Prediction of protein solvent accessibility using fuzzy k-nearest neighbor method

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ABSTRACT

Motivation: The solvent accessibility of amino acid residues plays an important role in tertiary structure prediction, especially in the absence of significant sequence similarity of a query protein to those with known structures. The prediction of solvent accessibility is less accurate than secondary structure prediction in spite of improvements in recent researches. The k-nearest neighbor method, a simple but powerful classification algorithm, has never been applied to the prediction of solvent accessibility, although it has been used frequently for the classification of biological and medical data.

Results: We applied the fuzzy k-nearest neighbor method to the solvent accessibility prediction, using PSI-BLAST profiles as feature vectors, and achieved high prediction accuracies. With leave-one-out cross-validation on the ASTRAL SCOP reference dataset constructed by sequence clustering, our method achieved 64.1% accuracy for a 3-state (buried/intermediate/exposed) prediction (thresholds of 9% for buried/intermediate and 36% for intermediate/exposed) and 86.7, 82.0, 79.0 and 78.5% accuracies for 2-state (buried/exposed) predictions (thresholds of each 0, 5, 16 and 25% for buried/exposed), respectively. Our method also showed slightly better accuracies than other methods by about 2–5% on the RS126 dataset and a benchmarking dataset with 229 proteins.

Availability: Program and datasets are available at http://biocom1.ssu.ac.kr/FKNNacc/

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INTRODUCTION

Predicting the three-dimensional (3D) structure of a protein from its sequence is an important issue because the gap between the enormous number of protein sequences and the number of experimentally determined structures has increased (Rost and Sander, 1994; Thompson and Goldstein, 1996). However, the prediction of the complete 3D structure of a protein is still a big challenge, especially in the case where there is no significant sequence similarity of a query protein to those with known structures (Ginalski and Rychlewski, 2003; John and Sali, 2004; Moult et al., 2003; Sander and Schneider, 1991). The prediction of solvent accessibility and secondary structure has been studied as an intermediate step for predicting the tertiary structure of proteins, and the development of knowledge-based approaches has helped to solve these problems (Cuff and Barton, 2000; Frishman and Argos, 1997; Jones, 1999; Przybylski and Rost, 2002; Wohlfahrt et al., 2002).

Secondary structures and solvent accessibilities of amino acid residues give a useful insight into the structure and function of a protein (Eyal et al., 2004; Russell et al., 2003; Totrov, 2004; Wohlfahrt et al., 2002). In particular, the knowledge of solvent accessibility has assisted alignments in regions of remote sequence identity for threading (Rost and Sander, 1994; Rost et al., 1997). However, in contrast to the secondary structure, there is no widely accepted criterion for classifying the experimentally determined solvent accessibility into a finite number of discrete states such as buried, intermediate and exposed states. Also, the prediction accuracies of solvent accessibilities are lower than those for secondary structure prediction, since the solvent accessibility is less conserved than secondary structure (Rost and Sander, 1994), although there has been some progress recently.

The prediction of solvent accessibility, as well as that of the secondary structure, is a typical pattern classification problem. The first step for solving such a problem is the feature extraction, where the important features of the data are extracted and expressed as a set of numbers, called feature vectors. The performance of the pattern classifier depends crucially on the judicious choice of the feature vectors. In the case of the solvent accessibility prediction, using evolutionary information such as multiple sequence alignment and position-specific scoring matrix generally has given good prediction results (Gianese et al., 2003; Pei and Grishin, 2004). Once an appropriate feature vector has been chosen, a classification algorithm is used to partition the feature space into disjoint regions with decision boundaries. The decision boundaries are determined using feature vectors of a reference sample with known classes, which are also called the reference dataset or training set. The class of a query data is then assigned depending on the region it belongs to.

Various classification algorithms have been developed. Bayesian statistics is a parametric method where the functional form of the probability density is assumed for each class, and its parameters are estimated from the reference data. In nonparametric methods, no specific functional form for the probability density is assumed. There are various nonparametric methods such as, for example, neural networks, support vector machines and nearest neighbor methods. In the neural network
methods, the decision boundaries are set up before the prediction using a training set. Support vector machines are similar to neural networks in that the decision boundaries are determined before the prediction, but in contrast to neural network methods where the overall error function between the predicted and observed class for the training set is minimized, the margin in the boundary is maximized.

