A New Model for Investigating the Evolution of Transcription Control Networks

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Abstract Biological systems show unbounded capacity for complex behaviors and responses to their environments. This principally arises from their genetic networks. The processes governing transcription, translation, and gene regulation are well understood, as are the mechanisms of network evolution, such as gene duplication and horizontal gene transfer. However, the evolved networks arising from these simple processes are much more difficult to understand, and it is difficult to perform experiments on the evolution of these networks in living organisms because of the timescales involved. We propose a new framework for modeling and investigating the evolution of transcription networks in realistic, varied environments. The model we introduce contains novel, important, and lifelike features that allow the evolution of arbitrarily complex transcription networks. Molecular interactions are not specified; instead they are determined dynamically based on shape, allowing protein function to freely evolve. Transcriptional logic provides a flexible mechanism for defining genetic regulatory activity. Simulations demonstrate a realistic life cycle as an emergent property, and that even in simple environments lifelike and complex regulation mechanisms are evolved, including stable proteins, unstable mRNA, and repressor activity. This study also highlights the importance of using in silico genetics techniques to investigate evolved model robustness.

Keywords

Transcription network, artificial evolution, in silico genetics, stochastic simulation, systems biology

I Introduction

Transcription regulatory networks provide essential and complex functionality for any cell. Understanding the mechanisms behind the interactions forming these networks, their behavior, and also their evolution and development, is essential for increasing our knowledge of this core process of life. However, as it has taken many millions of years of evolution for this complexity to arise, laboratory experiments in evolving transcription networks can only provide a fraction of this time frame. In this study, we introduce a new in silico model including several novel features for investigating the function, behavior, and evolution of transcription networks.

The availability of large-scale computational power has allowed the development of realistic in silico and quantitative modeling of many biological systems [49]. While long-term laboratory-based

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evolutionary experiments are possible [27, 52], computational methods allow the simulation of much longer periods of evolution in a practical timescale. This is because the life span of a simulated individual can take a fraction of the time of its real-life equivalent. Computational models allow selection of mutants and phenotypes at a much more specific level than laboratory experiments, as much more detail about specific pathways, interactions, genotypes, and behaviors can be more easily obtained. Indeed, the use of *in silico genetics* provides more than just a way of selecting or viewing molecules and organisms; it provides a new and powerful tool for investigating a model molecular system—allowing knockouts to be instantly generated, accurate and specific mutations to be applied to any molecule, and any kinetic rate to be modified.

Many models and methods have been developed to approach the question of transcription network evolution. Such models include the artificial genome (AG) [53], artificial regulatory network (ARN) [39], the contributions by François and Hakim [23] evolving networks with specific functions such as bistability or oscillatory dynamics, and those by Deckard and Sauro [19] evolving networks to perform specific computational functions, such as square-root and cube-root calculators. Also, a comprehensive review of early gene regulatory systems modeling is given by de Jong [18]. While these studies use the biological regulatory network paradigm, the models are often taken out of biological context. Alternatively, many other studies investigate networks to perform specific functions, typically logic functions analogous to electrical circuits. For example, many studies of transcription network models investigate global properties of the networks, such as whether the network is distributed as a power law, or is of a scale-free topology [1, 3, 7]. These studies are very valuable, as biological transcription regulatory networks share many attributes with the designed electrical circuits we use day to day, and indeed, analysis of the motifs within sequenced organisms (most notably *Escherichia coli* and *Saccharomyces cerevisiae*) show many similarities to traditional electrical components, such as the feed-forward loop motif, which can function as a low-pass filter [6, 42, 44].

Moreover, these previous studies treat the evolving transcription regulatory network as a standalone entity, whereas in reality the transcription regulatory network is just one of many systems interacting together within a biological cell. Also, the fitness functions used to evaluate the performance of the evolving networks are typically nonbiological, in that they have only a single, artificial goal, such as to produce a desired output from a given input. Indeed it has been suggested that this single, focused goal approach to evolving such networks produces non-modularity, which is in contrast to the highly modular structure we see in real transcription networks [34].

Another approach to modeling evolution of cells often used within the ALife literature is *individual-based models* (IbMs). In the IbM approach, each model is treated as an *individual*, or *agent*, with its own set of specific components. These individuals then compete within an environment for resources, much like any biological organism. The most biologically focused IbM to date is the COSMIC model [50], which aims to evolve bacterial function from the genetic level (transcription networks) up to the environment level (population dynamics). Other IbM approaches include the artificial chemistry model [29] and Avida [48].

The model presented in this study aims to more accurately model not only a transcription regulatory network and its processes and components (biological approach), but also the encapsulating cell and associated functions and systems within it (systems biology and ALife approaches). The sole objective of this cell is that of all organisms: to survive in its environment and propagate. While this single-objective approach may seem to contrast with the arguments presented by Kashtan and Alon [34], the objective is in fact a complex combination of many smaller, possibly conflicting objectives. Unlike many other models presented previously, the model is simulated stochastically, as previous studies have shown the stochastic nature of intrinsic and extrinsic noise found within any biological system [33, 43].

The model also introduces a method for incorporating *transcriptional logic*, which enables complex Boolean logic to be performed at the transcriptional regulation level and allows phenomena such as cooperativity between transcription factors similar to that found in biological cells.

In addition to this, the model also introduces a new method for determining molecule interaction strengths through binding affinities that are based on molecular *shape*. The introduction of such a

method means that proteins are not assigned a designated function, except in the case of the specialized function of RNA polymerase. This allows proteins to evolve their own functions, as, for instance, transcription factors, enzymes in metabolism, signaling, or indeed a combination of these functions.

This study presents the new model and methods in depth, along with results of comprehensive analysis of the model over parameter ranges and the behaviors observed. An introduction to the evolution methodology is also presented, supported by an analysis of the resultant evolution in an idealistic environment.

The study highlights the power and importance of using in silico genetics tools to investigate models and analyze their behavior, and we make hypotheses about the model's behavior in more complex environments.

2 Processes of Biological Cells

Biological cells have many interacting processes governing cell growth and division, metabolism of food releasing energy, transcription of genes, and translation of the resultant product into protein. The interaction between these processes and the cell's environment produce the complex behaviors we observe. One process in particular, transcription regulation, has an enormous influence on a cell's ability to respond to changes in environment, including food availability and starvation, or shock such as heat or acid, by the use of positive and negative feedback.

2.1 Transcription and Translation

Transcription and translation are the two main processes involved in the production of protein from a gene. Transcription involves a protein, known as RNA polymerase (RNAP), binding to the DNA at a specific place, known as a promoter site. Once the RNAP has bound to the promoter site for a gene, transcription initiates, causing the DNA helix to unwind immediately in front of the RNAP. The RNAP molecule then, using one of the strands of DNA as a template, produces a molecule of messenger RNA (mRNA). This mRNA transcript is then translated into one or more identical proteins by ribosomes. We have based our model on the simple processes involved in prokaryotic transcription and translation, and have not included more complicated processes found in eukaryotes, such as splicing.

2.2 Transcription Regulation

As transcription and translation require energy, it is favorable to only use these processes when necessary. Some gene products are required under many or all conditions, and so their production may be less strongly regulated. However, other products may only be required in specific conditions, such as shock, meaning that much stronger and complex regulation is required. Transcription can be regulated in a number of ways, one of which is via transcription factors (TFs). A gene may need to be turned on (activated) or turned off (repressed) by one or more TFs to affect when it is transcribed. TFs bind to specific sequences on the DNA, which act as regulatory sites for the associated genes, either helping the RNAP to bind to the promoter site in the case of activator TFs, or blocking the promoter site, preventing RNAP binding.

Networks of transcription regulation for responding to the environment can be both simple and complex. Many of the particularly well-studied networks, at both biological and theoretical levels, are in the model bacterium *Escherichia coli*. These include the *lac* operon, which enables response to glucose or lactose in the environment [32, 65], the tryptophan operon, which controls production of the amino acid tryptophan using a repressor [2, 56], and the heat shock system [22, 40].

3 Models and Methods

The model we present in this study is a novel transcription regulation network and cellular model for evolving bacteria within a range of environments. Like other models such as COSMIC, AG, and

ARN, our model can be viewed on a number of different levels: (i) molecular, (ii) interaction networks, and (iii) cellular and population.

Each level provides different challenges that must be met through evolution and natural selection.

3.1 Molecular Level

At the lowest level, the model consists purely of molecules. Molecules can be divided into two types: *mobile molecules*, such as proteins, which can move freely within the cell cytoplasm, and *DNA-based molecules*, which are portions of the DNA that perform specific functions, such as gene regulation.

3.1.1 Mobile Molecules

In a single cell there are thousands of different types of molecules, ranging from individual ions to sugars to larger macromolecules such as proteins [2]. Our model substantially reduces the types of molecules into five broad classes:

- Protein. Proteins are the workhorses of the model, as they can potentially perform a
 number of functions: as transcription factors, as metabolic enzymes, or for signaling.
 Proteins are not assigned any function; instead, their binding affinity with other molecules
 determines their functions.
- 2. RNA polymerase. This is a protein that performs the specific function of initiating transcription when bound to a gene promoter site, and transcribes the gene, forming a molecule of messenger RNA. The level of RNA polymerase is determined at the start of simulation, and no more of it can be created, nor can any be degraded (it is assumed that this intrinsic machinery would be managed elsewhere by the model). This is the only protein with a prespecified function.
- 3. mRNA. Messenger RNA molecules act as templates for proteins.
- 4. Energy. Energy is the global term used for any molecule that is used up to perform or fuel a function (such as in transcription or translation) and is thus analogous to ATP. Energy is used to determine cell states. The model has the capacity to include further types of energy that could be used in specific reactions.
- 5. *Food.* Food provides energy to the model cell. Food molecules are broken down by a protein binding to them. Each food type has a number of parameters:
 - (a) Time to be broken down
 - (b) Molecule type yielded (either a different type of food, or energy)
 - (c) Amount of molecules yielded.

