Biological network comparison using graphlet degree distribution

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ABSTRACT

Motivation: Analogous to biological sequence comparison, comparing cellular networks is an important problem that could provide insight into biological understanding and therapeutics. For technical reasons, comparing large networks is computationally infeasible, and thus heuristics, such as the degree distribution, clustering coefficient, diameter, and relative graphlet frequency distribution have been sought. It is easy to demonstrate that two networks are different by simply showing a short list of properties in which they differ. It is much harder to show that two networks are similar, as it requires demonstrating their similarity in all of their exponentially many properties. Clearly, it is computationally prohibitive to analyze all network properties, but the larger the number of constraints we impose in determining network similarity, the more likely it is that the networks will truly be similar.

Results: We introduce a new systematic measure of a network’s local structure that imposes a large number of similarity constraints on networks being compared. In particular, we generalize the degree distribution, which measures the number of nodes ‘touching’ $k$ edges, into distributions measuring the number of nodes ‘touching’ $k$ graphlets, where graphlets are small connected non-isomorphic subgraphs of a large network. Our new measure of network local structure consists of 73 graphlet degree distributions of graphlets with 2–5 nodes, but it is easily extendible to a greater number of constraints (i.e. graphlets), if necessary, and the extensions are limited only by the available CPU. Furthermore, we show a way to combine the 73 graphlet degree distributions into a network ‘agreement’ measure which is a number between 0 and 1, where 1 means that networks have identical distributions into a network ‘agreement’ measure which is a number between 0 and 1, where 1 means that networks have identical distributions and 0 means that they are far apart. Based on this new network agreement measure, we show that almost all of the 14 eukaryotic PPI networks, including human, resulting from various high-throughput experimental techniques, as well as from curated databases, are better modeled by geometric random graphs than by Erdős–Rény, random scale-free, or Barabási–Albert scale-free networks.

Availability: Software executables are available upon request.

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1 INTRODUCTION

Understanding cellular networks is a major problem in current computational biology. These networks are commonly modeled by graphs (also called networks) with nodes representing biomolecules such as genes, proteins, metabolites, etc., and edges representing physical, chemical, or functional interactions between the biomolecules. The ability to compare such networks would be very useful. For example, comparing a diseased cellular network to a healthy one may aid in finding a cure for the disease, and comparing cellular networks of different species could enable evolutionary insights. A full description of the differences between two large networks is infeasible because it requires solving the subgraph isomorphism problem, which is an NP-complete problem.

Therefore, analogous to the BLAST heuristic (Altschul et al., 1990) for biological sequence comparison, we need to design a heuristic tool for the full-scale comparison of large cellular networks (Berg and Lassig, 2004). The current network comparisons consist of heuristics falling into two major classes: (1) global heuristics, such as counting the number of connections between various parts of the network, and (2) local heuristics that measure relative distance between concentrations of small subgraphs (called graphlets) in two networks (Pržulj et al., 2004).

Since cellular networks are incompletely explored, global statistics on such incomplete data may be substantially biased, or even misleading with respect to the (currently unknown) full network. Conversely, certain neighborhoods of these networks are well-studied, and so locally based statistics applied to the well-studied areas are more appropriate. A good analogy would be to imagine that MapQuest knew details of the streets of New York City and Los Angeles, but had little knowledge of highways spanning the country. Then, it could provide good driving directions inside New York or Los Angeles, but not between the two. Similarly, we have detailed knowledge of certain local areas of biological networks, but data outside these well-studied areas are currently incomplete, and so global statistics are likely to provide misleading information about the biological network as a whole, whereas local statistics are likely to be more valid and meaningful.

Owing to the noise and incompleteness of cellular network data, local approaches to analyzing and comparing cellular network structure that involve searches for small subgraphs have been successful in analyzing, modeling, and discovering functional modules in cellular networks (Milo et al., 2002, 2004; Shen-Orr et al., 2002; Pržulj et al., 2004). Note that it is easy to show that two networks are different simply by finding any property in which they differ. However, it is much difficult to show that they are similar, since it involves showing that two networks are similar with respect to all of their properties. Current common approaches to show network similarity are based on listing several common properties, such as the degree distribution, clustering, diameter, or relative graphlet frequency distribution. The larger the number of common properties, the more likely it is that the two networks are similar. But any short list of properties can easily be mimicked by two very large and different networks. For example, it is easy to construct networks with exactly the same degree distribution whose structure and function differ substantially (Pržulj et al., 2004; Li et al., 2005; Doyle et al., 2005).

