Developmental Origin of Patchy Axonal Connectivity in the Neocortex: A Computational Model

Roman Bauer1, Frederic Zubler1, Andreas Hauri1, Dylan R. Muir2 and Rodney J. Douglas1

1Institute of Neuroinformatics, University of Zürich and Swiss Federal Institute of Technology Zürich, 2Department of Neurophysiology, Brain Research Institute, University of Zürich, Zürich CH-8057, Switzerland

Address correspondence to Roman Bauer, Institute of Neuroinformatics, University of Zürich and Swiss Federal Institute of Technology Zürich, Winterthurerstrasse 190, CH-8057 Zürich, Switzerland. Email: bauerr@ini.phys.ethz.ch.

Injections of neural tracers into many mammalian neocortical areas reveal a common patchy motif of clustered axonal projections. We studied in simulation a mathematical model for neuronal development in order to investigate how this patchy connectivity could arise in layer II/III of the neocortex. In our model, individual neurons of this layer expressed the activator–inhibitor components of a Gierer–Meinhardt reaction–diffusion system. The resultant steady-state reaction–diffusion pattern across the neuronal population was approximately hexagonal. Growth cones at the tips of extending axons used the various morphogens secreted by intrapatch neurons as guidance cues to direct their growth and invoke axonal arborization, so yielding a patchy distribution of arborization across the entire layer II/III. We found that adjustment of a single parameter yields the intriguing linear relationship between average patch diameter and interpatch spacing that has been observed experimentally over many cortical areas and species. We conclude that a simple Gierer–Meinhardt system expressed by the neurons of the developing neocortex is sufficient to explain the patterns of clustered connectivity observed experimentally.

Keywords: neural development, reaction–diffusion models, self-organization, simulation, superficial patch system

Introduction

Focal injections of neural tracers into the neocortex result in quasi-periodic patch labeling of somata and axonal terminations that may extend over several square millimeters within a cortical area (Rockland and Lund 1982, 1983; Rockland et al. 1982; Gilbert and Wiesel 1989; Lund et al. 2003; Fig. 1A). These patches are most prominent in the superficial layers where pyramidal neurons give rise to laterally extending intralaminar axons that support the clusters of boutons (Kisvarday and Eysel 1992; Buzás et al. 2006; Binzegger et al. 2007), suggesting that the laminar patches are composed of neuronal clusters (Muir and Douglas 2011).

The “patch system” (Rockland and Lund 1982; Rockland et al. 1982) or “daisy architecture” (Douglas and Martin 2004) is observed across many cortical areas and species. The remarkably regular scaling of patch diameter to interpatch distance across these many areas and species (Fig. 1B) suggests that patches are a fundamental motif of cortical organization and function (Douglas and Martin 2004; Muir et al. 2011). Indeed, there is good agreement between the spatial patterns of the functional domains observed by optical imaging of the intrinsic signal associated with cortical neuronal activity and the spatial patterns of the anatomical patches (Muir et al. 2011). The interneighbor distances and angles indicate that the patches form an hexagonal lattice that is relatively periodic and isotropic in the visual cortex, but may be less so in other areas (Muir and Douglas 2011; Muir et al. 2011).

Various explanations have been offered for how this patchy organization could arise. For example, Mitchison and Crick (1982) and Buzás et al. (2006) proposed mechanisms that depend on the developing functional relationship between neurons in the visual cortex that are already able to respond to visual stimuli. However, these models are incomplete because patches are found also in areas other than in visual cortex and can be observed in a coarse form before the afferents carrying structured electrical signals arrive in the superficial layers of the cortex (Price 1986; Callaway and Katz 1990; Ruthazer and Stryker 1996). These observations imply that the patchy organization is broadly prespecified, at least on a coarse scale, and that they are refined later by the suitable patterns of afferent electrical activity (Luhmann et al. 1986; Wong 1999; Grossberg and Seitz 2003; Liets et al. 2003; Kanold 2004).

In this paper, we explore the possibility of genetic specification of the patch system. Our hypothesis is that a precursor of the patchy organization develops as early as in the cortical preplate and that the pattern is preserved during corticogenesis and lamination. Neurons preserve clonal features of their precursors in a columnar fashion due to their migration along radial glial cells in a manner consistent with Rakic’s protomap hypothesis (Rakic 1988).

In our model of patch formation, neuronal precursors are genetically disposed to secrete a set of morphogens that are able to diffuse through the extracellular matrix. These morphogens are transcription factors whose interactions with the “genome” follow Gierer–Meinhardt reaction–diffusion dynamics (Turing 1952; Gierer and Meinhardt 1972). Consequently, the precursors of the preplate come to express a two-dimensional periodic profile of morphogens that provides the basis for clusters of neurons expressing similar profiles. This periodic identity is inherited from the precursors by their daughter neurons, which migrate radially to form the superficial cortical layers. When these migrating neurons come to rest, they extend lateral axons whose growth cones seek distant target neurons with similar morphogen expression profiles to their own, so generating the observed patchy organization.

We have explored this hypothesis using 2 different simulation approaches. For most of the work we used Cx3D (Zubler and Douglas 2009), in which the detailed physical mechanisms of neuronal growth and cortical development can be simulated. We used this software to demonstrate how a reaction–diffusion system in a layer of progenitor cells leads finally to the formation of patterned axonal lateral connections compatible with the observations.
Our investigations show that the superficial patch system could be specified in the very early stages of cortical development. In particular, we show how a coarse form of this connectivity pattern can be generated without any instructive electrophysiological activity. Our simulation is in agreement with and offers an explanation for several experimental findings.

**Materials and Methods**

Simulations were performed using the open-source Java Package Cx3D (Zubler and Douglas 2009; Zubler et al. 2011), available from http://www.ini.uzh.ch/projects/cx3d/ and with MATLAB (Mathworks Inc.). The computer used to run simulations had two 12-core processors (1.9 GHz, 64 GB of RAM).

**Reaction–Diffusion Parameters**

We used well established mathematical tools such as linear stability analysis to provide estimates of the regimes in the parameter space that lead to the desired pattern class. The parameters used for the various simulations of the pattern formation are listed in Table 1.