While the model abstracts an actual cell considerably, it still has an enormous and varying amount of complexity. For instance, a pathway such as the glycolytic cycle could be modeled completely, introducing numerous types of food, as each individual metabolite is included, also requiring many different protein enzymes; alternatively, a single food type could represent the entire pathway.

3.1.2 DNA-Based Molecules

In prokaryotic cells, the DNA typically has the following four types of region: *encoding genes*, which contain the genetic information used to produce mRNA molecules, *cis-activating elements* and *cis-repressing elements*, which when occupied by a transcription factor upregulate or downregulate transcription of

its associated gene, and *promoter elements*, which are used by RNAP molecules as an indicator for the beginning of an encoding gene, which can then be transcribed. Our model implements these types of regions by assigning a *regulatory region* consisting of a number of cis-activating, cis-repressing, and promoter elements to an encoding gene; and also associated with the gene are an mRNA and a protein. The encoding gene itself does not have a representation other than the transcribed product.

3.2 Molecule Shape and Binding Domains

Each molecule within the model has a specific shape, which is used to determine its binding affinity with other molecules. Molecule shape is represented by a number of binding domains, or sites; therefore, the number of binding sites a molecule has determines the number of molecules to which it can bind at any time, and also determines dynamically what functions it can perform. The shape of real molecules depends on their atomic and charge configuration, which would require a very high-dimensional space to be accurately represented. In our model, we represent the shape of a binding domain with just two dimensions, so that the shape is modeled by a point on the surface of a unit sphere. The two spherical polar coordinates (θ, ϕ) corresponding to the point on the sphere are the genetic information of the binding domain, and thus are free to mutate. The polar coordinates, transformed into the Cartesian coordinate system (x, y, z), are then used in the function to determine the binding affinity with another shape, and thus the corresponding phenotype.

3.2.1 Binding Affinity

The binding affinity between two binding sites is a function of the Euclidean distance between one site and the antipode of the other site (denoted as Δ). In this way the strongest binding would be from two complementary, opposite shapes. Because association is diffusion limited, different binding strengths are implemented as dissociation rates, which are given by

$$K_{\rm off} = \frac{\sigma \Delta}{1 - (\Delta/2r)^{\alpha}} \tag{1}$$

where σ is a scaling factor, r is the radius of the sphere (in this case 1), and α is a Hill-like coefficient for modifying the affinity curve saturation.

This binding affinity function is used to calculate the stability of all complexes. An exception to this is the RNAP-promoter complex. For that, our current model implementation uses a fixed complex dissociation rate that is dependent only on the occupancy of the associated activator and repressor sites, and not on the shape of the promoter or RNAP molecule. This is to ensure that regardless of mutation to the promoter site, the RNAP is still able to function.

3.2.2 Allosteric Effects

In the cases where a molecule has multiple binding domains, it is possible for it to be bound to several other molecules simultaneously. The occupation of a binding domain has been shown to be able to cause conformational changes to other domains of the molecule [2]. Our model introduces such a concept, so that each binding domain has two shapes: the *natural shape* in which the domain exists when the parent molecule is a monomer, and the *allosteric shape* in which the domain exists when it and another domain of the parent molecule are part of a larger, multi-molecule complex.

3.3 Molecule Interaction

The molecules are assumed to exist in a well-stirred system. This means that all molecules will have the same interaction rate. The diffusion-limited interaction rate of mobile-mobile molecule

interactions is slower than that of DNA-mobile molecule interactions [16, 36], and so interactions between two molecules depends on their molecular type.

3.4 Polymerization

Polymerization between molecules to form large complexes is an integral component of many cellular processes, such as in signaling networks, increasing molecular stability, or the formation of physical structures in a cell, such as the actin cytoskeleton or a flagellum. Our model allows polymer chains to form and break dynamically. This allows signaling mechanisms and transfer of information, and prevents protein and mRNA molecules from being degraded. Due to computational constraints, complexes are only permitted to consist of up to three molecules. Because we do not model physical structures, this constraint does not weaken the model.

3.5 Metabolism

Metabolism is a core function of any cell. Metabolic pathways within the model are any reactions involving a food molecule and any protein. Pathways can be implemented with various levels of realism. For instance, glycolysis could be included in a model by adding each metabolite from the cycle, each with its own catabolism time and product, or a single food could be used to represent the entire pathway.

3.6 Degradation

Molecule degradation can occur actively or passively. Active degradation involves another molecule binding to the molecule and changing its structure, causing it to degrade, whereas passive degradation does not require any interaction from other molecules, a single molecule breaking down either spontaneously or due to environmental conditions. The model currently only implements passive degradation, and so molecules will break down spontaneously according to a *stability* parameter, or rate. Only those that are produced by genes within the cell (i.e., generic proteins and mRNAs) degrade; other molecules are treated as stable.

3.7 Transcription and Translation

Transcription and translation are two of the fundamental processes represented within the model. Transcription initiation occurs after a promoter site has been bound by an RNA polymerase for a given period of time. Once transcription initiation has occurred, and the cell has enough free energy, the polymerase transcribes the gene in a single reaction. Each gene will have a specific length of nucleotides, which is used, together with a rate of elongation, to generate the reaction rates for transcribing a gene. The following equation shows the generic transcription reactions within the model:

RNAP + promoter
$$\rightleftharpoons$$
 RNAP_promoter + energy
$$\rightarrow \text{promoter} + \text{RNAP_transcribing}$$

$$\rightarrow \text{RNAP} + \text{mRNA}$$
(2)

Translation is modeled in a similar way to transcription, in that the process is reduced to a single reaction. If the cell has enough free energy, translation of an mRNA molecule can occur. Each mRNA molecule will have a length that is once again used, together with the abundance of ribosomes, to generate a reaction time for the translation process. The following equation shows the generic translation reactions within the model:

$$mRNA + energy \rightarrow mRNA + translating_mRNA \rightarrow protein$$
 (3)

Table I. Expression states and descriptions.

0	Repressed	No possible expression
1	Unactivated	Basal or leaky expression
2	Activated	Full possible expression

3.7.1 Transcription Regulation

Regulation of transcription is performed by transcription factors binding to the cis-activator, cisrepressor, or promoter sites in the regulatory region of a gene. The effect of an activated regulatory region is that the promoter site and RNA polymerase molecule will bind more strongly, increasing the chance of transcription initiation. Conversely, the effect of a repressed regulatory region is that binding is prevented between the promoter site and RNA polymerase, turning off any transcription.

To determine the state of a regulatory region (activated, repressed, or neutral) we employ a novel method that we term *transcription logic*. Transcription logic consists of a Boolean logic table and a corresponding function called the *expression state*. A column, or Boolean variable, is added to the logic table for each cis-activator and cis-repressor element in the regulatory region. All possible Boolean combinations of these variables are then generated in the table. For each row in the table an *expression level* is given as shown in Table 1 to reflect whether transcription is possible and how likely it is to initiate.

Using this method, any possible function can be applied to the regulatory region, giving the model its complexity and flexibility. For instance, to simulate the expression of the *lac* operon, the regulatory region would consist of a single cis-activator, a single cis-repressor, and a single promoter site. The transcription logic function for the *lac* operon is given in Table 2.

3.8 Model Simulation

The model is simulated using a modified Gibson-Bruck stochastic algorithm [24] (code available on request). Therefore, on using a stochastic framework, time is continuous, molecule abundances are discrete values rather than concentrations, and intrinsic noise is introduced. Due to the incorporation of realistic reaction rates for transcription, translation, and molecular interactions, accurate timescales for these processes are produced, providing a realistic timescale for model output.

Modifications to the algorithm include *static reactions*, which are non-Markov, fixed-time reactions that allow species abundances or reaction rates to be changed, for example due to environmental changes. Also, logic-based termination criteria have been introduced for ending each model simulation.

Models are simulated until one of the following termination criteria is met:

• The model has reached the appropriate replication threshold of free energy:

(base replication threshold) + (genome size) × (additional energy per gene)

Table 2. Example of transcription logic for lac regulation, where + is bound and - is unbound.

Activator	Repressor	Expression state
_	_	I
_	+	0
+	-	2
+	+	0

- The model has reached a maximum simulation time threshold (simulation wall time).
- The model does not have enough free energy to produce either an mRNA or a protein, and no protein or mRNA exists; then the model is classed as dead.

3.9 Model Parameters

The model consists of a number of free parameters, which are able to evolve, and fixed parameters. Free parameters include all molecule and DNA element shape parameters (θ, ϕ) , with the exception of energy, food, and RNAP, which are fixed during evolution. Protein and mRNA degradation rates are also free to evolve. The fixed parameters, such as transcription and translation rates, food uptake and metabolism rates, and diffusion-limited molecule interaction rates, are all derived where possible from *Escherichia coli* experiments. In the simulations we present, all proteins have two domains (with allosteric effects) with a simplified metabolism of a single food molecule that is broken down to yield energy. The fixed parameters used in the model are given in Table 3.

