly, the Bode et al. (2009) model gas mass fraction (dotted red line, right panel) is in reasonable agreement with our summary of observational data. If the simple Bode et al. (2009) cluster model is not an oversimplified description of true existing clusters, then the slope of the stellar mass fraction versus halo mass we determine in this paper implies that active galactic nuclei (AGN) feedback is not needed, at least not to reproduce X-ray scaling relations and stellar and gas mass fractions.

A couple of technical points are worth mentioning: in the Bode et al. (2009) model, the stellar mass fraction is determined within the virial radius, as our observational determination is, but is parametrized as a function of $M(<r_{500})$, which we converted to $M_{200} = M(<r_{200})$, assuming an NFW profile and a concentration of 3. Instead, gas mass fractions are computed within $r_{500}$ both for the model and for the data.

### 4.6 Stellar + gas mass fraction

In order to add the stellar and gas mass fractions to get the total fraction of baryons, we need to address some issues.

First, stellar and gas mass fractions are measured inside different reference radii ($r_{200}$ and $r_{500}$). Simulations show that the region inside $r_{500}$ is depleted, if any, by a small and poorly determined amount of the order of 2–10 per cent (Ettori et al. 2006; Kravtsov et al. 2005). We adopt a 5 per cent correction with a 3σ error of 6 per cent.

Secondly, we need to convert the fit in equation (3) from a fit versus $M_{500}$ to a fit versus $M_{200}$. The mass conversion is performed assuming an NFW of concentration 3. Any scatter of the concentration at a given mass or any change of the mean concentration with mass has little effect on this conversion, because equation (3) is the mean relation, and it is linear and shallow.

Thirdly, the gas and stellar masses measurements are assumed to be independent (which is true), and the intrinsic scatters of gas and stellar mass fractions around the mean are assumed to be unrelated to each other (which is unknown given the available data).

Fig. 11 displays the total fraction in baryons, $f_{\text{tot}} = f_{\text{gas}} + f_{\text{stars}}$, as a function of cluster mass, in the range where both $f_{\text{stars}}$ and $f_{\text{gas}}$ are constrained by the data, $13.7 \leq \log M_{200} \leq 15.0 M_\odot$. These values and errors come from the fit on individual data points in the stellar versus total mass plane and in gas mass fraction versus total mass, with the mentioned (minor) corrections. The variety of cluster properties at a given mass is fully accounted for by our derivation of $f_{\text{gas}}$ and $f_{\text{stars}}$.

Two points are striking in Fig. 11: (a) we observe an almost constant baryon fraction in the studied mass range, the increase of the gas mass fraction being approximatively compensated by the decrease of the stellar mass fraction; and (b) WMAP-derived baryon fraction differs from our estimate by about 6σ.

Readers interested in inferring the values of cosmological parameters from our measured baryon fraction should remember that our own determination of the baryon fraction has been derived for an assumed set of cosmological parameters (listed at the end of Section 1), instead of being marginalized over the uncertainty of cosmological parameters. The latter operation matters for estimates of cosmological parameters, which is, however, beyond the scope of the present paper.

How can one reconcile the observed value of the baryon fraction in clusters with the larger value derived from WMAP?

We explore a few possibilities in turn:

First, might a large bias on $f_{\text{stars}}$ be present? It is hard to accommodate, because in order to boost the stellar mass fraction one needs the following:

(a) that $L_{\text{tot}}$ is largely underestimated. This is only possible below the observed range of galaxy luminosities (we reach $-19.3 < M_\odot < -15.7$ magn. depending on redshift) and requires that the luminosity function keeps a diverging slope (i.e. $\alpha \lesssim -2$) for a large magnitude range below the one considered in this work. However, clusters with very deep observations do not display such a feature, down to...
assumes a non-universality of the baryon fraction. In such a case, a WMAP-derived baryon fraction might require a new derivation, under this less restrictive hypothesis.

Finally, McCarthy, Bower & Balogh (2007) suggested that the problem may be lying in an underestimation of the denominator of the WMAP baryon fraction, i.e. in $\Omega_b$.

Although we have not solved the baryon discrepancy, we can rule out almost for sure that the stellar fraction is responsible for the difference between cluster and global baryon fraction and we identify possible points that require investigation.

4.7 Comparison with previous works

Our results are in qualitative agreement with previous results (Gonzalez et al. 2007; Giodini et al. 2009), displaying an offset between the measured total baryon fraction and the WMAP value, and a decreasing stellar mass fraction with increasing mass. Some specific results might instead differ from some published results; for example, we do not confirm the claim of Giodini et al. (2009) that the baryonic fraction increases with mass. However, our statements are fundamentally different from those published in other works.