**Reaction–Diffusion Mechanism**

We used the Gierer–Meinhardt reaction–diffusion system (Gierer and Meinhardt 1972) for simulating the pattern formation mechanism. The system is described by the following partial differential equations:

\[
\begin{align*}
\frac{\partial a}{\partial t} &= \rho \frac{a^3}{b} - \mu_a a + \rho_a + D_a \frac{\partial^2 a}{\partial x^2} \\
\frac{\partial b}{\partial t} &= \rho a^2 - \mu_b b + \rho_b + D_b \frac{\partial^2 b}{\partial x^2}
\end{align*}
\]

where \(a(x,t)\) and \(b(x,t)\) indicate the activator and inhibitor substance concentrations at location \(x\) and time \(t\), and \(D_a\) and \(D_b\) are the morphogen diffusion coefficients, and \(\rho\) is the production coefficient, \(\mu_a\) and \(\mu_b\) are the substance decay coefficients, and \(\rho_a\) and \(\rho_b\) are the basal production coefficients. Appropriate parameters allow this system to converge toward a spatially patterned equilibrium of morphogen concentrations.

The equations for the extended secretion model in the case of multiple Gierer–Meinhardt systems can be written as follows:

\[
\begin{align*}
\frac{\partial a_i}{\partial t} &= \rho_i \frac{a_i^3}{b_i} - \mu_{a_i} a_i + \rho_{a_i} + D_{a_i} \frac{\partial^2 a_i}{\partial x^2} - \sum_{j \neq i} r_{aj} \\
\frac{\partial b_i}{\partial t} &= \rho_i a_i^2 - \mu_{b_i} b_i + \rho_{b_i} + D_{b_i} \frac{\partial^2 b_i}{\partial x^2}
\end{align*}
\]

where the repulsion term \(\sum_{j \neq i} r_{aj}\) is subtracted from the activator term.

The indices \(i,j\) represent different activator types.

**Multiagent Simulation**

Cx3D provides a sophisticated framework for simulating neural development in 3-dimensional (3D) space (Zubler and Douglas 2009). Neurons are composed of discrete physical components such as spheres (somata) and chains of cylinders (neurites), each located at a particular point in 3D space. Extracellular space is also discretized into small nonoverlapping domains, allowing for the diffusion of signaling molecules. Each cell element is the center of such a space.
domain. Additional space domains are added to increase the precision of diffusion. To provide the desired cellular functionality, Cx3D users can write biological modules, Java classes that are inserted into the cells or cell components of the simulation. These modules lend the cells their functional attributes.

The main difference to the classical approach of reaction–diffusion on a regular grid is that in Cx3D we decouple the mechanisms occurring in the extracellular space (diffusion and degradation). For instance, for the implementation of the system given by equations (1), the terms \[ \rho_a^+ h \rho_a^+ p_e^a \] and \[ \rho_a^+ h \rho_e^a \] are coded in a "biological module" inside the cells, releasing the amounts of substances \( a \) and \( b \) according to the extracellular concentrations of these substances felt locally by each cell. Diffusion and degradation of these substances are automatically performed by the physics engine of Cx3D and occur even in the absence of cells.

Cellular somata are modeled as spheres with a diameter of 20 \( \mu \text{m} \), placed in an irregular constellation, to form a sheet of 100 \( \times 100 \) cells. Physical interactions ensure that they redistribute themselves after initialization, such that the average intersomatic distance converges to roughly 22 \( \mu \text{m} \). We add 25,000 additional space nodes for a more accurate simulation of diffusion. For a detailed description of the numerical procedure in Cx3D, we refer to the original description in Zubler and Douglas (2009).

**Regular Grid**

We performed some simulations of pattern formation on regular grids, which provide an advantage in numerical simulation performance over the irregular environment of Cx3D. Consequently, some investigations requiring numerous trials or larger-scale simulation were based on MATLAB simulations on regular grids.

The differential equations were solved numerically on a discretized grid (in 2-dimensional (2D) in contrast to the 3D simulations in Cx3D) of 150 \( \times \) 150 cells with the explicit Euler method for calculating the time evolution of the substance concentrations. Unlike in Cx3D, we did not make a distinction between concentration and quantity, because in this case, all domains have the same dimension. At each time step, we solved first the diffusion, that is, we updated the value of each bin \( i \) based on the Fickian flux with its 4 neighbors (given by the concentration difference multiplied by the diffusion coefficient multiplied by the time step, \( dt = 0.001 \)). Then we updated the value to account for the reaction component, by computing the change in the substance quantities based on the current activator and inhibitor values, and adding it to each bin \( i \) (explicit Euler method).

Simulation was initialized with concentration values drawn from a uniform distribution between 0.3 and 0.7. An example script of a Gierer–Meinhardt activator–inhibitor system with parameters leading to patchy patterns is included in the Supplementary Material (Supplementary Scripts 1).

**Pattern Characterization**

Quantitative analysis of the outcome of reaction–diffusion simulations was performed in MATLAB. We defined a "patch" as an area of increased concentration of a morphogenetic substance, identified by an automated method based on the fitting of Gaussians, as described in Muir et al. (2011). Subsequently, a graph connecting neighboring patch locations was constructed using a Gabriel graphing technique (Gabriel and Sokal 1969; Tanigawa et al. 2005; Muir et al. 2011). This graph provided estimates of the patch locations, number of patches, mean distances between patches and angles between neighboring patches in a given pattern. These measures were used to compare simulation results against the experimental data. The estimates depend on the expected size of the patches, which is given as an input to the algorithm. This input was determined using the method described in Shen and Jung (2005). This method yields estimates of the average size and number of patches by first segmenting the concentration patterns using binary thresholding and subsequently calculating standard image processing measures. Our implementation is included in Supplementary Material (Supplementary Scripts 2).

We developed an algorithm that uses the methods described above to classify the patterns of substance concentrations as patchy or non-patchy. We first assessed the positions of the patches of the activator and inhibitor substance patterns. In the ideal case, the patches of the activator morphogen should match in position with the inhibitor patches (see Results). If the estimated locations of the corresponding patches in those 2 patterns deviated too much from one another, that is, if more than 25% of the patches are separated by more than 6 grid cells, then the pattern was classified as nonpatchy. The parameters of the algorithm were determined heuristically to optimize its performance (Supplementary Fig. 2 for 3 example patterns that were correctly classified).

**Axonal Growth**

Axonal growth was simulated as a growth cone able to sense substance concentrations and gradients (in Cx3D). When an axon bifurcates, its daughter branches receive a copy of the parent growth cone (and its rules) resulting in a recursive ramification of the terminal axon.