3.10 Evolutionary Framework

The evolutionary framework used in this work is based on a standard genetic algorithm, in which a population size is fixed, and random models are initialized to fill this population. Each model in the initial population is then simulated sequentially. Upon termination of the simulation, the simulated time and energy level are recorded. As the fitness function for the model is the time taken for replication, models with a small fitness value (quicker replication) are therefore fitter than models with a larger fitness (slower replication). Model fitness is determined as follows:

- If the model reached the replication threshold before the simulation time was exceeded, then the fitness is the simulated time for the model to replicate.
- If the model did not replicate, but still had some free energy, then the fitness is

max simulation time × (max simulation time/final energy level)

Using this fitness function, models that were terminated with higher levels of energy will be treated more favorably than those with lower levels.

• If the model died, then its fitness is infinity.

Once the initial population has been created and initially simulated, the evolution process begins. The use of a fixed-size population structure provides a source of competition between organisms. Each model in the population (regardless of its previous simulation) replicates to produce an identical model. If the cell survived (replicated or hit the simulated time threshold), then the mobile molecules within the parent cell (proteins, mRNAs, and food), excluding RNA polymerase, are randomly divided between the two cells using a random normal ($\mu = 0.5$, $\sigma = 0.1$) for each molecular species. Dead models receive no molecules. Evolutionary operators are then applied to each model in turn, and each copy of the model is simulated. Once again the simulated time and energy are recorded. The population must then be reduced to its original size using an elitism strategy: models are selected (without replacement) according to their fitness. In this, and subsequent generations, models that did not replicate but did not die are allowed to be selected; if not enough surviving models exist, new random models are introduced. The resulting new population is then carried forward to the next generation, where the process starts again. Each parameter setting is run three times.

The structural parameters for the evolutions (the binding affinity parameters α and σ) were determined from analysis of simulation results over a wide range of parameters. This analysis can be found in Appendix 2.

Table 3. Parameters that are fixed during evolution in the current model implementation.

Parameter	Value(s)	Notes
Food species	I	Represents glucose (I food molecule ≈ I4 glucose)
Initial genome size (number of genes)	1	
Mobile-mobile molecule interaction rate	10 ⁻⁴ s ⁻¹	[41, 16]
DNA-mobile molecule interaction rate	10 ⁻² s ⁻¹	[36]
Regulatory region	Lac operon regulation	
RNA polymerase per gene	3	Each cell has ~2000 active RNAP [26] and up to 700 operons [55]
Gene length	1,080 nt	E. coli K-12 genome length 4,639,221 bp with 4,289 genes [14]
Transcription rate	50 nt/s	[4, 12]
Transcription cost	8 energy molecules	~2000 ATP to transcribe 1,080 nucleotides [47]
Transcription initiation rate	I s ⁻¹	
Activated RNAP-promoter complex off rate	0.1 s ⁻¹	Gives 90% chance of transcription starting
Unactivated RNAP-promoter complex off rate	l s ⁻¹	Gives 50% chance of transcription starting
Protein size	360 aa	Each amino acid is three nucleotides
Translation rate	15 aa/s	[65, 2]
Translation cost	6 energy molecules	~1,500 ATP to translate 360 aa [47]
Ribosome abundance	4.5 ribosomes/mRNA	18,000 ribosomes per cell; up to 4,000 mRNA molecules per cell [12]
Food uptake rate	1.5 s ⁻¹	Loosely calculated from actual glucose uptake rates
Food metabolism rate	3.5 s ⁻¹ per enzyme	Loosely calculated from glycolytic cycle rates
Energy released from metabolism	2 molecules	Glycolysis yields 36 ATP molecules (1 energy molecule = 252 ATP)
Initial energy amount (and after replication)	100	
Initial protein amount	10	

Table 3. (continued)

Parameter	Value(s)	Notes
Initial food amount	10	
Replication base energy threshold	1,000	
Additional energy per gene	100	
Population size	100	
Number of generations	50	
Maximum simulation time	l h	
Mutation rate $P(m)$	0.1, 0.3, 0.5	Varied rates used for sensitivity analysis
Gene duplication rate $P(d)$	0.1, 0.3, 0.5	Varied rates used for sensitivity analysis
Gene loss rate P(I)	0.1, 0.3, 0.5	Varied rates used for sensitivity analysis
Binding affinity $\boldsymbol{\sigma}$	1, 10, 20, 30, 40, 50	Approximate range determined from model dynamics analysis
Binding affinity $\boldsymbol{\alpha}$	1	Fixed value determined from model dynamics analysis
Mutation shape, random normal, std. dev.	0.2	
Initial protein degradation rate	10 ^{random} normal (-2.5,0.5)	Average time 612 s
Initial mRNA degradation rate	10 ^{random normal (-2.5,0.1)}	Average time 324 s
Mutation protein degradation rate, std. dev.	0.2	
Mutation mRNA degradation rate, std. dev.	0.05	

3.11 Evolutionary Operators

The evolution framework currently supports three evolutionary operators, *gene duplication*, *gene loss*, and *mutation*. These operators are applied to each parameter within each gene with a given probability. The evolutionary results presented in the results section are obtained using low gene duplication, gene loss, and mutation rates (P(d) = P(l) = P(m) = 0.1).

3.11.1 Gene Duplication

Gene duplication has been shown to have had a significant influence on the evolution of genomes [60, 30], and has been used in previous models such as ARN [5, 39] and the mathematical model by Wagner [63]. Therefore, it is important for this process to be included within our model. However, in view of real evolutionary timescales and the timescale that can be feasibly simulated computationally, the duplication and loss events are simulated at a much higher rate than has been estimated over the course of millions of years of evolution.

Gene duplication is implemented using the following algorithm: For each gene in the genome, the gene and its regulatory region are duplicated, with the specified probability P(d). The products of the original and duplicated gene are considered to be different molecular species.

3.11.2 Gene Loss

While the genome can increase in size using gene duplication, it can also decrease in size by gene loss. Gene loss is also an important process in the evolution of genomes, as it allows the genome to remove useless (nonfunctional) *junk* genes. This is preferable in that junk genes would still be replicated or transcribed, and so waste energy.

Gene loss is implemented using the following algorithm: For each gene in the genome (while there are still at least two genes), the gene, its mRNA and protein products, and its regulatory region are removed from the model, with the specified probability P(l).

3.11.3 Mutation

Mutation (or divergence) is the primary operator for increasing diversity within bacteria that are reproducing asexually. Any shape (including natural and allosteric forms of domains, and cis-regulatory DNA elements) or degradation rate in the model is available to mutate. The mutation operator used is a random normal noise added to the shape, or a lognormal random noise to the degradation rate. More technical details of this mutation operator are described in Appendix 1.

3.12 In Silico Genetics

In silico genetics is the equivalent of performing genetic experiments in vitro, except the cells are simulated on a computer. To allow similar experiments to be performed on our model, a custom in silico genetics tool was developed, allowing modification of any free or fixed parameter within the cell. This enables mutant cell lines to be created, with changes such as gene or regulatory site knockout, novel genes, increased or decreased molecule stability, or change in molecular shape. Using this technique, it is possible to examine the effects of perturbations in a cell, similarly to the techniques used in the laboratory.

4 Results and Discussion

4.1 Model Dynamics

Models consisting of a single gene exhibited four different classes of behaviors, as seen in Figure 1. The first behavior is growth (Figure 1a), where the energy gradually increases up to the replication threshold; this behavior may indicate a linear cell volume increase, which is consistent with observed volume growth in E. ali [38]. The second behavior is death (Figure 1b), where the energy hits 0 (or some other death criterion level), due to over expression of the genes and unsustainable usage of energy. These two behaviors are *primary* behaviors, of which only one is observed over the course of a simulation (the cell either replicates or dies). The second set of behaviors are secondary, in that there can be many instances of them observed throughout the simulation. Peaking behavior can be seen in Figure 1c. This behavior consists of a growth phase, followed immediately by a substantial decrease in energy (this can be seen from the figure at around 600 and 1050 s into the simulation). Coinciding with the drop in energy is an immediate increase in protein, indicating that the peaking of energy is due to transcription and translation. The sudden decrease in energy over a matter of minutes would be expected with the current parameters, as the approximate time to initiate transcription is 1 s, the time to transcribe the gene is 21.6 s, and a further 24 s for a fully translated protein to be produced (with 4.5 ribosomes per mRNA), meaning that in a matter of minutes multiple mRNA molecules can be produced and many more proteins can be produced from them. Plateauing behavior can be seen in Figure 1d. This behavior consists of the energy level remaining static for a period of time.

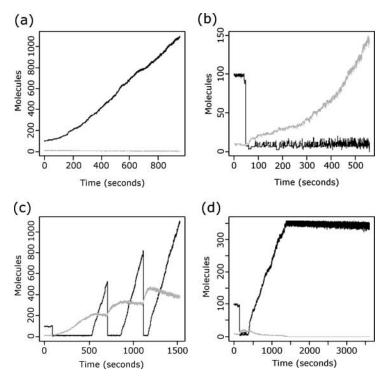


Figure I. Examples of model behaviors. All models have the same structural parameters $\sigma=1$ and $\alpha=1$, and randomly initialized evolvable parameters. (a) is an example of growth, where the protein level stays constant and the energy level rises steadily, reaching the replication threshold of 1,100 free-energy molecules in around 900 s. (b) is an example of death, where the protein level slowly increases up to around 150 molecules after 500 s, whereas the energy rapidly falls to around 20 molecules and stays close to this amount before it eventually runs out. (c) is an example of peaking, where the protein level slowly rises to around 200 molecules, before a large rapid increase in energy around 500 s; the protein level then rises again, followed by an even faster drop in energy, causing a peak in the energy. This behavior is repeated several more times before the energy threshold is reached. (d) is an example of plateauing, where, after an initial drop followed by increase in energy, the energy and protein levels appear to reach a steady state around 1500 s, causing a plateau in both protein and energy levels. Black lines plot the energy; gray lines plot the protein level.