We have already discussed, in Section 3.5, the advantages of an accurate analysis of the data, of studying a sample of truly existing clusters located in a narrow range of redshift and having individually measured, and large, reference radii. We continue on the same line by noting that the cluster mass enters in the stellar mass fraction (it is at the denominator of the fraction), and thus is certainly an advantage to studying clusters with known and precisely measured masses, instead of those with noisy or unknown masses. Our sample has accurate cluster masses derived, under a parsimonious hypothesis that does not require the cluster to be in dynamical equilibrium but hydrostatic equilibrium, from the caustic analysis of Rines & Diaferio (2006) of about 208 galaxy members per cluster, on average. Instead, Gonzalez et al. (2007) masses are derived from velocity dispersion computed on small samples and with Beers, Flynn & Gebhardt (1990) estimators. These velocity dispersions (and masses) have low reliability (Arendt et al. 2008a; Andreon 2009; Gal et al. 2008). Giodini et al. (2009) assume that mass is proportional to a poorly estimated X-ray luminosity without any scatter; when instead the two quantities display a large scatter (e.g. Stanek et al. 2006; Vikhlinin et al. 2009; Andreon & Hurn 2010), it is just enough to remember the existence of cool-core clusters.

A second key difference between our and others’ works lies in performing an analysis that does not contradict the expected and observed spread in cluster properties at a given mass. Galaxy groups and clusters are the result of the assembly history of dark matter haloes, and also shaped by star formation processes affecting the gas. These physical processes (and possibly others) lead to multivariate outcomes and produce an intrinsic spread in the distribution of the observed properties of groups and clusters, a spread that is readily apparent in any stellar or gas mass fraction versus cluster mass plot, such as our Fig. 7 or Fig. 8. The spread manifests itself also as a variance of concentrations (and thus $r_{200}$) at a given cluster mass. Therefore, it is of paramount importance to account for the variance of cluster properties at a given cluster mass. Previous analyses failed to account for the above, with all of them assuming instead that clusters are identically equal at a fixed mass (or mass proxy). For example, Giodini et al. (2009) assume that all clusters of a given X-ray luminosity have the same size. Our analysis allows a variance in the cluster properties at a given halo mass. Finally, we have already noted that our analysis avoids the use of fitting methods in conditions where they must not be used.
In spite of our accounting for a larger number of error terms, we are able to reject the WMAP value at ‘much more sigmas’ than previous works, 6 versus 3.2 (Gonzalez et al. 2007) or ~5 (Giodini et al. 2009). This is the result of a different choice of the data and cluster sample: we choose clusters with accurate masses, good photometry and low galaxy background contribution, i.e. nearby clusters with caustic masses.

5 SUMMARY

We analysed a sample of 52 clusters with precise and hypothesisparsimonious measurements of mass, derived from caustics based on about 208 member velocities per cluster on average, and with measured $r_{200}$ values. We found that low-mass clusters and groups are not simple scaled-down versions of their massive cousins in terms of stellar content: lighter clusters have more stars per unit cluster mass. The same analysis also shows that the stellar content of clusters displays an intrinsic scatter at a given cluster mass, i.e. clusters are not similar to each other in the amount of stars they contain, not even at a fixed cluster mass. The amplitude of the spread in stellar mass, at a fixed cluster mass, is 0.15 ± 0.02 dex. The stellar mass fraction depends on halo mass with (logarithmic) slope = 0.55 ± 0.08. These results are confirmed by adopting masses derived from velocity dispersion.

The intrinsic scatter at a fixed cluster mass that we determine for gas mass fractions taken from literature is smaller, 0.06 ± 0.01 dex. The intrinsic spread is not restricted to low-mass systems only, but extends to massive systems. Since the studied systems look relaxed in X-ray images, the observed spread is not due to the presence in the sample of clusters manifestly out of equilibrium (e.g. merging). The non-zero intrinsic scatter of the gas mass fraction decreases the efficiency of $f_{\text{gas}}$ for cosmological studies, and requires investigation of whether the studied samples are representative, in terms of $f_{\text{gas}}$, of the population of clusters in the Universe.

The intrinsic scatter in both the stellar and gas mass fraction is a distinctive signature that, when taken individually, the regions in which clusters and groups collected matter are not yet representative, in terms of stellar and gas content and therefore in the baryon content, of the mean matter content of the Universe.

The observed stellar mass fraction values are in marked disagreement with gasdynamics simulations with cooling and star formation of clusters and groups. Instead, the amplitude and cluster mass dependency of the observed stellar mass fraction are those that do not need any AGN feedback to describe X-ray scale relations and gas and stellar mass fractions in simple semi-analytic cluster models.

By adding the stellar and gas masses, or, more precisely speaking, by fitting both of them and accounting for the intrinsic variance of both quantities, we found that the baryon fraction is fairly constant for clusters and groups with $13.7 < \log M_{200} < 15.0 \, M_\odot$ and it is offset from the WMAP-derived value by about $6\sigma$. The offset is unlikely to be due to an underestimate of the stellar mass fraction and could be related to the possible non-universality of the baryon fraction, pointed out by our measurements of the intrinsic scatter.

Our analysis is the first that does not assume that clusters are identically equal at a given halo mass and it is also more accurate in many aspects than previous works. The data and code used for the stochastic computation are distributed with the paper.