We used a growth rule that uses the activator substance in the Gierer–Meinhardt system as a guidance cue. Growth direction was defined at each time step as the weighted vectorial sum of a random direction, the gradient of the activator substance and some measure of the previous movement direction: \[ \mathbf{d} = w_{\text{noise}} \mathbf{d}_{\text{noise}} + w_{\text{grad}} \mathbf{d}_{\text{grad}} + w_{\text{prev}} \mathbf{d}_{\text{prev}} \]. In all simulations, we used \( w_{\text{noise}} = 0.34 \), \( w_{\text{grad}} = 0.03 \), and \( w_{\text{prev}} = 0.60 \). These weights have been chosen to fit the curvature of long-range layer II/III projections as observed in the cat visual cortex (Ruesch 2011). Outgrowth speed was constant (35 \( \mu\text{m}/\text{h} \), independent of activator concentration). The probability of an axon to bifurcate was computed at each time step as \( P_{\text{Bifurcate}} = u_a \cdot \Delta t \), where \( C_a \) is the concentration of the activator. The constant \( u \) determines how strongly bifurcation probability is influenced by the extracellular substance concentration, and \( \Delta t \) is added to allow bifurcation to occur also in the space between patches. Axon diameter reduces during elongation and at branch points. When a specified minimal diameter is reached, growth ceases. For the growth rule of a single-patch system (see Results for a description of the 2 growth rules), \( u \) and \( v \) were chosen to be \( 2.6 \times 10^{-4} \) and \( 2.1 \times 10^{-5} \), respectively. In the multiple patch systems, these values were \( 5 \times 10^{-7} \) and \( 2.1 \times 10^{-5} \). Diameter reduction parameters due to growth and bifurcation were \(-0.1\%\) and \(-10\%\) (at each step) in the first scenario, and \(-0.05\%\) and \(-10\%\) in the second. In both cases, the initial diameter was \( 3 \mu\text{m} \) and the minimal diameter criteria to stop outgrowth was \( 0.5 \mu\text{m} \).

Simulations with these parameters resulted in axonal arborizations with distinct patchy projections that matched our experimental observations. For example, the number of clusters formed by a single axon lay in the range of 1–7, and cluster diameters were between 90 and 950 \( \mu\text{m} \) (Binzegger et al. 2010).

**Results**

**The Gierer–Meinhardt Model**

We used the reaction–diffusion model proposed by Gierer and Meinhardt (1972) (equation 1), because it offers the necessary stability to generate patchy patterns, and because its dynamics can be interpreted as the interaction of 2 morphogens. Their system consists of a local autocatalytic activator \( a \) and a rapidly diffusing inhibitor \( b \); \( a \) promotes its own production, as well as the production of the inhibitor \( b \), whereas \( b \) suppresses the production of \( a \). These 2 antagonistic substances can lead to regions (patches) of high activator and inhibitor concentration (because the activator drives production of the inhibitor), separated by regions of low morphogen concentration. With a grasp of the various regimes of this system (see Materials and Methods), we could demonstrate the required patchy patterns in continuous space.
Single Global Pattern in a Sheet of Cells
Patchy patterns were computed using standard numerical methods on a regular grid. However, our question of whether sheets of individual cells can generate a similar patterning of their behavior brings complications that need not be confronted in the more simple numerical/continuous case (Bonabeau 1997). First, the generators and consumers of morphogens are now individual cells, whose volume and separation effectively quantize the space in which the reaction–diffusion process will play out. Of course, morphogens can diffuse between cells. This diffusion through extracellular space is quantized more finely than the discretization imposed by the cellular positions alone. Secondly, cells are not restricted to a regular grid. They interact mechanically with their neighbors, and so cell locations within a layer are perturbable. And finally, these cells must maintain the patchy morphogen distributions during the developmental process, when cells are migrating radially from their birthplace in the subventricular zone to become superficial layer neurons. It is this more complex problem that we have explored by simulations in Cx3D, rather than in MATLAB.

We simulated the development of a pattern of patches on a 2D sheet of cells that secrete morphogens according to the Gierer–Meinhardt kinetics. Simulations begin with a random distribution of morphogens across random cell body locations. Figure 2 shows a sequence of images derived from a Cx3D simulation in which the process of pattern formation evolves over time. In the initial stages, symmetry-breaking drives the initial random pattern (A) toward blurred patches consisting of high levels of both the activator and inhibitor morphogens. These patches become more distinct over time and decrease in number due to the growing lateral influence of the inhibitor substance (B–E). For appropriately chosen parameters, the final pattern converges to a steady state (F) that resembles strongly the observed pattern of cortical patches. The parameters of the pattern formation kinetics (equations 1) are listed in Table 1.

Supportive Evidence for the Gierer–Meinhardt Model
Linear Scaling of Spatial Characteristics
Analysis of experimental data from the cortical areas of many species has shown that there is a linear relationship between the patch diameter and mean interpatch distance (Lund et al. 1993; Binzegger et al. 2007; Muir et al. 2011), the spacing being approximately twice the average width of the patches. This as yet unexplained relationship can be understood in the context of our model.

In their mathematical analysis of the Gierer–Meinhardt model, Page et al. (2005) explored the effect of certain parameters on the resulting patterns. They show analytically that the average patch size is proportional to \( D_a \) and that the interpatch distance is proportional to \( D_h \). If we consider a common scaling factor \( D \) for \( D_a \) and \( D_h \), such that \( D_a = D \cdot D'_a \) and \( D_h = D \cdot D'_h \), then this result explains the linear relationship between patch diameter and interpatch distance when \( D \) and therefore both the diffusion coefficients vary. However, the assumption of different diffusion coefficients in different cortical areas and species is not biologically plausible. The magnitudes of physical variables influencing the diffusion coefficients, such as viscosity or temperature, are not thought to vary by large amounts. We therefore investigated what other parameters influence the spatial profile in a similar manner. We found both analytically and by simulation that the linear scaling is also obtained when the production...
coefficient (parameter $\rho$ in equations 1) is varied. This effect can be shown as follows: In the converged state ($\partial a / \partial t = \partial b / \partial t = 0$), the decay and the basal production (parameters $\mu_a$, $\rho_a$, $\mu_b$, and $\rho_b$ in equations 1) can be neglected as they are usually relatively small:

$$-\rho \frac{a^2}{b} \approx D \cdot D_a \frac{\partial^2 a}{\partial x^2}$$

$$-\rho \frac{a^2}{b} \approx D \cdot D_b \frac{\partial^2 b}{\partial x^2}$$

Together with the result from Page et al. (2005), our results show that varying the diffusion coefficients or the production coefficient changes the scale of the patch size and spacing. $\rho$ and $D$ linearly scale the right or left-hand side term of equations (3), so they influence the spatial characteristics of the pattern by varying the proportion of the production versus the diffusion term. We find that the linear relationship for the case when the production coefficient is varied is valid also under conditions where the basal production coefficients are not negligible, as for example in the simulations in Figure 3. The slope of the linear relationship is similar for our simulations and the experimental data (approximately 2), but depends on the parameters of the model: Different parameters yield different relations. The appropriate linear scaling was also confirmed in simulations done in MATLAB (Supplementary Fig. 1). The MATLAB simulations showed a more linear scaling behavior, which can be explained through the larger simulation grid ($150 \times 150$ cells instead of $100 \times 100$ in Cx3D) and the regular arrangement of substance producing cells. Figure 3 shows 2 examples of patterns (A,B) produced with 2 different production coefficients ($\rho = 600$ and $\rho = 35$) and the scaling behavior across 120 patterns with different production coefficients (B). Also note the higher density of patches with small patch diameter and spacing, a feature that is shared with biological data (Fig. 1B). The Gierer–Meinhardt parameters used in these simulations are listed in Table 1.

Our interpretation is that the observed relationship of patch size versus interpatch distance arises, because the production rate of morphogens secreted by cells varies between cortical areas and species.

**Distribution of Interpatch Angles**

We compared the distribution of angles formed between neighboring patches in our simulations with the distributions measured in biological data. Angles formed between sets of neighbors within the Gabriel graph provide a sensitive statistical measure of the spatial structure inherent in the patch layout. For example, Muir et al. (2011) have used the distribution of interpatch angles to differentiate between artificial sets of points and experimental measurements. We measured this distribution over our simulation results and compared it with data from the primary visual cortex in the cat and macaque monkey (Fig. 4). Our analysis confirms that the spatial arrangement of patches produced by our model matches experimental observations very well. The model distribution was inferred from the same patterns composed of $100 \times 100$ cells that were used to demonstrate the linear scaling relationship in the previous section.

**Robustness of Patchy Patterns to Parameter Variation**

An important condition for the biological plausibility of the pattern formation process is its robustness against parameter variations. We investigated this aspect by assessing the sensitivity of the patchy patterns to the various parameters (diffusion, decay, production, and basal production) of the Gierer–Meinhardt model. For each simulation, we chose a different set of parameters by modifying a template parameter set. This was done as follows: $P = P^0 + \varepsilon_P$, where $P$ is a parameter from the Gierer–Meinhardt model, $P^0$ is the original template parameter before modification, and $\varepsilon_P$ is the modification variable. For each parameter, this modification was drawn from a Gaussian distribution $N(0,\sigma^2)$. The variance $\sigma^2$ of the modification was increased stepwise. For each level of variation, we conducted 10 simulations in MATLAB. To treat all the parameters in the same way, the standard deviation $\sigma$ was chosen to be proportional to the parameter magnitude. This implies that the magnitude of the coefficient of variation $\varepsilon_P = \sigma/\mu$ (where $\sigma$ is the standard deviation and $\mu$ the mean, which is equal to the original parameter magnitude) was the same for all parameters. Our results (Supplementary Fig. 3)
Figure 4. Comparison of the probability density functions of the measured interpatch angles from experimental data of the cat and macaque monkey (blue) and Cx3D simulations (red). Shading corresponds to the 90% confidence interval, as estimated by bootstrap analysis. The distributions are not different according to a 2-sample Kolmogorov–Smirnov test at the 5% significance level.

Figure 5. Self-organized development of a patchy pattern. The initial precursor cell divides in the 2D plane, giving rise to several daughter cells (A: early division phase, B: progressed division phase). Cell division continues until an intracellular concentration reaches a predefined threshold, which stops the cell division. Based on this preplate, the Gierer–Meinhardt reaction–diffusion mechanism leads to a patchy pattern (C). A video of the self-organization of multiple patchy patterns is included in Supplementary Material (Supplementary Movie 5).

**Development From a Single Precursor Cell**

So far, we have assumed that the sheet of cells across which patches are formed is provided externally to our model. Now, we will consider the question whether these systems can develop from a single precursor cell in a self-organizing way. In this case, the whole structure has to develop from rules encoded only in the initial cell. This precursor and all subsequent daughter cells divide in the horizontal plane and give rise to a circularly arranged sheet of cells able to secrete the necessary morphogens.

The simulated developmental process is divided into 2 phases: First, a phase of cell division that produces a sheet of cells by mitotic replication of the mother cell, followed by a phase during which the cells of the sheet secrete the morphogens that control patch formation. These 2 phases are determined by the concentration of an intracellular signaling molecule, produced at a constant rate by each cell. This molecular marker is passed on at each cell division by the molecule, produced at a constant rate by each cell. This secreted signal is necessary for the formation of patches.

The simulations above can explain the emergence of a single, static patch system. However, those simulations use only a single activator–inhibitor pair. Multiple patch systems are possible when multiple pairs are present. Different patch systems develop as a consequence of the separate activator–inhibitor pairs, and if the substances of the activator–inhibitor pairs inhibit each other (Fig. 6A), then patches of the different systems are prevented from emerging at the same location.

The step from single to multiple patch systems is a small one, because the interactions between activator and inhibitor morphogens are unchanged. The developmental cost of increasing the number of patch systems is also low in terms of the extra information required in the genetic code: The code length increases only linearly with the number of patch systems.

We extended the secretion model to permit multiple patch systems by including a term that reduces the activator production in the presence of activator morphogens from other Gierer–Meinhardt systems at the same location (equations 2). High activator levels produce high inhibitor concentrations, and inhibitor substances can also cross-inhibit the activators of other systems. Both mechanisms prevent the patches of different activator–inhibitor systems from appearing at the same location (as for example in Fig. 6B, C).

Experimental data obtained from adjacent injections in inferior temporal (IT) cortex of the macaque monkey suggest that there is very little or no overlap in patch locations.
Topography of Patch Systems

Functional maps, for example maps of orientation selectivity in the visual cortex, are quasi-periodic and have a topographic neighborhood relation (Hubel et al. 1978; Bosking et al. 1997). If we assume similar characteristics for the superficial patch system, then the locations of the patches have to fulfill certain conditions. The targets of projections from nearby neurons should share common features. Neurons that are located close to each other should make target patches in locations that are only slightly offset (Lund et al. 2003; Muir and Douglas 2011; Muir et al. 2011). For example, in a scenario with 3 patch systems (U, V, and W), patches of system U could be on average closer to the patches of system V than to the patches of system W. We investigated how such a topography could be achieved with multiple Gierer–Meinhardt systems that interact with each other.