This indicates a period of transcriptional and translational inactivity, as the figure shows there is enough energy for producing an mRNA transcript, but no transcription takes place, meaning either the gene is repressed, or the limited RNA polymerase molecules are bound to other molecules. This behavior may be observed in real cells undergoing a stress, such as heat or acid shock. The stress response often leads to large changes in gene expression, as unimportant genes are switched off and only essential response genes (such as those encoding chaperon or helper proteins) are switched on to conserve energy [47]. Laboratory evolution of *E. coli* has shown that mutations reducing the transcription of flagella synthesis genes in the stringent response regulatory network offer a significant fitness advantage [52].

The behaviors and dynamics of the model described above were investigated using random initializations with the structural parameters $\sigma=1$ and $\alpha=1$. Investigation of the sensitivity of the model to these structural parameters is detailed in Appendix 2.

4.2 Parameters Essential for Model Replication

An investigation was conducted into which evolvable parameters are most important for model replication. 1,000 models were randomly initialized and simulated in a constant-external-food environment, and the evolvable parameters were recorded. To compensate for stochasticity, each initialization was simulated 20 times, recording if the model replicated. Each model was classified

either as replicating (class 1) or not (class 0), depending on the majority results from the 20 simulations. Both univariate and multivariate methods were used to determine important parameters for replication.

4.2.1 Univariate Analysis

Logistic regression [15] with a controlled false-discovery rate [10] was used to determine the significance of each parameter as a predictor for model replication. Table 4 shows the eight significant parameters (q < 0.05). The most significant and accurate predictor for class membership was the protein degradation rate, with an accuracy of over 81%. Other significant parameters included the mRNA degradation rate and various repressor- and promoter-complex minimum dissociation rates, although their classification accuracy is only slightly higher than for classifying all models as class 0 (nonreplicating, 55.4%). These results indicate that the optimal network topology for replication in this simplistic environment would require specific interaction between various molecules and the repressor and promoter sites, and is also very sensitive to the degradation rates of gene products. The sensitivity to the protein degradation rate is likely to be due to the protein molecule's role as a metabolic enzyme. As the model can only gain energy by breaking down food molecules and only protein molecules have this functionality, the interaction of protein and food molecules is very important. The advantage of a stable protein is that there is an increased probability that the protein will interact with food molecules before it degrades, allowing more metabolic reactions to take place. Interestingly, the stability of the protein-food complex does not appear to be a significant parameter. This indicates that only the rates of food-protein bindings are important, as stochastic effects mean that sufficient numbers of weakly active proteins may be sufficient to allow replication. Stable proteins also need to be replaced less frequently than unstable proteins, requiring less transcription and translation activity and therefore saving energy.

4.2.2 Multivariate Analysis

Multivariate analysis was performed with GALGO [61], using the diagonal linear discriminant analysis (DLDA) classifier, 200 solutions, and a goal fitness of 0.85. All other options were set to default. Models consisting of two to five parameters were generated, and each model size was used

Table 4. Univariate analysis of significant evolvable parameters. For each parameter its ID number, original p-value from a logistic regression, adjusted q-value from controlling the false discovery rate, classification accuracy, sensitivity, and specificity are shown.

Parameter	ID	Þ	q	Classification accuracy (%)	Sensitivity	Specificity
Protein degradation rate	22	< 2e ⁻¹⁶	5.2e ⁻¹⁵	81.7	0.77803	0.84838
Protein-repressor complex $k_{\rm off}$	5	1.38e ⁻¹⁰	1.794e ⁻⁹	54.7	0.32287	0.77617
Protein-promoter complex $k_{\rm off}$	6	1.29e ⁻⁸	I.II8e ⁻⁷	60.4	0.34978	0.80866
All-promoter complex $k_{\rm off}$	26	1.06e ⁻⁷	6.89e ⁻⁷	57.6	0.28027	0.81408
mRNA degradation rate	23	6.05e ⁻⁷	3.146e ⁻⁶	58.1	0.32287	0.78881
Energy-promoter complex $k_{\rm off}$	14	8.1e ⁻⁵	3.5 le ⁻⁴	58.3	0.23318	0.86462
Food-repressor complex $k_{\rm off}$	10	0.00273	0.01014	55.3	0.12556	0.89711
Protein-protein complex k_{off}	8	0.00346	0.011245	56	0.12108	0.91336

five times. Multivariate solutions were able to improve the classification accuracy by more than 5% over univariate solutions. Table 5 shows the optimal solutions generated during each GALGO run on each model size, and Table 6 shows the proportion of parameters selected in the optimal solutions. A model size of 2 generates a solution that includes the two most significant parameters from the univariate analysis, which again indicates a network topology dependent on repressor interaction and protein degradation rate. This solution only improves the classification by 2% over the single most significant single parameter, therefore highlighting the major contribution this parameter makes to model replication. Increasing the model size further only yields slight improvements in classification. A five-parameter classifier achieves only 5% improvement, and a 10-parameter classifier only improves by around 0.5% on that. This result indicates that very few parameters have any significant effect on classification, though most of them were found to be significant from the univariate analysis. The parameters that appeared most frequently in the multivariate solutions were again protein and mRNA degradation rate, indicating the model's sensitivity to molecule stability and interactions with the repressor and promoter sites on the DNA.

4.3 Evolution: Constant, Single-Food Environment

4.3.1 Realistic Replication Time is an Emergent Property

The cell cycle, or time to replicate, appeared to reach a minimum of around 300 s, with typical replication times for the evolved population between 400 and 1000 s. The replication time of *E. coli* K-12 depends on the growth medium, ranging from 20 min up to an hour or more [47]. The replication time of our most efficient evolved cells ranged from around 6 to 15 min (the average time for one final generation was 11.5 min); therefore it is fair to claim realistic cell replication times as an emergent property, as our cells only model regulatory, metabolic, and signaling genes, while processes such as cell growth and DNA replication are not explicitly included in the model. Models consisting of two or more genes evolved similar cell replication times to models consisting of only a single gene, indicating that having multiple genes may not always be prohibitive of efficient replication times. Figure 2a shows an example simulation of an evolved model that replicates in 13.4 min and has a protein steady state level of around 200 molecules.

Replication times and chance of replication were also evolved to be more consistent. 1000 simulations of an evolved model and of its ancestor model and were examined. The evolved model replicated in 96.7% of the simulations, and the ancestor model achieved only 94.9% replication. 100 replication events were selected from each model for comparison, and the results are shown in Table 7. The maximum speed of replication was similar between the ancestor and evolved models; however, the mean replication time and standard deviation were reduced in the evolved model. This indicates that the model has evolved not to maximize the speed of replication, but rather to replicate as consistently as possible.

4.3.2 Evolution of Stable Proteins and Unstable mRNA

Investigating other aspects of the evolved model also shows some interesting and lifelike trends and principles. The degradation rates of mRNA and protein species within a range of models from different evolutionary environments displayed similar behavior, selecting for unstable mRNA molecules with typical mean half-life of under 3 min and stable proteins with typical mean half-life of several hours (see Table 8).

These are remarkably close to turnover rates in biological cells. The average turnover time for an mRNA molecule in *E. coli* is around 5 min [11], and protein stabilities in *E. coli* and *Saccharomyces cerevisiae*, although wide ranging, are often an order of magnitude higher than those of mRNA [9, 46, 64]. Table 8 shows the evolved changes in mean mRNA and protein turnover rates. Although the two start at similar levels, the mRNA half-life decreases from 5.53 to 2.8 min, whereas the protein half-life increases from 10.46 to around 360 min. The increased stability of the protein would allow

Table 5. Multivariate solutions generated by GALGO. For each model size and run, the best solution, and its classification accuracy (using logistic regression), sensitivity and specificity are shown. All five runs with a model size of 2 generated the same optimal solution. All optimal solutions included parameters 5 (protein-repressor complex $k_{\rm off}$) and 22 (protein degradation rate), which were also the two most significant parameters identified from the univariate analysis. All parameters in the optimal solutions, with the exception of 3 (protein-RNAP complex $k_{\rm off}$), 13 (energy-repressor complex $k_{\rm off}$), 16 (RNAP-repressor complex $k_{\rm off}$), 19 (mRNA-promoter complex $k_{\rm off}$) and 25 (all repressor complex $k_{\rm off}$), were identified as significant from the univariate analysis. The only significant univariate parameter not included in the multivariate solutions was 10 (food-repressor complex $k_{\rm off}$).

Model size	Run no.	Optimal solution	Classification accuracy (%)	Sensitivity	Specificity
2		5, 22	83.8	0.80493	0.86462
3	I	5, 14, 22	84	0.81839	0.85740
	2	5, 6, 22	85.5	0.82511	0.87906
	3	5, 22, 26	84.5	0.81839	0.86643
	4	5, 6, 22	85.5	0.82511	0.87906
	5	5, 22, 23	84.8	0.82287	0.86823
4	I	5, 6, 13, 22	86.2	0.84081	0.87906
	2	5, 22, 23, 26	86	0.84081	0.87545
	3	5, 6, 14, 22	86.3	0.83632	0.88448
	4	5, 6, 14, 22	86.3	0.83632	0.88448
	5	3, 5, 6, 22	85.1	0.82287	0.87365
5	1	5, 6, 14, 22, 23	86.8	0.85650	0.87726
	2	5, 16, 22, 23, 26	86	0.84081	0.87545
	3	5, 6, 8, 14, 22	86.3	0.83632	0.88448
	4	5, 6, 14, 19, 22	86.3	0.83632	0.88448
	5	5, 14, 22, 25, 26	84.5	0.82511	0.86101

the same protein to metabolize more food molecules, and so decrease the need for further protein production. However, the large standard deviation of the mean protein degradation rate indicates a very large variation between individual models.