In the k-nearest neighbor method, the decision boundaries are determined implicitly during the prediction, where the prediction is performed by assigning the query data the class most frequently represented among the k-nearest reference data. The standard k-nearest neighbor rule is to place equal weights on the k-nearest reference data for determining the class of the query, but a more general rule is to use weights proportional to a certain power of distance. Also, by assigning the fuzzy membership to the query data instead of a definite class, one can estimate the confidence level of the prediction. The method employing these more general rules is called the fuzzy k-nearest neighbor method (Keller et al., 1985; see Methods section for details).

Neural network methods are very popular and have been widely used for solving accessibility prediction (Adamczak et al., 2004; Ahmad and Gromiha, 2002; Ahmad et al., 2003; Cuff and Barton, 2000; Pollastri et al., 2002; Rost and Sander, 1994), and support vector machines, a recently developed method, shows comparable results to neural network methods (Kim and Park, 2004; Yuan et al., 2002; Yuan and Huang, 2004). Bayesian statistics has also been used by Thompson and Goldstein (1996).

The k-nearest neighbor method has been frequently used for the classification of biological and medical data, and despite its simplicity, the performances are competitive compared to many other methods. However, the k-nearest neighbor method has never been applied for predicting solvent accessibility, although it has been used to predict protein secondary structure (Salamov and Solovyev, 1995, 1997; Salzberg and Cost, 1992; Yi and Lander, 1993).

In this work, we apply the fuzzy k-nearest neighbor method to the prediction of solvent accessibility where PSI-BLAST (Altschul et al., 1997) profiles are used as the feature vectors. We obtain relatively high accuracy on various benchmark tests.

**MATERIALS AND METHODS**

**Definition and thresholds of solvent accessibility**

Amino acid solvent accessibility is the degree to which a residue in a protein is accessible to a solvent molecule. The relative solvent accessibility can be calculated by dividing the DSSP accessibility (Kabsch and Sander, 1983) by the maximum accessibility of amino acid residues (Rost and Sander, 1994) corresponding to the accessibility for a Gly-X-Gly extended tripeptide conformation.

Various thresholds have been used to classify residues as buried (B) and exposed (E) (2-state prediction) or buried (B), intermediate (I) and exposed (E) (3-state prediction) in previously published results. In this paper, thresholds of 9% for B/I and 36% for I/E (9%; 36% thresholds) in the 3-state prediction and thresholds of 0, 5, 16 and 25% for B/E in the 2-state predictions are used.

**Feature vector and distance measure**

PSI-BLAST (Altschul et al., 1997) generates the profile of a protein in the form of a $20 \times N$ position-specific scoring matrix, where $N$ is the length of the sequence. PSI-BLAST is run with default options ($\sim J 3$ $-h 0.001$ $-e 10.0$) and the non-redundant protein sequence database (ftp://ncbi.nlm.nih.gov/blast/db) filtered by PFILT (Jones, 1999) to mask out regions of low complexity sequence, the coiled coil regions and transmembrane spans. The BLOSUM62 (Henikoff and Henikoff, 1992) substitution matrix is used for PSI-BLAST.

We construct a window of size 15 centered on a target residue (Jones, 1999; Kim and Park, 2004; Yuan et al., 2002), and use the profile that falls within this window, a $15 \times 20$ matrix, as a feature vector. Then, the distance between two feature vectors $A$ and $B$ is defined as

$$D_{AB} = \sum_{i,j} W_i |P_{ij}^A - P_{ij}^B|$$

where $P_{ij}^A (i = 1, 2, \ldots, 15; j = 1, 2, \ldots, 20)$ is a component of the feature vector $A$, and $W_i$ is a weight parameter. Since we expect the profile elements for residues nearer to the target residue to be more important in determining the local environment of the target residue, we use weights $W_i = (8 - |8 - i|)^2$.