Our approach is as follows. We assume that there is Gaussian variation in the cellular secretion dynamics. Consequently, some cells have higher production and basal production coefficients than others. This variation is sufficient to predispose some regions to express the high levels of morphogen concentration, so constituting a patch. Therefore, with a sufficiently high variance in the cellular production, the patches of the different activator–inhibitor systems will fall predominantly into the same specific regions that are composed of highly productive cells (Fig. 7B).

The system of equations (2) implies that substances of different Gierer–Meinhardt systems mutually inhibit one another. Figure 7C,D are 2 examples in which the repulsion strength between patch systems varies (red and blue indicate the 2 different systems). The repulsion between the morphogens in Figure 7C is weaker than in D. This is reflected in the distances between the red and blue patches, because the red patches in (C) are usually closer to the blue patches than in the pattern (D). Different mutual repulsion strengths influence the average spacing that will result between patches from different systems. Our simulations indicate that the distance between patch systems is more consistent when the inhibitory morphogen also inhibits the activator production of other types, because the fast diffusion of the inhibitory substance leads to smoother patches. The pattern in Figure 7D was generated by the same model parameters, but with a stronger repulsion parameter r and an additional repulsion from the inhibitory morphogen.

Analogously, one can extend the model to include several types of activators and inhibitors. The set of repulsion coefficients imposes neighborhood relationships between the several patch systems. Theoretically, this kind of topographic relationship could also be imposed by the repulsion coefficients alone, without introducing variance in cellular production coefficients. Cellular inhomogeneity causes the different patch systems to compete for the most productive regions. In addition, cells that produce very little morphogen will not express patches and so will not participate in the superficial patch system. There are several lines of evidence that support the existence of such regions. For example, some locations in the visual cortex, namely the orientation pinwheel centers, do not collectively form long-range projections (Sharma et al. 1995; Yousef et al. 2001; Mariño et al. 2005). An early proposal for the patch system was that neurons in some regions make long-range projections, while

Figure 6. (A) Interactions of 2 Gierer–Meinhardt systems. In addition to the basic antagonism of the activator and inhibitor morphogens (as used in the single-patch system scenario), the activator substances of different Gierer–Meinhardt systems inhibit each other. Sufficiently strong inhibition between different activator morphogens ensures that patches belonging to distinct systems do not overlap. (B) Simulation of 4 interacting patch systems from a Cx3D simulation. Each system is based on 2 morphogens interacting according to the Gierer–Meinhardt model. Red, green, blue, and purple indicate the concentrations of distinct activator substances. Repulsion constants between activators were chosen to be identical for all of the activator pairs. (C) Multiple patch systems defined by inhibitory substances (same simulation as in Fig. 6B). Red, green, blue, and purple indicate the concentrations of distinct inhibitor types. In contrast to the scenario where patches are defined by the activator substance concentration, here, there is a smooth overlap between patches because there is no mutual inhibition between inhibitory substances. Patch systems are still guaranteed to develop at distinct locations, because the different activator substances compete with each other, such that also the patches of the inhibitor concentrations are at different locations.

(Tanigawa et al. 2005). This situation occurs in our model when the mutual inhibition is sufficiently strong. On the other hand, the patches of several patch systems can overlap if, instead of the activator substance, the concentration of the inhibitor substance defines the patches. In this case, the appearance of patches is modified, in 2 ways: They are larger because of the larger diffusion constant (a necessary condition for stationary patterns); and they are smoother because the different inhibitory substances do not directly interact with one another. In this model, cells can exist inside multiple different patch systems. Figure 6C shows the inhibitory morphogen patches from the same pattern as in Figure 6B.
Laminated Structure

Although the overall laminar organization of the patch system is still unclear, the characteristic long-range projections have been observed mainly in the superficial layers. We investigated whether our hypothesis is consistent with patch expression only in specific layers, by simulating the development of a laminated structure with periodic long-range clustered projections in only the superficial layers. We achieved this by following the protomap concept of Rakic (1988). First, the cells of the cortical plate generate a patchy system as described above. If the activator concentration in a cell exceeds a given threshold, it becomes imprinted as belonging to a patch. This model can be extended to multiple patch systems on the same plate, as will be explained later.

All the cells of the initial patterned sheet divide horizontally, so that daughter cells form the next higher sheet (for simplicity we do not model here the detailed process of cortical lamination). Each division of a cell causes the decay of an intracellular laminar signal substance, so allowing the cells to track their radial position. Some of these cells have been imprinted as potential secretors as a result of the earlier Gierer-Meinhardt process, and those that reach layer II/III will secrete the appropriate activator morphogen and so contribute to the formation of a patch. The patchy expression pattern then provides the basis for establishing the appropriate axonal connectivity, as shown in Figure 8.

Axonal Growth Model

With the patchy morphogen concentrations in place, the neurons in other regions may not (Rockland and Lund 1982; Rockland et al. 1982). These points can be explained by our model by incorporating variation in morphogen production efficacy across the cells. As described later, our (simplified) model of axonal growth assumes that the long-range projections are made only from cells that lie inside a patch. Because the regions that are composed of cells with low morphogen production efficacy do not induce patches, these regions do not participate in the superficial patch system.
by intralaminar axonal projections under active guidance of their growth cones. Growth cones follow the concentration gradient of relevant morphogenetic guidance cues, bifurcating recursively as a probabilistic function of the cue concentration (see Materials and Methods for a detailed description of the axonal branching rules). Consequently, laterally extending axons ramify in target patches.

We studied axon growth in the case of single and multiple patch systems. In the first case, the lamina of cells generates only a single global patch system. In this scenario, all (or a randomly selected percentage of) the cells that comprise the cortical sheet extend their axons. The axons follow the gradient of the activator morphogen to grow toward the patches and make their arborizations, leading to the clustered axonal long-range projections shown in Figure 9A.

In the case of multiple patch systems, axons follow the gradients of different morphogens for each patch system. Axonal outgrowth is triggered when a neuronal soma senses a supra-threshold activator concentration, subsequently extending an axon that follows the positive gradient of only this morphogen. This simple rule leads to clustered axonal projections over separate patch systems, as shown in Figure 9B. A video of a simulation implementing this growth rule is included as Supplementary Movie 6.