We use in silico genetics to investigate the response of the model to changes in the degradation rates. Decreasing the mRNA degradation rate (mRNA stability increased to 35 min from 3.1 min)

Table 6. Evolvable parameters selected in optimal solutions generated by GALGO. For each parameter, its ID number and its percentage in solutions of different model sizes are shown. Parameter proportion in model solutions is averaged over five runs.

		Percentage in model size				
Parameter	ID	2	3	4	5	
Protein-RNAP complex k _{off}	3	0.3	2.4	11.3	4.2	
Protein-repressor complex $k_{\rm off}$	5	88.7	81.5	74.4	97.8	
Protein-promoter complex $k_{\rm off}$	6	7.5	29.4	66.1	65.4	
Protein-protein complex $k_{\rm off}$	8	0	0.1	6	6.3	
Energy-repressor complex $k_{\rm off}$	13	0	0.8	9.2	19.4	
Energy-promoter complex $k_{\rm off}$	14	0	13.6	23.3	31.8	
RNAP-repressor complex $k_{\rm off}$	16	0	0.2	3.1	7.1	
mRNA-promoter complex $k_{\rm off}$	19	0	1.6	2.8	11.8	
Protein degradation rate	22	100	100	100	100	
mRNA degradation rate	23	0.5	36.7	31.2	23.4	
All-repressor complex $k_{\rm off}$	25	0	7.1	2.7	9.6	
All-promoter complex $k_{\rm off}$	26	2.9	6.7	17.3	21.9	

has the effect of increasing steady state protein levels from around 200 molecules in the evolved model to around 850 molecules in the mutated model and increasing the replication time from 13.4 to 38 min (Figure 2c). This is because the mRNA molecules exist within the system for a longer period of time, therefore allowing more transcription. In this example the model is still capable of replication, but with a longer replication time. Increasing the protein degradation rate (protein stability is decreased to 6 min from 246.2 min) leads to a decreased protein steady state level after the initial transcription activity of around 150 molecules, which rapidly decreases, leading to an increased replication time of 18.8 min, up from 13.4 min. Figure 2d shows how the initial protein level is reached and then transcription is repressed, as expected. However, the protein level then quickly decreases, rather than staying constant. Once again, in this example the protein level was high enough to support replication, but with decreased efficiency.

The evolution of very stable protein molecules for metabolism is paralleled in real organisms. In general, however, the stability of proteins is highly dependent on their function. Signaling proteins are often very unstable, allowing rapid response to stimuli; proteins that harm the cell under stressed conditions may be unstable, or actively degraded, to deal with this. Therefore, the environmental conditions and functions required by the cell are likely to strongly influence the evolution of the stability of proteins. It is important to note that even though the protein is very stable, it is being diluted as a result of cell division, and so the cells need to replenish the protein to be able to function.

Rapid mRNA turnover has previously been suggested as a mechanism to enable rapid response to environmental changes [22]. Here, however, we find that mRNA is rapidly turned over on realistic timescales, even in an unchanging environment. Thus it would seem that this turnover is an

emergent property associated with two-step gene product synthesis that enables protein production for minimum energy cost. It is, more than anything else, an adaptation for efficiency.

4.3.3 Evolution of Basic Repressor Activity

Models evolved for effective growth in a constant food environment all developed a single-gene repressor regulatory network, where the single gene was repressed either by a product of the gene (mRNA or protein) or by energy or food molecules. This structure was seen in all model lineages.

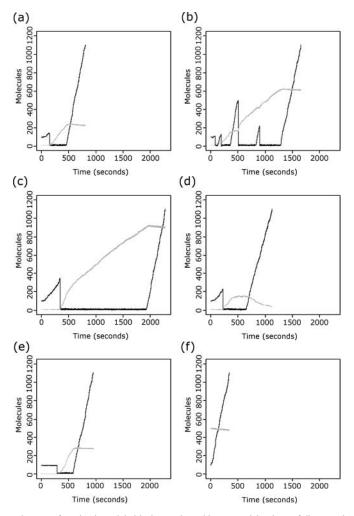


Figure 2. Example simulations of evolved model. (a) shows the *wild-type* model, where, following the usual *lag* phase of the energy level dropping to below 20 molecules due to initiation of transcription and subsequent increase in protein, the energy level rapidly increases at around 500 s, with the protein reaching a steady state of 200 molecules. The energy threshold is reached by 800 s. (b) shows the repressor knockout mutant, in which peaking has been introduced, as the protein level does not enter steady state due to the increased transcription. After several peaks, the energy threshold is reached after 1,500 s. (c) shows the increased mRNA stability mutant, in which the lag phase is significantly increased, due to increased translation. Wild-type growth occurs around 2,000 s, however, with a protein steady state of 850 molecules. (d) shows the decreased protein stability mutant, in which wild-type growth occurs after 550 s; however, a protein steady state is not reached. (e) shows the 0-protein mutant, in which the lag phase continues for around 500 s, after which transcription and translation occur, causing wild-type growth after 650 s with a protein steady state of 300 molecules. (f) shows the 500-protein mutant, in which no lag phase is evident and wild-type growth occurs immediately, the energy threshold being reached in around 500 s, with a protein steady state of 500 molecules. Black lines plot energy; gray lines plot protein level. All plots are shown on the same scale.

Table 7. Mean replication times and standard deviations and minimum replication times for 100 replication simulations of the ancestor and the evolved model.

Model	Mean replication time (min)	Minimum replication time (min)	
Ancestor	15.48	5.19	9.27
Evolved	14.14	3.73	9.38

Figure 3a shows a typical ancestor-model gene regulatory network (a connection between DNA and molecules is shown only if the K_d of the binding between them is less than 100 nM). We can see that the ancestor model already has a simple repressor system, with the protein product negatively self-regulating its own production.

Figure 3b shows an evolved model from the ancestor model in Figure 3a. Here we can see that the repressor still exists, but the network has grown to include the protein's second binding domain as a TF, with the repressor shape remaining relatively fixed during the course of the evolution. We can also see that the model has evolved to use the promoter site as a secondary repressor, with fairly large changes in the promoter site's shape. The large changes to the promoter site do not affect the RNAP binding (see Section 3.2.1). Figure 2a shows the cell initially producing protein up to a required threshold and then repressing any more production, saving energy for replication, whereas Figure 2b shows a simulation of the knockout mutant. Without repression, peaking has been introduced into the model dynamics. As shown previously, peaking is the result of mass transcriptional and translational activity. Instead of the model repressing protein production when a required level was reached, in the mutant there is no evidence of repression, and proteins are produced in several bursts of transcription and translation activity, which uses large amounts of energy. This causes the model to make several false starts before finally reaching its required energy threshold, thereby doubling the replication time from 13.4 to 27.7 min.

Therefore the optimal regulatory system for the single-constant, abundant food environment is a single-gene repressor. This allows the model to metabolize food successfully and efficiently to ensure that enough energy is saved to reach the replication threshold. This behavior is fundamentally realistic, as there are more than 2,000 known negative regulation interactions in *E. coli* [35], such as the tryptophan operon [2, 56], and many of these are autoregulated. Negative feedback performs several functions: it (i) turns off potential transcription of the gene, if not currently required (for example, for stress-response proteins), thereby saving energy, (ii) helps to maintain a specific concentration of the protein (homeostasis), (iii) increases the speed of response within a transcription network [54], and (iv) minimizes mRNA usage [58].

Other network topologies were also evolved. Figure 3c shows an evolved network where both an activator and a repressor exist. However, the transcription factors in this example are food and energy molecules, rather than gene products. Energy or food molecules binding directly to the DNA is permitted in this model, although for steric reasons it does not appear to happen in life. Real cells have evolved to use energy, food, or other types of molecules as signals in regulation by using their binding to

Table 8. Mean protein and mRNA half-lives and standard deviations for initial and evolved generations.