In this article, we design a new local heuristic for measuring network structure that is a direct generalization of the degree distribution. In fact, the degree distribution is the first in the spectrum of 73 graphlet degree distributions that are components of this
new measure of network structure. Thus, in our new network similarity measure, we impose 73 highly structured constraints in which networks must show similarity to be considered similar; this is a much larger number of constraints than provided by any of the previous approaches and, therefore, it increases the chances that two networks are truly similar if they are similar with respect to this new measure. Moreover, the measure can be easily extended to a greater number of constraints simply by adding more graphlets. The extensions are limited only by the available CPU.

Based on this new measure of structural similarity between two networks, we show that the geometric random graph model shows exceptionally high agreement with 12 out of 14 different eukaryotic protein–protein interaction (PPI) networks. Furthermore, we show that such high structural agreements between PPI and geometric random graphs are unlikely to be beaten by another random graph model, at least under this measure.

### 1.1 Background

Large amounts of cellular network data for a number of organisms have recently become available through high-throughput methods (Ito et al., 2000; Uetz et al., 2000; Giot et al., 2003; Li et al., 2004; Stelzl et al., 2005; Rual et al., 2005). Statistical and theoretical properties of these networks have been extensively studied (Jeong et al., 2000; Maslov and Sneppen, 2002; Shen-Orr et al., 2002; Milo et al., 2002; Vazquez et al., 2004; Yeger-Lotem et al., 2004; Pržulj et al., 2004; Tanaka, 2005) owing to their important biological implications (Jeong et al., 2001; Lappe and Holm, 2004).

Comparing large cellular networks is computationally intensive. Exhaustively computing the differences between networks is computationally infeasible, and thus efficient heuristic algorithms have been sought (Kashkan et al., 2004; Pržulj et al., 2006). Although global properties of large networks are easy to compute, they are inappropriate for use on incomplete networks because they can at best describe the structure produced by the biological sampling techniques used to obtain the partial networks (Han et al., 2005). Therefore, bottom-up or local heuristic approaches for studying network structure have been proposed (Milo et al., 2002; Shen-Orr et al., 2002; Pržulj et al., 2004). Analogous to sequence motifs, network motifs have been defined as subgraphs that occur in a network at frequencies much higher than expected at random (Milo et al., 2002; Shen-Orr et al., 2002; Milo et al., 2004). Network motifs have been generalized to topological motifs as recurrent ‘similar’ network sub-patterns (Berg and Lassig, 2004). However, the approaches based on network motifs ignore infrequent subnetworks and subnetworks with ‘average’ frequencies, and thus are not sufficient for full-scale network comparison. Therefore, small connected non-isomorphic induced subgraphs of a large network, called graphlets, have been introduced to design a new measure of local structural similarity between two networks based on their relative frequency distributions (Pržulj et al., 2004).

The earliest attempts to model real-world networks include Erdős–Rényi random graphs (henceforth denoted by ‘ER’) in which edges between pairs of nodes are distributed uniformly at random with the same probability $p$ (Erdős and Rényi, 1959, 1960). This model poorly describes several properties of real-world networks, including the degree distribution and clustering coefficients, and therefore it has been refined into generalized random graphs in which the edges are randomly chosen as in ER random graphs, but the degree distribution is constrained to match the degree distribution of the real network (henceforth, we denote these networks by ‘ER-DD’). Matching other global properties of the real-world networks to the model networks, such as clustering coefficients, lead to further improvements in modeling real-world networks including small-world (Watts and Strogatz, 1998; Newman and Watts, 1999a, b) and scale-free (Simon, 1955; Barabási and Albert, 1999) network models (henceforth, we denote by ‘SF’ scale-free Barabási–Albert networks). Many cellular networks have been described as scale-free (Barabási and Oltvai, 2004). However, this issue has been heavily debated (de Aguiar and Bar-Yam, 2005; Stumpf et al., 2005; Han et al., 2005; Tanaka, 2005). Recently, based on the local relative graphlet frequency distribution measure, a geometric random graph model (Penrose, 2003) has been proposed for high-confidence PPI networks (Pržulj et al., 2004).

### 2. APPROACH

In Section 2.1, we describe the 14 PPI networks and the four network models that we analyzed. Then we describe how we generalize the degree distribution to our spectrum of graphlet degree distributions (Section 2.2); note that the degree distribution is the first distribution in this spectrum, since it corresponds to the only graphlet with two nodes. Finally, we construct a new measure of similarity between two networks based on graphlet degree distributions (Section 2.3). We describe the results of applying this measure to the 14 PPI networks in Section 3.