Additional modifications of the axonal growth patterns could be made in the scenario of multiple patch systems. For example, the patches could be defined by high inhibitor morphogen concentrations, as discussed before. In this case, the target regions of neurons belonging to the different patch systems can overlap. Cells lying in an overlapping location could randomly switch to one of the patch identities before the initiation of neurite outgrowth. This would increase the potential electrophysiological communication between different patch systems (although in the separated patch systems scenario there is no strict boundary, so there can always be communication between different patch systems). Another possible extension that would increase the degree of intercommunication could involve the growth rule itself, so that some additional patch systems could also be connected to one another. For example, neurons in the patches of a patch system U could project to patches belonging to systems U and V, while the patches of system V project to systems U and W. A mathematical analysis of the topology and activity dynamics in different scenarios for the superficial patch system has been performed by Voges et al. (2010).

Our goal here was not to model the detailed biological processes of the growth cone and the resulting morphology, but simply to incorporate principles that lead to patchy connectivity patterns and that match experimental observations (such as the distribution of angles between neighboring patches, addressed in the Results section).

Discussion

We have demonstrated by detailed simulation of neuronal development how the experimentally observed superficial patch system of the neocortex can arise on the basis of the quasi-periodic spatial patterns produced by a Gierer–Meinhardt type reaction–diffusion system. This entire process arises out of the genetic-like specification inserted into a single precursor cell. This progenitor cell undergoes cell division, distributing its genetic instructions to its offspring, who finally give

Figure 9. (A) Development of axonal long-range projections on a single-patch system. Growth cones of randomly selected cells follow the gradient of an extracellular cue secreted by cells located inside the patches. This same cue promotes more dense arborization by increasing the probability of the axon to bifurcate. (1) Initially, cells extend their axons in random directions. The yellowish somata are the strongest producers of the guidance cue. Newly extended axons and their cell bodies are colored red. (2 and 3) The region of high guidance cue concentration (yellow cell bodies) already has denser arborizations. (4) Arborization is triggered when a neuronal soma senses a suprathreshold activator concentration, subsequently extending an axon that follows the positive gradient of only this morphogen. (B) Sequence of axonal growth on multiple patch systems from the pattern in Figure 6B. This axonal growth rule makes use of many patchy patterns generated by the Gierer–Meinhardt model. In contrast to the simpler growth rule with only 1 global patch system, in this case, the location of the soma determines the targeted activator type (different colors indicate different types). Axons that arise from cell bodies lying in a patch will make long-range projections only to the patches of a similar identity. Cell bodies that are not located inside a region of high activator and inhibitor concentration levels make only nonspecific local connections. The specificity of the resulting connections can be controlled by the parameters of the growth model. For example, as mentioned in the Materials and Methods section, the probability to bifurcate is given by

\[ P_{\text{bifurcate}} = u \cdot c_a + v \]

where \( c_a \) is the concentration of the activator substance and \( u, v \) are variable parameters. Large \( v \) increases the probability to branch outside of the patches, leading to less specific connectivity. In the scenario with multiple patch systems, a growth cone could also target activator patches of multiple types with different scaling parameters \( u \), such that the communication between different patch systems is increased. Additionally, the bifurcation could be guided by the inhibitor substance, which increases the overlap between different patch systems (as shown in Fig. 6B,C).
rise to the cortical plate. The individual genetic codes instruct the cells of the plate to secrete a small number of different morphogens. These morphogens have either localized or extensive extracellular diffusion; and they either activate or suppress the production of other morphogens. Overall, these morphogenetic network interactions express Gierer–Meinhardt reaction–diffusion dynamics that converge to a spatial pattern of interlaced hexagonal lattices of similarly labeled (by their morphogen profile) neurons. These labeled neurons then spread radially to become a more superficial layer of neurons and then begin to extend long-range intralaminal axons. The direction of growth of these axons, and their propensity to bifurcation, are determined by the gradient and concentration of their target morphogen. Consequently, axons have a bias to grow toward adjacent regions of like-labeled neurons and to ramify there (Fig. 9), so giving rise to the experimentally observed patchy connectivity.

Overall, our model demonstrates how the patchy connectivity pattern of cortex can construct itself on the basis of only local cell–cell chemical interactions and each cell’s (similar) genetic code, without the support of external, organizing electrical spike patterns.

**Apparently Complex Structure Arising From a Simple Mechanism**

The concept that the complicated spatio-temporal patterns observed in animal morphogenesis could be due to a relatively simple underlying molecular mechanism was proposed by Alan Turing in his seminal paper of 1952. He demonstrated that a suitably constrained interaction between 2 fundamental physical processes—reaction and diffusion—could give rise to many kinds of pattern formation observed in nature. This mechanism is based on the secretion, decay, and diffusion dynamics of different substances that compete for control of their sources. Small random fluctuations in the initial concentrations can lead to global symmetry-breaking and the emergence of stationary spatial “Turing” patterns. Counter-intuitively, symmetry-breaking is driven by diffusion: A necessary condition for the symmetry-breaking is that the diffusion coefficients differ between competing morphogens. Unfortunately, Turing’s original formulation of the reaction–diffusion system is not molecularly plausible, because it allows negative concentrations. However, in 1972, Gierer and Meinhardt proposed the feasible formulation that we have chosen as a basis for simulating spatial organization. Other reaction–diffusion models that are also based on interacting antagonistic morphogens (e.g. the Gray–Scott [Gray and Scott 1983; McGough and Riley 2004] or Schnakenberg model [Schnakenberg 1979; Iron et al. 2004]) may yield similar results.

Grossberg (1976) explored the use of reaction–diffusion systems to model neural map formation. Since then, several reaction–diffusion systems have been used to model the development of neural tissue. For example, Cartwright (2002), Striegel and Hurdal (2009), Lefèvre and Mangin (2010), and Garzón-Alvarado et al. (2011) investigated the problem of the generation of gyri and sulci during cortical development. Other models based on reaction–diffusion dynamics have been used to explain ocular dominance and orientation maps (Swindale 1980; Grossberg and Olson 1994), as well as disparity selectivity (Siddiqui and Bhaumik 2011). All of those models were essentially analytical and so differ from the detailed physical cellular growth simulations that we report here.