		Protein		mRNA			
Generation	Mean half-life (min)	Std. dev. (min)	Range (min)	Mean half-life (min)	Std. dev. (min)	Range (min)	
I	10.46	14.21	0.13-75.36	5.53	1.44	3.002 – 10.72	
50	359.59	384.14	25.5 – 1833.27	2.8	0.505	1.41 – 3.95	

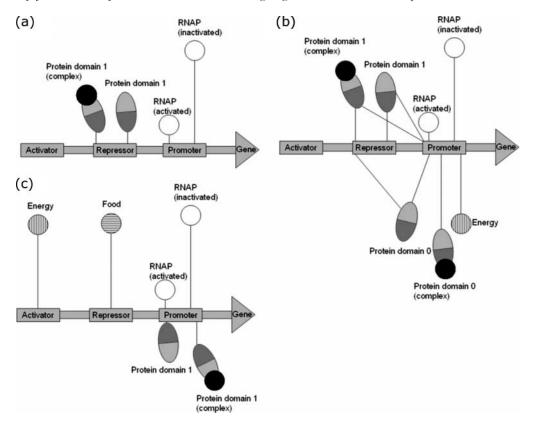


Figure 3. Example of transcription regulation networks. Two cell lineages were observed, each originating from the initial generation. The final population consisted of 95% of models from the major cell lineage, and the remaining 5% from the minor lineage. Specific bindings of $K_d < 100$ nM are shown. (a) shows the ancestor network of the major cell lineage from the population. Very strong repressor binding by a single binding domain of the protein is evident. (b) shows an example evolved network from the major cell lineage. The ancestor repressor connections are still present, although slightly weakened. However, the same protein domain has evolved a specific binding to the promoter site as well. Other evolved specific bindings are the other binding domain of the protein to both the repressor and promoter sites, and energy binding to the promoter site. (c) shows an evolved network from the minor cell lineage from the same population. Specific binding to the repressor site again exists, although using the food molecule, as does specific binding to the promoter site by a single binding domain of the protein. A specific binding to the activator site using the energy molecule also exists, which was not present in the major cell lineage. Binding strength is approximated by molecules' distance from DNA.

transcription factors, causing allosteric changes and affecting the function of the transcription factor. An example is allolactose in the *lac* regulatory mechanism, in which the lactose metabolite binds to the LacI repressor and prevents it from binding to the DNA, potentially allowing the transcription of the *lacZ* gene. A simple solution would be to restrict the domain shapes that the DNA regulatory elements can take. On limiting the shape space, the food or energy molecules will be unable to bind sufficiently well to the DNA regulatory elements, therefore forcing the model to use a protein as a transcription factor.

The emergence of such a fundamental and lifelike network structure indicates the potential power and complexity of the new model as a tool for investigating the evolution of transcription networks.

4.3.4 Protein Is Regulated to a Realistically Small Copy Number

The protein copy numbers observed within evolved models are typically between 50 and 400 molecules, and in the majority of simulations a stable level was reached within this range. The protein copy

numbers per *E. voli* cell of enzymes within the glycolytic pathway range from only 100 copies up to several thousand, each varying in the course of the cell cycle [59], although the numbers for many enzymes are unknown. Although our simulations appear to be at least an order of magnitude different, an enzyme copy number is likely to be a function of its substrate copy number, and so we should observe different levels of protein under different conditions. Each food molecule in our model is equivalent to 14 glucose molecules (see Table 3), and therefore, once we have taken the scaling of food molecules within the model into consideration, the levels of our simulated cell's enzymes are similar to those observed in biological cells. For example, the enzyme phosphoglycerate kinase has a copy number of around 3,000 molecules in the growth phase [59], and assuming each molecule can metabolize only a single 1,3-bisphosphoglycerate molecule at a time, our model would require around 200 proteins to metabolize the equivalent food molecules. This enzyme copy number is well within the observed simulated copy number of many evolved cells; however, it must be noted that our model approximates the glycolytic pathway into a single reaction and so is a much simplified, inexact pathway.

Using the in silico genetics tool, we investigated the effect on the cell's ability to replicate by changing the starting protein level to simulate biased cell replication, which leaves the cell with an extreme amount of protein (very small or large). It is important for biological cells to cope with extremes of protein level, as the replication process may create these situations. Figure 2 shows an example of each extreme case: no protein (Figure 2e) and 500 proteins (Figure 2f). The behavior for no protein is similar to that in the wild-type cell, with the exception of a longer lag period at the beginning of the simulation, as there are no proteins to metabolize the food, nor any transcription taking place. Once the cell has started to transcribe the gene and proteins are produced, the growth of the cell is very similar to wild-type growth. In the opposite case, where there is a large number of proteins at the beginning of the simulation, we see a different dynamic. Due to the large number of free proteins in the cell, the food molecules entering the cell are immediately consumed, producing large amounts of energy. For the same reason, the gene is immediately repressed, preventing any transcription, and so the protein level remains constant.

4.4 Further Discussions

4.4.1 Environments with Increasing Complexity

The results presented previously indicate that even in the simplest of evolutionary environments, we observe nontrivial and realistic behaviors and mechanisms, such as the evolution of rapidly turned-over mRNA and repressor activity. However, the evolved network structures are relatively simple, which is an indication of the simplicity of a chemostatlike environment (an environment that free-living bacteria such as *E. coli* would not normally encounter, nor be adapted to). We predict that in increasingly complex environments, that would be more representative of evolutionary conditions in nature, the model would produce even more complex network structures and solutions. Due to the flexibility of the model, it will be straightforward to create more complex environments, each presenting different problems to be solved.

An example complex environment to investigate would consist of multiple food sources. *E. coli* is able to grow on a number of sugars; in the presence of multiple sugars it is able to selectively metabolize the most energy-efficient food first, using regulatory mechanisms such as the *lac* operon. As the model already implements the *lac* operon's transcription logic, it is fair to assume that a similar switching mechanism requiring both activation and repression activity may evolve within an environment with two or more different food sources.

Another environment may consist of a food source that is varying in a predictable way, analogous to a day-night cycle. Organisms have evolved mechanisms for responding to these cycles, known as circadian rhythms, by developing circadian biological clocks. Prokaryotic circadian clocks, found within cyanobacteria such as *Synechococcus*, consist of only three genes, *kaiA*, *kaiB*, and *kaiC*, which are able to exhibit rhythmic behavior [21]. The proposed regulation of the circadian clock is a feedback

loop involving all three proteins, with unknown interactions between them, and both activation and repression of the genes [31]. Eukaryotes, including mammals and plants, have evolved more complex clocks that include multiple oscillating loops that are thought to provide robustness to noise and seasonal effects [20, 28]. This proposed feedback loop could be represented within our model and could produce a circadian clock that is tuned to the availability of food.

Many organisms live in an environment in which food or other resources are limited and their availability to the organism may fluctuate. The organism therefore requires mechanisms to optimally use these limited resources, for example, the starvation response in $E.\ coli$ governed by RpoS (σ^{5} , σ^{38}) [51]. It is predicted that our model will behave in a similar, albeit simpler, way to that of $E.\ coli$ cells when faced with starvation. Upon detection of carbon starvation, RpoS upregulates the transcription of hundreds of genes that help to protect the cell against stresses, while downregulating hundreds of other genes. The cell enters a stationary phase in which it has an increased chance for survival. Although RpoS is in fact a σ factor that binds to RNAP, helping it to recognize specific promoter sequences, our model could still simulate a similar mechanism. For instance, if the starvation TF could bind strongly to the enzyme's repressor site as an unbound monomer, but when in a complex (with food) were unable to bind, then the same response would be observed: When food is available, the repressor site is unbound, allowing production of the enzyme, whereas if no food is detected by the starvation TF, then enzyme production is prevented. While the current model does not support σ factors, they can easily be incorporated by removing the specific RNAP molecule and allowing any protein with appropriate shape to function as an RNA polymerase.

The current formulation of the model, with its constant environment and generational population structure, is in some ways analogous to a chemostat. Further developments could include an explicit spatial structure, which could potentially lead to coexistence of different species [37]. In the current formulation, replication time is a fair measure of fitness, since in a chemostat the fastest-growing bacteria will dominate the population; in a spatially explicit environment, this is not necessarily the case, and an alternative approach to fitness may be necessary.

4.4.2 Molecule Shape Dimensionality

Our scalable 2D continuous shape space is a substantial simplification of the high-dimensional protein shapes in real cells. Other models, such as the model proposed by van Noort et al. [62] and extended by Cordero and Hogeweg [17], use an even greater simplification, with a 1D discretized shape space, and yet are still able to produce complex and realistic networks. This indicates that a high-dimensional shape space is not essential for the evolution of complex networks; however, an adequately large shape space is required. Future work could investigate the effect of shape space dimensionality on the evolution of complex networks.

4.4.3 Recombination

Recombination is essential for higher-order eukaryotes, and is also thought to be a major source of genetic variation in primeval genomes [57]. While modern day bacteria such as *Escherichia coli* and *Campylobacter jejuni* do not use sexual recombination, they do have other mechanisms for DNA exchange, such as DNA uptake, horizontal gene transfer via plasmids and phages (HGT), and internal genome recombination [47]. In the current model formulation, genes can only be transferred vertically (VGT), that is, they are passed from parent cell to daughter cell only. Future model formulations may include processes of DNA exchange between organisms, such as HGT.

4.4.4 Limitations of the Model

The maximum genome size of the models is currently limited to six genes. This is due to computational requirements of the simulation algorithm (Gibson-Bruck) when simulating large genomes. Use of an alternative simulation algorithm such as the Gillespie algorithm [25] may reduce the computational requirements of larger genomes.

Due to the modeling approach and the necessity for efficient simulation of the model, polymerization is limited to generating complexes of up to three molecules. However, as previously noted, physical structures of the cell, for instance, long polymers, are not modeled, and so this limitation does not harm the model.

A further limitation is the simulation of the environment and evolution. A generational approach, using a genetic algorithm, does not accurately model a growing bacterial culture, in which cells would be dividing at different times. This could lead to some cells dividing several times while others divide only once. This, as well as spatial structure, may be included in future model formulations.

4.4.5 Potential Network Analysis Techniques

The analysis of both the final networks and the dynamics of the evolution of these networks is likely to become increasingly difficult as the complexity of the environment and hence networks increases. The analysis of biological networks currently suffers from a number of problems, such as obtaining networks from data and determining the functionality of particular sections of the network, due to the size of the whole-genome networks and noise in the data collected [45]. The concept of *network motifs* has been introduced to analyze the building blocks of complex networks as a way to elucidate function in the networks, and has been applied to several genomes, including artificial networks [6, 42, 44]. Such an approach may be required to analyze the structure and function of the evolved networks from the model. Applying such a technique across several generations and large simulated evolutionary timescales may help to identify how and why specific network structures are evolved, which is currently not possible with laboratory experiments.