**Reference dataset for predictions**

A reference dataset was constructed by clustering the protein chains in ASTRAL SCOP (version 1.63) chain-select-90 subset (Brenner et al., 2000). Since ASTRAL SCOP provides only three kinds of chain sequence sets (100, 95 and 90% sequence identity), we used BLASTCLUST (NCBI BLAST 2.2.5, http://www.ncbi.nlm.nih.gov/BLAST/) for sequence clustering to make a non-redundant dataset. BLASTCLUST was run with 25% sequence identity option ($-S 25$) over an area covering 90% of the length ($-L 0.9$). We also removed the proteins equal or shorter than 50 residues, and excluded unusual residues or those corresponding to chain breaks. The first protein was selected from each cluster and placed in the reference dataset. Therefore no two proteins have more than 25% sequence identity in the dataset. The dataset clustered with the $-L 0.9$ option is a more stringent non-redundant set than datasets constructed by normal pairwise sequence identity. The sequence clustering with the option of $-L 1.0$ in BLASTCLUST is similar to that based on normal pairwise matches. The resulting reference dataset consists of 3644 non-redundant proteins with 854 876 feature vectors.

**The RS126 set and the dataset with 229 proteins**

The solvent accessibility was predicted for two sets of proteins in order to evaluate the performance of our method. In the first test, the protein residues in the RS126 dataset (Rost and Sander, 1994) were used as queries. The proteins in the RS126 dataset have less than 25% pairwise sequence identity. This set was used to evaluate different methods of solvent accessibility prediction, for example, PHDacc (Rost and Sander, 1994) and other methods (Kim and Park, 2004; Thompson and Goldstein, 1996; Yuan et al., 2002). For a rigorous benchmark test, the chains of the reference dataset and the RS126 dataset were split into domains according to the SCOP annotation, and the chains that have any domain with >25% identity to those of the RS126 dataset were excluded from the reference dataset. The resulting set consisted of 3460 proteins with 819 090 feature vectors, which was used as the reference dataset for the benchmark test on the RS126 dataset.

The second set of query proteins was constructed from newly added proteins, >50 residues, in the 90% identity chain set of the ASTRAL SCOP (version 1.65). We removed from the test set the chains having domains with >25% sequence identity to those of the reference dataset. We also removed one of the chains for any pair in the dataset containing domains with >25% sequence identity. The resulting set consisted of 229 protein chains that had <25% sequence identity with the reference dataset and with each other.

**Algorithm**

The nearest neighbor algorithm is a simple classification algorithm; a query data is classified according to the classification of the nearest neighbor from a database of known classifications, i.e. a reference dataset. A natural generalization of the nearest neighbor algorithm is the so-called k-nearest neighbor algorithm, where the k-nearest samples are selected and the query data is assigned the class most frequently represented among them. A further extension is to weight the k-nearest samples with a certain power of the distance.
from the query data. Also, instead of assigning a definite class to the query data, one can calculate the fuzzy membership (see below), which can be used to estimate the confidence level of the prediction. The algorithm incorporating these generalizations is called the fuzzy k-nearest neighbor algorithm (Keller et al., 1985).

Despite its simplicity, nearest neighbor methods can give competitive performance compared to many other methods. The nearest neighbor methods have been used to predict protein secondary structure (Salamov and Solovyev, 1995, 1997; Salzberg and Cost, 1992; Yi and Lander, 1993) and classify biological and medical data (Kaufmann and Jurs, 2001; Singh et al., 1996; Vaidyanathan et al., 1997). Also it has been reported that performances of classification were improved by using fuzzy k-nearest neighbor algorithms (Bezdek et al., 1993; Cabello et al., 1991; Huang and Li, 2004; Leszczynski et al., 1999; Seker et al., 2003; Sokolowska et al., 2003). However the k-nearest neighbor method has never been used to predict protein solvent accessibility.