ACKNOWLEDGMENTS

We thank Andrey Kravtsov and Paul Bode for giving us their theoretical predictions in electronic format. The author greatly benefited from comments on this draft by Stefano Ettori, Fabio Gastaldello, Stefania Giodini, Anthony Gonzalez, Paolo Tozzi and the referee. For the standard SDSS and NED acknowledgements, see http://www.sdss.org/dr6/coverage/credits.html and http://nedwww.ipac.caltech.edu/.

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S. Andreon


APPENDIX A: MODEL LISTING AND CODING

In this section we give the listing of the full model, and its coding in *JAGS*.

Observed values of halo and stellar mass (\(obslgM200\) and \(obslgM_{\star}\), respectively) have a Gaussian likelihood:

\[
\text{obslgM}_{200} \sim \mathcal{N}(\lg M_{200}, \text{errlgM}_{200}^2). \tag{A1}
\]

\[
\text{obslgM}_{\star,i} \sim \mathcal{N}(\lg M_{\star,i}, \text{errlgM}_{\star,i}^2). \tag{A2}
\]

The tilde sign denotes ‘is drawn from’, and the symbol \(\mathcal{N}(y, \sigma^2)\) denotes a Gaussian centred on \(y\) with variance \(\sigma\).

True values of stellar and halo mass are linearly related (on a log scale), with an intrinsic scatter \(\sigma_{\text{scat}}\):

\[
z_i = \alpha + 12.5 + \beta \ (\lg M_{200} - 14.5), \tag{A3}
\]

\[
\lg M_{\star,i} \sim \mathcal{N}(z_i, \sigma_{\text{scat}}^2). \tag{A4}
\]

Masses are centred, purely for computational advantages in the MCMC algorithm used to fit the model (it speeds up convergence, improves chain mixing, etc.). Please note that the relation is between true values, not between observed values, which may be biased.

Uniform priors are taken: the halo mass, \(\text{obslgM}_{200}\), has a strictly uniform prior; the intercept, \(\alpha\) has a zero-mean Gaussian with very large variance; the slope, \(\beta\), has a uniform prior on the angle (which becomes a Student’s \(t\) distribution for the angular coefficient), because we do not want the cluster properties to depend on astronomer rules to measure angles (see Andreon 2006 and Andreon & Hurn 2010 for a discussion); \(1/\sigma_{\text{scat}}^2\) has a Gamma distribution with small values for its parameters, as in Andreon & Hurn (2010). This has the welcome property that the intrinsic scatter variable is positively defined, as the intrinsic scatter is. In symbols:

\[
\lg M_{200} \sim U(0, 500), \tag{A5}
\]

\[
\alpha \sim \mathcal{N}(0, 10^4), \tag{A6}
\]

\[
\beta \sim t_1, \tag{A7}
\]

\[
1/\sigma_{\text{scat}}^2 \sim \Gamma(10^{-5}, 10^{-5}). \tag{A8}
\]

Our model makes weaker assumptions than other models adopted in previous analyses, and plainly states what is actually also assumed by other models (e.g. the conditional independence and the Gaussian nature of the likelihood), also removing approximations adopted in other approaches.

For the stochastic computation and for building the statistical model, we use Just Another Gibb Sampler (*JAGS*; Plummer 2008). *JAGS*, following *BUGS* (Spiegelhalter et al. 1996), uses precisions, \(\tau = 1/\sigma^2\), in place of variances \(\sigma^2\). The arrow symbol reads ‘take the value of’. Normal, \(t\) and Gauss distributions are indicated by \(\text{dnorm}(), \text{dt}(), \text{dgamma}()\), respectively.

```
model
{
    for (i in 1:length(obslgMstar))
    {
        obslgM200[i] ~ dnorm(lgM200[i], tau.lgM200[i])
        lgM200[i] ~ dunif(0,500)
        obslgMstar[i] ~ dnorm(lgMstar[i], tau.lgMstar[i])
        z[i] <- alpha + 12.5 + beta*(lgM200[i] - 14.5)
        lgMstar[i] ~ dnorm(z[i], prec.intrscat)
    }
    intrscat <- 1/sqrt(prec.intrscat)
    prec.intrscat ~ dgamma(1.0E-5,1.0E-5)
    alpha ~ dnorm(0.0,1.0E-4)
    beta ~ dt(0,1,1)
}
```

The code above, which is an almost literal translation of equations (A1)–(A8), is only about 10 lines long in total, about 2 orders of magnitude shorter than any previous implementation of a regression model (e.g. Akritas & Bershady 1996; Andreon 2006; Kelly 2007). The model is quite general, and applies to every quantity linearly related, with Gaussian errors, and with an intrinsic scatter. For example, in this paper the same model (and program) has been used for the \(f_{\text{gas}}\) versus mass and \(f_{\text{gas}}\) versus temperature scalings. The same fitting model can be used for, say, the \(L_{\nu},\sigma_{\nu}\), richness–mass and halo occupation number versus mass scalings.

2 http://sourceforge.net/projects/mcmc-jags/

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