**Experimental Support for Reaction–Diffusion Processes**

The relevance of Turing patterns as an explanation of natural morphogenesis, and specifically cortical development, is matter of debate. The mechanism is elegant and appealing, but experimental verification is difficult because it requires not only identification of the different morphogens, but also their in vivo diffusion or cellular reaction constants, data which are very difficult to obtain. Nevertheless, there is substantial circumstantial evidence for the role of reaction-diffusion processes in development. Turing patterns have been confirmed experimentally in chemical reactions (Castets et al. 1990; De Kepper et al. 1991), and there is experimental evidence that these systems play a role in animal development. For example, 2 antagonistic pattern-forming substances have been shown to be involved in the generation of the oral–aboral axis in sea urchins (Duboc et al. 2004), and in mouse hair follicle formation (Mou et al. 2006). It can predict the time evolution of the skin patterns of the angelfish Pomacanthus (Kondo and Asai 1995) and explain head regeneration in the freshwater coelenterate hydra (Gierer and Meinhardt 1972), or stripes on the shells of molluscs (Meinhardt and Klingler 1987).

Morphogens that follow dynamics of the activator–inhibitor type do occur in development. For example, transforming growth factor (TGF)-β signals can act as activator–inhibitor morphogens (Schier 2009), as demonstrated in the zebrafish blastula (Meno et al. 1999; Chen and Schier 2002; Müller et al. 2012). Müller et al. (2012) have shown that the inhibitor has a larger effective diffusion constant than the activator, which is a necessary condition for stationary Turing patterns. There is evidence that TGF-type morphogens have an autocalytic role in vertebrate limb formation (Newman and Bhat 2007). The sonic hedgehog (SHH) signaling molecule, which is involved in various pattern formation mechanisms in the central nervous system, acts together with fibroblast growth factor as an activator–inhibitor system that is responsible for the formation of ridges in the mammalian palate (Economou et al. 2012). The WNT/bone morphogenetic protein activator–inhibitor pair has been implicated in hair and feather follicle development (Sick et al. 2006; Plikus et al. 2011). Other possible candidates of morphogens are Semaphorins (Matsuoka et al. 2011). Moreover, these morphogens have been shown to act also as guidance cues (Webber et al. 2003; Schnorrer and Dickson 2004; Charron and Tessier-Lavigne 2007; Zou and Lyuksyutova 2007; Sánchez-Camacho and Bovolenta 2009; Gordon et al. 2010).

It is difficult to estimate the parameter values of the morphogenetic substances in our simulations, because these values depend also on assumptions concerning somatic diameter, density of morphogen producing cells, computation of diffusion, etc. Consequently, we have not assigned units to the parameters. However, we are able to make qualitative estimates, such as the proportions that some coefficients have with respect to one another. For example, the inhibitor diffusion coefficient is approximately 3 orders of magnitude larger than the activator diffusion coefficient. The decay rate of the inhibitor substance in our simulations was always larger than the rate of the activator, by about a factor of two.
**Agreement with Experimental Data, and Concepts of Cortical Organization and Development**

The spatial patterns produced by our model are in good agreement with experimental observations, such as the remarkable observation of the linear relationship between patch diameter and spacing across cortical areas and species (Lund et al. 1993; Binzegger et al. 2007; Muir et al. 2011). It also exhibits the correct distribution of angles between neighboring patches (Muir et al. 2011). Differences in the morphogen production coefficients in the different cortical areas and species are the only assumptions required to explain this intriguing relationship. Our hypothesis could be confirmed by identifying and modifying the cellular secretion efficacies of the hypothetical morphogens.

Our reaction–diffusion model is consistent with Rakic’s protomap concept (Rakic 1988), which is likely a central organizing principle of the much disputed “cortical column” (Mountcastle 1957; Hubel and Wiesel 1977; da Costa and Martin 2010). Postmitotic cells, by their migration outwards along the radial glial cells and their formation of the cortical lamination, project the patch lattice columnwise out of the 2-dimensional neural plate. Several studies provide evidence for this similar ontogenetic unity along the radial dimension (Luskin et al. 1989; Kornack and Rakic 1995; Rakic 1995), which can be seen in the laminar organization of the patch system (Rockland 1985; Galuske and Singer 1996; Angelucci and Sainsbury 2006).

Of course, the original protomap hypothesis was made in the context of the rodent brain, and there is evidence that the superficial patch system does not exist in rodents (Van Hooser et al. 2006; Muir and Douglas 2011). However, the important principle here is that organizational patterns laid down in the ventricular zone propagate radially and are elaborated in the developing cortical laminations (Kennedy and Dehay 1993). The reason why certain species do exhibit patchy connectivity may be due to the combinations of production and diffusion rates in vivo that do not fulfill the conditions for stationary hexagonal patterns.

It remains unknown whether the superficial patches reflect a single lattice, or whether there are several distinct or overlapping patch systems (Muir and Douglas 2011). Studies based on adjacent injections using multiple tracers point in the direction of multiple patch systems (Matsubara et al. 1987; Tanigawa et al. 2005). Tanigawa et al. (2005) used adjacent injections of multiple tracers to demonstrate that intra-areal long-range projections cluster at nonoverlapping locations. Our simulations show that nonoverlapping and partially overlapping patch systems can be easily realized with multiple interacting Gierer–Meinhardt systems. In this scenario, the regions targeted by an axon depend on the location of it’s soma: Somata located in a given patch extend axons only toward patches belonging to the same system. We have also shown that patches in our model can overlap, if the patch identity is conferred by the concentration of the inhibitor substance.

These anatomical results offer a link to features of functional maps [periodicity and topographic mapping, described for example by Mitchison and Crick (1982) and Bosking et al. (1997)]. For example, the orientation tuning of neurons inside connected patches tends to be similar (Bosking et al. 1997; Schmidt et al. 1997). Further work in this direction could investigate how the transitions between patches of different reaction–diffusion systems could provide a scaffold for establishing the connectivity of functional maps such as orientation selectivity.

There is also evidence for a relationship between the patch system and metabolically derived patterns. For example, cytochrome oxidase–reactive regions and the superficial patch system share some features (Rockland and Lund 1983; Muir and Douglas 2011; Muir et al. 2011). We did not address ocular dominance columns or cytochrome-oxidase (CO) blobs in this work, because they stem from thalamocortical projections, and we restrict ourselves to corticocortical connections. However, it is intriguing that CO blobs in the cat visual cortex can develop in the absence of visual input (Murphy et al. 2001), raising the possibility that molecular markers such as those used in our model are involved in patterning geniculocortical afferents. Bressloff and Oster (2010) have studied just this scenario, using a patchy scaffold of markers which modulate synaptic plasticity and promote the formation of ocular dominance columns. Our work complements their model since it provides an explanation for the development of this periodic specification.