In this work, we apply the fuzzy k-nearest neighbor method to the solvent accessibility prediction. In the fuzzy k-nearest neighbor method, the fuzzy class membership ui(x) to the class i is assigned to the query data x according to the following equation:

\[ u_i(x) = \sum_{j=1}^{m} \frac{u_i(x^{(j)})D_j^{2/(m-1)}}{\sum_{j=1}^{m} D_j^{2/(m-1)}}, \quad i = 1, \ldots, c, \]

where \( m \) is a fuzzy strength parameter, which determines how heavily the distance is weighted when calculating each neighbor’s contribution to the membership value, \( k \) is the number of nearest neighbors, and \( c \) is the number of classes. Also, \( D_j \) is the distance between the feature vector of the query data \( x \) and the feature vector of its \( j \)-th nearest reference data \( x^{(j)} \), and \( u_i(x^{(j)}) \) is the membership value of \( x^{(j)} \) to the \( i \)-th class, which is 1 if \( x^{(j)} \) belongs to the \( i \)-th class, and 0 otherwise. The advantage of the fuzzy k-nearest neighbor algorithm over the standard k-nearest neighbor method is quite clear. The fuzzy class membership \( u_i(x) \) can be considered as the estimate of the probability that the query data belongs to class \( i \), and provides us with more information than a definite prediction of the class for the query data. Moreover, the reference samples which are closer to the query data are given more weights, and an optimal value of \( m \) can be chosen along with that for \( k \), in contrast to the standard k-nearest neighbor method with a fixed value of \( 2/(m-1) = 0 \). In fact, the optimal value of \( k \) and \( m \) are found from the leave-one-out cross-validation procedure (see Results section), and the resulting value for \( 2/(m-1) \) is indeed nonzero.

**Performance measures**

In this work, two measures are used to evaluate the performance of prediction methods. One is the accuracy, the percentage of correctly classified residues, and the other is the Matthew’s correlation coefficients (MCC). These measures can be calculated by the following equations:

\[
\text{accuracy} = \frac{\sum p_{ij}}{N},
\]

\[
\text{MCC}_{ij} = \frac{p_{ij}n_{ij} - o_{ij}u_{ij}}{\sqrt{(p_{ij} + o_{ij})(p_{ij} + u_{ij})(o_{ij} + u_{ij})(n_{ij} + u_{ij})}},
\]

where \( N \) is the total number of residues, and \( c \) is the class number. Also, \( p_{ij}, n_{ij}, o_{ij}, \) and \( u_{ij} \) are the number of true positives, true negatives, false positives and false negatives for class \( i \), respectively. The MCCs have the same value for the two classes in the case of the 2-state prediction, i.e., MCC_0 = MCC_1.

**Implementation of fuzzy k-nearest neighbor algorithm**

The program implementing the fuzzy k-nearest neighbor algorithm for protein solvent accessibility prediction was written in ANSI C and run on a Linux machine with the CPU of AMD Athlon MP2400. It occupies 69 MB of disk space including the reference data. The prediction program has two running modes: a normal mode and a fast mode. The normal mode generates the feature vectors from the PSI-BLAST profiles of the reference dataset whenever it calculates the distance between two feature vectors. It requires the execution time of 8.1 s per query residue on average and 69 MB memory. In the fast mode feature vectors are loaded in memory all at once in the beginning. It takes 4.7 s to predict the solvent accessibility of a query residue.

**RESULTS AND DISCUSSION**

**Prediction accuracy of the fuzzy k-nearest neighbor method of leave-one-out cross-validation**

First, leave-one-out cross-validation on the ASTRAL SCOP dataset of 3644 proteins (see Methods section) was performed, where we...
Table 1. The optimal values of the fuzzy parameter \(m\), the number of nearest neighbors \(k\) and the corresponding prediction accuracies of leave-one-out cross-validation on the reference dataset derived from ASTRAL SCOP.

<table>
<thead>
<tr>
<th>Fuzzy k-NN</th>
<th>State threshold (%)</th>
<th>3-state (9%; 36%)</th>
<th>2-state (0%)</th>
<th>2-state (5%)</th>
<th>2-state (16%)</th>
<th>2-state (25%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>m</td>
<td>1.33</td>
<td>1.5</td>
<td>1.25</td>
<td>1.29</td>
<td>1.33</td>
<td></td>
</tr>
<tr>
<td>k</td>
<td>65</td>
<td>40</td>
<td>75</td>
<td>65</td>
<td>65</td>
<td></td>
</tr>
<tr>
<td>Accuracy</td>
<td>64.1</td>
<td>86.7</td>
<td>82.0</td>
<td>79.0</td>
<td>78.5</td>
<td></td>
</tr>
<tr>
<td>MCC</td>
<td>B:0.577, I:0.245, E:0.528</td>
<td>0.464&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.564&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.578&lt;sup&gt;a&lt;/sup&gt;</td>
<td>0.570&lt;sup&gt;a&lt;/sup&gt;</td>
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</table>