#### 2.1 PPI and model networks

We analyzed PPI networks of the eukaryotic organisms yeast Saccharomyces cerevisiae, fruitfly Drosophila melanogaster, nematode worm Caenorhabditis elegans, and human. Several different datasets are available for yeast and human, so we analyzed five yeast PPI networks obtained from three different high-throughput studies (Uetz et al., 2000; Ito et al., 2000; von Mering et al., 2002) and five human PPI networks obtained from the two recent high-throughput studies (Stelzl et al., 2005; Rual et al., 2005) and three curated databases (Bader et al., 2003; Peri et al., 2004; Zanoni et al., 2002). We denote by ‘YHC’ the high-confidence yeast PPI network as described by von Mering et al. (2002), by ‘Y11K’ the yeast PPI network defined by the top 11 000 interactions in the von Mering et al. (2002) classification, by ‘YIC’ the Ito et al. (2000) ‘core’ yeast PPI network, by ‘YU’ the Uetz et al. (2000) yeast PPI network, and by ‘YICU’ the union of Ito et al. (2000) core and Uetz et al. (2000) yeast PPI networks [we unioned them as did Han et al. (2005) to increase coverage]. ‘FE’ and ‘FH’ denote the fruitfly D.melanogaster entire and high-confidence PPI networks published by Giot et al. (2003). Similarly, ‘WE’ and ‘WC’ denote the worm C.elegans entire and ‘core’ PPI networks published by Li et al. (2005). Finally, ‘HS’, ‘HG’, ‘HB’, ‘HH’, and ‘HM’ stand for human PPI networks by Stelzl et al. (2005), Rual et al. (2005), from BIND (Bader et al., 2003), HPRD (Peri et al., 2004), and MINT (Zanoni et al., 2002), respectively [BIND, HPRD, and MINT data have been downloaded from OPHID (Brown and Jurisica, 2005) on February 10, 2006]. Note that these PPI networks come from a wide array of experimental techniques; e.g. YHC and Y11K are mainly coming from tandem affinity purifications (TAP) and high-throughput MS/MS protein complex identification (HMS-PCI), whereas YIC, YU, YICU,
FE, FH, WE, WH, HS, and HG are yeast two-hybrid (Y2H), and HB, HH, and HM are a result of human curation (BIND, HPRD, and MINT).

The four network models that we compared against the above 14 PPI networks are ER, ER-DD, SF, and 3-dimensional geometric random graphs (henceforth denoted by ‘GEO-3D’). Model networks corresponding to a PPI network have the same number of nodes and the number of edges within 1% of the PPI network’s [details of the construction of model networks are presented by Przulj et al. (2006)]. For each of the 14 PPI networks, we constructed and analyzed 25 networks belonging to each of these 4 network models. Thus, we analyzed the total of 14 + (14 × 4 × 25) = 1414 networks. We compared the agreement of each of the 14 PPI networks with each of the corresponding 4 network models described above (our new agreement measure is described in Section 3). The results of this analysis are presented in Section 3.

2.2 Graphlet degree distribution (GDD)

We generalize the notion of the degree distribution as follows. The degree distribution measures, for each value of $k$, the number of nodes of degree $k$. In other words, for each value of $k$, it gives the number of nodes ‘touching’ $k$ edges. Note that an edge is the only graphlet with two nodes; henceforth, we call this graphlet $G_0$ (illustrated in Fig. 1). Thus, the degree distribution measures the following: how many nodes ‘touch’ one $G_0$, how many nodes ‘touch’ two $G_0$s, ..., how many nodes ‘touch’ $k$ $G_0$s. Note that there is nothing special about graphlet $G_0$ and that there is no reason not to apply the same measurement to other graphlets. Thus, in addition to applying this measurement to an edge, i.e. graphlet $G_0$, as in the degree distribution, we apply it to the 29 graphlets $G_1, G_2, ..., G_{29}$ presented in Figure 1 as well.