**Axonal Arborization Patterns**

The orderly axonal projection patterns depend on simple and biologically plausible axonal growth rules, which make use of morphogen concentration profiles for targeting arborization locations over long distances. This direct sensitivity to an organizational signal makes the arborization quite specific, rather than having an initial widespread exuberance of projections followed by pruning (Callaway and Katz 1990).

Importantly, in our model, axonal outgrowth and organization do not depend on electrical signaling that has particular sensory statistics (as for example proposed by Grabska-Barwińska and von der Malsburg (2008), suggesting that activity waves and locally periodic response patterns shape the connectivity). Electrical signaling might be required for refinement of the crude clusters established at the early developmental stage. This does not contradict the experiments of Ruthazer and Stryker (1996), where suppression of spiking activity using the sodium channel blocker tetrodotoxin prevented the formation of clustered long-range projections in the ferret. We argue that electrical activity might be permissive rather than instructive, with growth at the very early stages of development based on the intrinsic pattern, so accounting for the presence of the superficial patch system in cortical areas that are remote from the potential organizing properties of sensory afferents.

There is indeed evidence that neural activity has a large impact on axonal branching (Uesaka et al. 2006). In this vein, it has been shown in the cat visual cortex that at the very early stages of connectivity development, long-range intra-areal projections are not yet clustered (Price 1986; Callaway and Katz 1990). Only at the end of the second postnatal week is extensive clustering observed. Our interpretation of these data is that axonal outgrowth is under the control of a 2-step process. Axons initially search for their target patches without extensive ramification. A subsequent axonal cluster-forming process is invoked only when an axon finds a suitable target region and the appropriate electrical activity conditions are met. Due to retinal waves and recurrent thalamocortical loops, animals are exposed to relatively
structured activity possibly very early in development, which could provide enough correlation structure for Hebbian mechanisms to play a role (Wong 1999; Welisky and Hall 2000; Butts 2002; Huberman et al. 2008). Studies in other species also show that a crude form of the patch system is present at very early stages. In the ferret patches develop before eye opening (Durack and Katz 1996); and in macaque monkey, the system can even be observed prenatally (Coogan, Van Essen, et al. 1996). Consequently, we predict that as long as the branching and axon guidance machinery is not affected, disturbance of the pattern of electrical input to the neurons will not abolish the development of the superficial patch system. This has been shown to be the case for retinal activity (Callaway and Katz 1991; Ruthazer and Stryker 1996).

Simulations of Cellular Processes in Physical 3D Space
The simulation methods used in the paper demonstrate a substantial advance in computational neuroscience. In classical mathematical models, the environment is abstracted as a regular 2-dimensional grid in which each discrete element of space participates in both diffusion and reaction. In our work, we have simulated the behavior of physical cells, behaving in a physically realistic 3D space. Each cell is an independent agent able to interact only with its local environment; there is no global organizer. Such physical simulations in Cx3D (for example) offer a novel and powerful tool for the investigation of anatomical and developmental processes that is likely to be at least as influential as the theoretical electrophysiological investigations performed in simulators such as NEURON (Hines and Carnevale 1997). Of course, dense multiagent simulations such as ours come with a high computational cost and also bring some interesting new questions. One of these, relevant to the present paper, is the question of stability.

Turing patterns have been shown to be very robust against noise (Pena and Perez-Garcia 2001; Leppänen et al. 2003). This robustness is especially important in a biological context, because there is inherent variation in the cellular secretion. We have shown that Turing patterns that emerge in our simulations are stable to disturbances, noise or the initial distribution of morphogen concentrations. However, it is not only the stability of the reaction–diffusion system that is at issue here. It is important to note that the developmental process arises by the cell division from a precursor, in which only local morphogenetic production rules and axonal growth rules are specified. Thus, overall stability of the patchy lattice depends also on the developmental strategy (Zubler et al. 2011) in which the reaction–diffusion processes are embedded.

Our goal in this paper was to describe only the principles of developmental construction of the patch system, rather than attack the more difficult problem of how these principles play out when embedded in a detailed simulation of cortical development. However, we have previously shown (Zubler and Douglas 2009) how to produce a laminated cortical structure in an unprepared environment, and how to make layer specific branching patterns in Cx3D. It remains to bring these 2 lines of work together, to demonstrate how the patchy protomap promotes columnar organization of inter- and intralaminar connections in the context of a large-scale simulation of cortical development, a task in which we are presently engaged.

Conclusion
In the modern interdisciplinary approach to neuroscience, theoretical models and their simulation, such as we present here, complement experimental neuroscience in 2 important ways: They explore and they explain. Our model explores implications of the assumption that the development of the general and rather complex patterning of the cortical patch system depends on a simple underlying molecular mechanism: The presence of a cooperative–competitive interaction of the morphogen secretion between cells. Of course, we have not yet confirmed the existence of the crucial proposed cooperative–competitive morphogens. We have, however, presented evidence from the literature for the probable existence of such substances. And our simulations have shown how, on the basis of this simple assumption, the model is able to explain a wide variety of experimental observations such as the occurrence of the patches, their spatial distribution, their linear scaling over areas and species, and their independence (initially) of electrical activity in well-formed neuronal circuits that occur only later in development. Our model also explains how this process can unfold from a single precursor cell, so demonstrating how complex organization of connections could be simply genetically encoded. Importantly, our simulations are of physical cells in a physically realistic environment, in which cells act as individual agents able to interact only with their local environment. This means that our results extend beyond the ideal of mathematical models, toward what is physically realizable in biology and future technology.

Supplementary Material
Supplementary material can be found at: http://www.cercor.oxfordjournals.org/

Funding
This work was supported by European Union Project grant FP7-216593 “SECO.” Funding to pay the Open Access publication charges for this article was provided by the Institute of Neuroinformatics, UZH/ETH Zürich.

Notes
The authors thank Michael Pfeiffer, Ueli Rutishauser, Adrian Whatley, Matthew Cook, Kevan Martin, Elisha Ruesch, Jiri Kriz, and Boris Wrobel for valuable feedback and for the very supportive critical readings of the manuscript. Conflict of Interest: None declared.

References


da Costa N, Martin K. 2010. Whose cortical column would that be? Front Neuroanat. 4:16.