Standard k-NN \((m = \infty)\)

| k          | 35                  | 15               | 20          | 20          | 30           |              |
| Accuracy   | 61.2                | 85.8             | 80.2        | 77.3        | 76.9         |              |
| MCC        | B:0.534, I:0.180, E:0.496 | 0.414<sup>a</sup> | 0.521<sup>a</sup> | 0.542<sup>a</sup> | 0.533<sup>a</sup> |

<sup>a</sup>For the 2-state predictions, the MCC values are the same for the two classes, i.e. MCC<sub>B</sub> = MCC<sub>E</sub>.

Table 2. The prediction results on the RS126 dataset.

<table>
<thead>
<tr>
<th>Fuzzy k-NN</th>
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<tr>
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<tr>
<td>Fuzzy k-NN</td>
<td>63.8</td>
</tr>
<tr>
<td>PHDacc</td>
<td>57.5</td>
</tr>
<tr>
<td>SVMpsi</td>
<td>59.6</td>
</tr>
<tr>
<td>Thompson and Goldstein</td>
<td>57.9</td>
</tr>
</tbody>
</table>

<sup>NN means nearest neighbors. PHDacc (Rost and Sander, 1994) used neural networks, SVMpsi (Kim and Park, 2004) was based on support vector machines, and Thompson and Goldstein (1996) applied Bayesian statistics for the solvent accessibility prediction on the RS126 dataset. These accuracies are from their published results.</sup>
Table 3. The prediction results on the benchmarking dataset with 229 proteins

<table>
<thead>
<tr>
<th></th>
<th>State threshold</th>
<th>3-state (9%; 36%)</th>
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<tr>
<td>Accuracy (%)</td>
<td>62.6</td>
<td>85.5</td>
<td>80.8</td>
<td>78.1</td>
<td>77.8</td>
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<td>PHDacc</td>
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<tr>
<td>Accuracy (%)</td>
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<tr>
<td>MCC B</td>
<td>0.560</td>
<td>1.0.199</td>
<td>0.0.508</td>
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<td>0.541</td>
<td>0.560</td>
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<tr>
<td>MCC I</td>
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<tr>
<td>MCC E</td>
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*PHDacc and PROFacc results were obtained from PredictProtein Server (http://cubic.bioc.columbia.edu/pp/index.html), and Jpred results were obtained from Jpred server (http://www.compbio.dundee.ac.uk/~www-jpred/). The predictions with PredictProtein Sever and Jnet were performed with default options.

and Jpred (http://www.compbio.dundee.ac.uk/~www-jpred/) were performed with default options. It should be noted that any query protein has <25% sequence identity with those in the reference dataset in our method, whereas no such restriction was placed on the sequence similarity between the query protein and training set in other methods. Therefore, our method has no advantage over other methods in this respect. However, it should also be admitted that the other methods were trained on a much smaller dataset, and database growth can give an indirect advantage to newer methods (Przybylski and Rost, 2002) like ours.

The prediction accuracies of our method are slightly better than other methods on the benchmarking dataset with 229 proteins, as shown in Table 3. For the 3-state prediction (9%; 36% thresholds), PHDacc and PROFacc give 57.1 and 62.0% accuracies, and our method gives a 62.6% accuracy. For the 2-state predictions (thresholds of 0, 5 and 25%), Jpred shows 84.8, 80.7 and 77.6% prediction accuracies, and our method shows slightly better prediction accuracies of 85.5, 80.8 and 77.8%, respectively. Our result is better also in terms of MCCs as shown in Table 3.

## CONCLUSION

In this work, we applied the fuzzy k-nearest neighbor method to solvent accessibility prediction, using PSI-BLAST profiles as feature vectors. We achieved better prediction accuracies than other methods such as neural network methods and support vector machines.

## ACKNOWLEDGEMENTS

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