Analyzing the evolutionary dynamics using techniques such as evolutionary activity statistics [8, 13] may provide valuable information and details about the evolutionary process, and may also highlight specific and important components of the system. Once these components have been identified, this information can be used along with traditional network analysis, such as network motifs, to help identify and separate functional modules within the networks.

5 Summary and Conclusion

In this study a new model of evolving transcription control networks in prokaryotic cells has been introduced. The model incorporates several novel mechanisms, realistic and evolvable parameters, and a scalable level of complexity. The models are simulated using a stochastic framework, from which the dynamics of the model were investigated over a range of parameters. Several key realistic network structures and model behaviors were observed, and important parameters determining whether a model would replicate are presented and discussed.

Evolutionary runs of the models were performed using a standard genetic algorithm incorporating realistic evolutionary operators, in an idealized constant-food environment. The initial and evolved networks are presented, as well as overall population dynamics. The results of these evolutions show that over the short evolutionary time frame used, the models optimize their initial network configurations to produce a more robust and shorter replication time, and a few novel network interactions were introduced. Several realistic behaviors emerged during the simulated evolution. A realistic cell replication time emerged, and the most efficiently replicating models consisted of a single gene, which controlled its own expression through a repressor mechanism, indicating a necessity to remove nonessential genes. This network structure (or motif) is prevalent in many instances in all organisms, and typically one of its purposes is maintaining protein levels. Realistic mRNA and protein degradation rates evolved that also follow the general principles found in *E. coli* and *S. cerevisiae* in typically displaying differences up to several orders of magnitude between the stabilities of mRNA and proteins.

The robustness of the evolved models was investigated using in silico genetics to produce mutant models consisting of various knockouts and perturbations to the stability of molecules and com-

plexes. Many models were shown to be resilient against fairly large perturbations; however, the dynamics of the models after certain mutations (such as regulatory site knockouts) were substantially changed, as would be expected from real cells.

The exploratory results presented in this study indicate that the model allows reasonably realistic modeling and evolution of transcription control networks in an abstracted prokaryotic cell, allowing complex behaviors in simple environments, and provides the functionality to easily simulate more complex and biologically interesting environments.

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Appendix I: Mutation Operator

For each gene in the genome, the binding sites of its regulatory region elements, its mRNA product, and its protein product can mutate with a specified probability. The mutation operator on shape is as follows:

• Random noise is generated at the pole of the shape sphere

$$\eta$$
 = random normal (mean = 0, std. dev. = SHAPE NOISE_SDEV) (in the θ direction) (4)

$$\psi = \text{random } [0, 2\pi) \quad \text{(in the } \phi \text{ direction)}$$
(5)

• The generated noise is then rotated to the current coordinates $(\theta, \, \varphi)$ using Cartesian algebra:

$$x = \cos\theta \, \cos\phi \, \sin\eta \, \cos\psi - \sin\phi \, \sin\eta \, \sin\psi + \sin\theta \, \cos\phi \, \cos\eta \tag{6}$$

$$y = \cos\theta \sin\phi \sin\eta \cos\psi + \cos\phi \sin\eta \sin\psi + \sin\theta \sin\phi \cos\eta$$
 (7)

$$z = -\sin\theta \sin\eta \cos\psi + \cos\theta \cos\eta \tag{8}$$

The Cartesian coordinates can then be transformed back into polar coordinates in the standard way.

As well as the shape mutation, the mRNA and protein product can mutate their degradation rate with lognormal noise:

degradation rate_{new} = degradation rate_{old}
$$\times$$
 10^{random normal (mean=0,std. dev.=DEG RATE NOISE SDEV)} (9)

Appendix 2: Structural Parameter Analysis

The distribution of random models meeting the three termination criteria (replicate, stationary, and death) was investigated over a large range of the binding affinity parameters, σ and α . The results of 1000 randomly initialized models for each parameter setting (10^{-3} up to 10^{3}), simulated in a constant and abundant food environment (meaning that the model will always be able to take up food at the specified rate), are shown in Figure 4. Figure 4a shows the replicating models for each

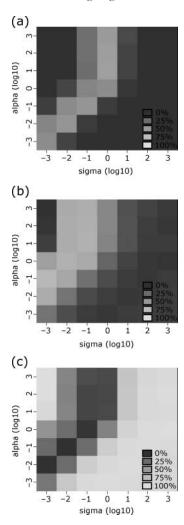


Figure 4. Random model simulations over structural parameters. (a) shows the proportion of models replicating in each of the environments. A clear light band can be seen passing through from bottom left to top middle, indicating environments that are easier to survive in. (b) shows the proportion of models that are stationary. A darker band is seen, indicating fewer stationary models following the same pattern as in (a), although skewed to the left. (c) shows the proportion of models that died in each environment. A light band can again be seen, and follows the same pattern as the dark band in (b). Black is 0%, white is 100%.

parameter, where a clear band of livable parameters can be seen. We see in Figure 4b that it is highly likely for a random model to be simulated for an hour without replicating; from Figure 4c we have the inverse of (a), and we see a band of non-dying parameters and the majority of parameters giving a large percentage of dying models. It is useful to see the parameter ranges in which random models struggle to replicate, as parameters in those ranges will provide good starting points for evolution, and will encourage more searching of the solution space. The parameter ranges used for subsequent evolutionary experiments were $\sigma=1$ to 50 and $\alpha=1$.

Appendix 3: Parameter Analysis

Table 9 shows the full univariate analysis results for all 26 parameters, and Table 10 shows the proportions of all 26 parameters in the optimal solutions generated from the multivariate analysis.

Appendix 4: Evolution Results: Population Dynamics A4.1 Affects of σ and Mutation Rate on Population Dynamics

Results from the experiments indicate that the binding affinity parameter σ has a substantial effect on the potential for evolving models. In Figure 5a we can see a low-mutation environment with a very small σ. The population is very quickly (within five generations) dominated by models that are replicating, and by the end of the short evolution of 50 generations we can see that the final population had around 95% replicating models, with no models being in the stationary phase after 1 h. In comparison with the initial population, less than 40% of models were replicating, and around 20% were in the stationary phase, leaving the remaining 40% of models dying. However, we see a very different population dynamic if we have a larger σ value. Figure 5b shows a low-mutation environment, but with a large binding affinity value $\sigma = 50$. Here 95% of the initial population die, with no models replicating at all. In the early stages of the evolution we see a slight increase in the number of models that do not die, but do not replicate either, and we start to see models that are persistently capable of replicating, but do not quickly take over the population as was seen in Figure 5a. Around halfway through the evolution by generation 25, we start to see a monotonic increase in replicating models, and by generation 40 up to 75% of the population consists of replicating models. However, the proportion of stationary models each generation remains fairly constant between 10% and 20%, as do those of replicating and dying models after generation 40.

In a high-mutation environment we see a similar population dynamic (Figure 5c). The small value of σ once again quickly reaches a large number of models, which replicate, albeit slightly slower than in the low-mutation environment. Also, the replicating models only consist of around 90% of the population, less than in the low-mutation environment. In a high-mutation environment with a larger σ we can also see a similar behavior to that in a low-mutation environment. Figure 5d shows $\sigma=30$, where the same initial lag period before the models capable of replicating begin to fill the population occurs as in the low-mutation environment. Once again the maximum number of replicating models is lower than in the low-mutation environment. In some cases of larger σ , no replicating models are able to establish themselves within the population, as shown in Figure 6.

This change in behavior can be explained in two ways. Firstly, the size of the binding affinity parameter σ determines the shape space's complexity. In a low-value shape space, there are effectively fewer shapes that each molecule can take, and so it is more likely to have an initial population with a number of models that have similar enough shapes to provide the required interactions and dynamics. With a larger value, the shape space increases in size; therefore molecule shapes have to be more accurate to achieve the same interactions and dynamics required. As we can see from the figures, low-σ environments start with a larger number of replicating models, up to 40% of the population, whereas in a higher- σ environment it takes many generations of searching the shape space for a random model to survive and replicate well enough to start propagating through the population. Secondly, the mutation rate affects the rate of evolution within the population. In the low-mutation environment, the population quickly reaches equilibrium, where around 95% of the population are replicating models. The low mutation rate also means that once a model has achieved the required interactions and dynamics to replicate, it is unlikely to mutate away from this state, and so we see only 5% of the population dies each generation. This death rate will also be due to stochastic affects, as there is a small probability that even the most highly optimized model will die. In the high-mutation environment, we can see that the mutation rate of 50% is having a detrimental affect on the evolution. While the initial population has a similar distribution of models to that in the low-mutation environment, it takes several generations longer to reach equilibrium, and once it has reached it there is a larger proportion of dying models, as it is more likely that a model will mutate and lose required interactions.

A4.2 Genome Size in the Population

Genome size was also recorded during evolution. In a low-mutation environment, the average genome size is no larger than 1.3 genes per model, larger models are quickly selected out, and a low equilibrium

genome size is achieved within the population. In contrast, in the high-mutation environment the average genome size quickly reaches around 1.7 genes per model, and again stays around this size. A small genome size is expected, due to the simple environmental challenges requiring little complex regulation and also due to the selection pressure implicitly imposed by the replication criteria. Each gene requires an extra 10% energy of the replication threshold, which means that junk genes will be detrimental to reaching its replication threshold. Results of evolutionary runs where the genome size was initially larger than 1 gene also show an average final gene size slightly larger than 1, indicating that the extra genes are not likely to be required for efficient and fast replication.

A4.3 Cell Lineages in the Population

Examining the final population of each evolution shows that the majority of all models in the population come from a single common ancestor. In the low-mutation, low- σ environment the final population usually consisted of two *lineages*; in one case the population was split approximately equally between them, but in another case 95% of the models had the same initial ancestor. In all cases in this environment, all the lineages could be traced back to the initial population. In a high- σ environment we see a different pattern. Instead of multiple lineages competing for space in the population, we see the dominance of a single model. In two cases 100% of the final population consisted of models derived from a single model (emerging in generations 1 and 3), and the third case consisted of two lineages with offspring from one model from generation 19 contributing to 98% of the population; the other 2% were from a model from the initial population. In a high-mutation environment we see different population distributions. In a low- σ environment there is a mixture between complete dominance of a single model and partial dominance of one model against either one or two other models. In all cases, however, all the models trace back to the initial population. In the high- σ environment a different population distribution is dominant. In each case the final population consists of over 50 lineages, each occupying only 1–10% of the population, but tracing back up to 20 generations.

Table 9. Univariate analysis of all evolvable parameters. For each parameter its ID number, original p-value from a logistic regression, adjusted q-value from controlling the false-discovery rate, its classification accuracy, and its sensitivity and specificity are shown.

Parameter	ID	Þ	q	Classification accuracy (%)	Sensitivity	Specificity
Protein degradation rate	22	<2e ⁻¹⁶	5.2e ⁻¹⁵	81.7	0.77803	0.84838
Protein-repressor complex $k_{\rm off}$	5	1.38e ⁻¹⁰	1.794e ⁻⁹	54.7	0.32287	0.77617
Protein-promoter complex $k_{\rm off}$	6	1.29e ⁻⁸	1.118e ⁻⁷	60.4	0.34978	0.80866
All-promoter complex $k_{\rm off}$	26	1.06e ⁻⁷	6.89e ⁻⁷	57.6	0.28027	0.81408
mRNA degradation rate	23	6.05e ⁻⁷	3.146e ⁻⁶	58.1	0.32287	0.78881
Energy-promoter complex $k_{\rm off}$	14	8.1e ⁻⁵	3.51e ⁻⁴	58.3	0.23318	0.86462
Food-repressor complex $k_{\rm off}$	10	0.00273	0.01014	55.3	0.12556	0.89711
Protein-protein complex $k_{\rm off}$	8	0.00346	0.011245	56	0.12108	0.91336
Protein-RNAP complex $k_{\rm off}$	3	0.0233	0.06731	56.8	0.08969	0.95307
Energy-repressor complex $k_{\rm off}$	13	0.0375	0.0975	55.1	0.03587	0.96570

Table 9. (continued)

Parameter	ID	Þ	q	Classification accuracy (%)	Sensitivity	Specificity
Protein-food complex k _{off}	I	0.0428	0.097301	55.3	0.04484	0.96209
All-repressor complex $k_{\rm off}$	25	0.044908	0.097301	55.5	0.06278	0.95126
Protein-energy complex $k_{\rm off}$	2	0.0975	0.195	55.1	0.01794	0.98014
Food-activator complex $k_{\rm off}$	9	0.38195	0.70934	55.6	0.00673	0.99819
mRNA-activator complex k_{off}	17	0.43156	0.7480	55.3	0	0.99819
mRNA-promoter complex $k_{\rm off}$	19	0.4857	0.7893	55.4	0	1
Protein-activator complex $k_{\rm off}$	4	0.5166	0.7901	55.4	0	1
Energy-activator complex $k_{\rm off}$	12	0.56378	0.81435	55.5	0.00224	I
Protein-mRNA complex $k_{\rm off}$	7	0.61995	0.84835	55.4	0	1
mRNA-repressor complex $k_{\rm off}$	18	0.6368	0.82784	55.4	0	1
Food-promoter complex $k_{\rm off}$	П	0.739600	0.9156952	55.4	0	1
All-activator complex $k_{\rm off}$	24	0.906519	0.9712	55.4	0	1
RNAP-repressor complex $k_{\rm off}$	16	0.9084	0.9712	55.4	0	1
mRNA-energy complex $k_{\rm off}$	21	0.9651	0.9712	55.4	0	1
RNAP-activator complex $k_{\rm off}$	15	0.9655	0.9712	55.4	0	1
mRNA-food complex $k_{\rm off}$	20	0.9712	0.9712	55.4	0	1
All-activator complex $k_{\rm off}$	24	0.906519	0.9712	55.4	0	1
RNAP-repressor complex $k_{\rm off}$	16	0.9084	0.9712	55.4	0	1
mRNA-energy complex $k_{\rm off}$	21	0.9651	0.9712	55.4	0	1
RNAP-activator complex $k_{\rm off}$	15	0.9655	0.9712	55.4	0	I
mRNA-food complex $k_{\rm off}$	20	0.9712	0.9712	55.4	0	1

Table 10. Evolvable parameters selected in all solutions generated by GALGO. For each parameter its ID number and its percentages in solutions of different model sizes are shown.

			Percentage	Percentage in model size	
Parameter	ID	2	3	4	5
Protein-food complex k _{off}	I	0	1.2	0.5	2.4
Protein-energy complex $k_{\rm off}$	2	0	1.2	3.8	7.4
Protein-RNAP complex $k_{\rm off}$	3	0.3	2.4	11.3	4.2
Protein-activator complex $k_{\rm off}$	4	0	1.5	3.3	10.1
Protein-repressor complex $k_{\rm off}$	5	88.7	81.5	74.4	97.8
Protein-promoter complex $k_{\rm off}$	6	7.5	29.4	66.1	65.4
Protein-mRNA complex $k_{\rm off}$	7	0	2.6	3.9	6.1
Protein-protein complex $k_{\rm off}$	8	0	0.1	6	6.3
Food-activator complex $k_{\rm off}$	9	0	1.8	4.7	5.2
Food-repressor complex $k_{\rm off}$	10	0	0.2	4.4	5
Food-promoter complex k_{off}	П	0	0.3	4.4	3.8
Energy-activator complex $k_{\rm off}$	12	0	0.1	4	7
Energy-repressor complex $k_{\rm off}$	13	0	0.8	9.2	19.4
Energy-promoter complex $k_{\rm off}$	14	0	13.6	23.3	31.8
RNAP-activator complex $k_{\rm off}$	15	0	0.1	4.6	7.4
RNAP-repressor complex $k_{\rm off}$	16	0	0.2	3.1	7.1
mRNA-activator complex $k_{\rm off}$	17	0.1	0	2.2	5.7
mRNA-repressor complex $k_{\rm off}$	18	0	0.4	1.6	6.6
mRNA-promoter complex $k_{\rm off}$	19	0	1.6	2.8	11.8
mRNA-food complex $k_{\rm off}$	20	0	0	3.9	4.9
mRNA-energy complex $k_{\rm off}$	21	0	0.5	1.4	6.1
Protein degradation rate	22	100	100	100	100

Table 10. (continued)

Parameter	ID	Percentage in model size			
		2	3	4	5
mRNA degradation rate	23	0.5	36.7	31.2	23.4
All-activator complex $k_{\rm off}$	24	0	7.6	1.9	5.4
All-repressor complex k _{off}	25	0	7.1	2.7	9.6
All-promoter complex $k_{\rm off}$	26	2.9	6.7	17.3	21.9

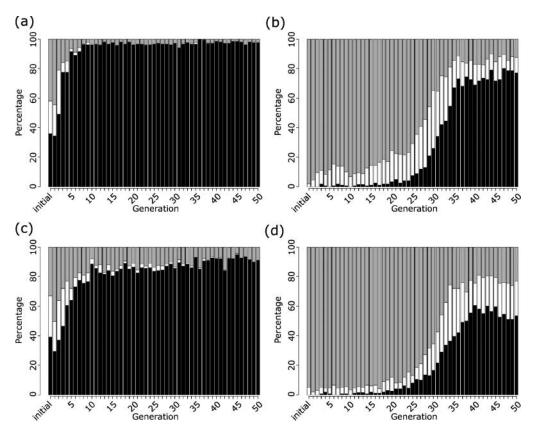


Figure 5. Population status of each generation. Black replication, white stationary, gray death. (a) shows a low-mutation environment and σ = 1, in which the population very quickly becomes dominated by replicating models. A small proportion of models in each generation die, likely due to stochasticity. (b) shows a low mutation environment and σ = 50, where the population initially consists mainly of dying models, but after around 20 generations replicating models begin to establish themselves within the population. The population then rapidly becomes dominated by the replicating models, reaching an equilibrium around generation 35. (c) shows a high-mutation environment and σ = 1, where the population again rapidly becomes dominated by replicating models. However, the proportion of dying models each generation is higher than in a low-mutation environment, indicating more detrimental mutations taking place. (d) shows a high-mutation environment and σ = 30, which again shows a substantial number of generations dominated by dying models. Replicating models again begin to establish themselves within the population around generation 20, and rapidly dominate the population. The proportion of models replicating when the population has reached equilibrium is smaller than in other regimes.

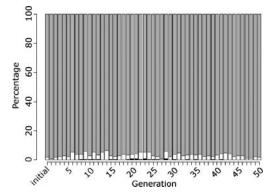


Figure 6. Population status of each generation. Black replication, white stationary, gray death. High-mutation environment and σ = 50. Due to the large σ value, it is very difficult to generate replicating models, and so the population consists mainly of dying models.