When we apply this measurement to graphlets $G_0, G_1, ..., G_{29}$, we need to take care of certain topological issues that we first illustrate in the following example and then define formally. For graphlet $G_i$, we ask how many nodes touch a $G_i$; however, note that it is topologically relevant to distinguish between nodes touching a $G_1$ at an end or at the middle node. This is due to the following mathematical property of $G_1$; a $G_1$ admits an automorphism (defined below) that maps its end nodes to each other and the middle node to itself. To understand this phenomenon, we need to recall the following standard mathematical definitions. An isomorphism $g$ from graph $X$ to graph $Y$ is a bijection of nodes of $X$ to nodes of $Y$ such that $xy$ is an edge of $X$ if and only if $g(x)g(y)$ is an edge of $Y$; an automorphism is an isomorphism from a graph to itself. The automorphisms of a graph $X$ form a group, called the automorphism group of $X$, and is commonly denoted by $\text{Aut}(X)$. If $x$ is a node of graph $X$, then the automorphism orbit of $x$ is $\text{Orb}(x) = \{y \in V(X) | y = g(x) \text{ for some } g \in \text{Aut}(X)\}$, where $V(X)$ is the set of nodes of graph $X$. Thus, end nodes of a $G_1$ belong to one automorphism orbit, whereas the mid-node of a $G_1$ belongs to another. Note that graphlet $G_0$ (i.e. an edge) has only one automorphism orbit, as does graphlet $G_2$; graphlet $G_3$ has two automorphism orbits, as does graphlet $G_4$, graphlet $G_5$ has one automorphism orbit, graphlet $G_6$ has three automorphism orbits, etc. (Fig. 1). In Figure 1, we illustrate the partition of nodes of graphlets $G_0, G_1, ..., G_{29}$ into automorphism orbits (or just orbits for brevity); henceforth, we number the 73 different orbits of graphlets $G_0, G_1, ..., G_{29}$ from 0 to 72, as illustrated in Figure 1. Analogous to the degree distribution, for each of these 73 automorphism orbits, we count the number of nodes touching a particular graphlet at a node belonging to a particular orbit. For example, we count how many nodes touch one triangle (i.e. graphlet $G_3$), how many nodes touch two triangles, how many nodes touch three triangles, etc. We need to separate nodes touching a $G_1$ at an end-node from those touching it at a mid-node; thus, we count how many nodes touch one $G_1$ at an end-node (i.e. at orbit 1), how many nodes touch two $G_1$s at an end-node, how many nodes touch three $G_1$s at an end-node, etc. and also how many nodes touch one $G_1$ at a mid-node (i.e. at orbit 2), how many nodes touch two $G_1$s at a mid-node, how many nodes touch three $G_1$s at a mid-node, etc. In this way, we obtain 73 distributions analogous to the degree distribution.
(actually, the degree distribution is the distribution for the 0-th orbit, i.e. for graphlet $G_0$). Thus, the degree distribution, which has been considered to be a global network property, is one in the spectrum of 73 'graphlet degree distributions (GDDs)’ measuring local structural properties of a network. Note that GDD is measuring local structure, since it is based on small local network neighborhoods. The distributions are unlikely to be statistically independent of each other, although we have not yet worked out the details of the inter-dependence.

2.3 Network ‘GDD agreement’

There are many ways to ‘reduce’ the large quantity of numbers representing 73 sample distributions. In this section, we describe one way; there may be better ways, and certainly finding better ways to reduce this data is an obvious future direction. Some of the details may seem obscure at first; we justify them at the end of this section.

We start by measuring the 73 GDDs for each network that we wish to compare. Let $G$ be a network (i.e. a graph). For a particular automorphism orbit $j$ (refer to Fig. 1), let $d_j^{\mathcal{G}}(k)$ be the sample distribution of the number of nodes in $G$ touching the appropriate graphlet (for automorphism orbit $j$) $k$ times. That is, $d_j^{\mathcal{G}}$ represents the $j$-th graphlet degree distribution (GDD). We scale $d_j^{\mathcal{G}}$ as

$$S_j^{\mathcal{G}}(k) = \frac{d_j^{\mathcal{G}}(k)}{k}$$

(1)

to decrease the contribution of larger degrees in a GDD (for reasons we describe later that are illustrated in Fig. 2), and then normalize the distribution with respect to its total area $A$,

$$T_j^{\mathcal{G}} = \sum_{k=1}^{\infty} S_j^{\mathcal{G}}(k)$$

(2)

giving the ‘normalized distribution’

$$N_j^{\mathcal{G}}(k) = \frac{S_j^{\mathcal{G}}(k)}{T_j^{\mathcal{G}}}.$$ (3)

In words, $N_j^{\mathcal{G}}$ is the fraction of the total area under the curve, over the entire GDD, devoted to degree $k$. Finally, for two networks $G$ and $H$ and a particular orbit $j$, we define the ‘distance’ $D^{(G,H)}$ between their normalized $j$-th distributions as

$$D^{(G,H)} = \left( \sum_{k=1}^{\infty} [N_j^{\mathcal{G}}(k) - N_j^{\mathcal{H}}(k)]^2 \right)^{1/2},$$

(4)

where again in practice the upper limit of the sum is finite due to the finite sample. The distance is between 0 and 1, where 0 means that $G$ and $H$ have identical $j$-th GDDs, and 1 means that their $j$-th GDDs are far away. Next, we reverse $D^{(G,H)}$ to obtain the $j$-th GDD agreement:

$$A_j^{(G,H)} = 1 - D^{(G,H)},$$

(5)

for $j \in \{0,1,\ldots,72\}$. Finally, the agreement between two networks $G$ and $H$ is either the arithmetic [Equation (6)] or geometric [Equation (7)] mean of $A_j^{(G,H)}$ over all $j$, i.e.

$$A_{\text{arithmetic}}^{(G,H)} = \frac{1}{73} \sum_{j=0}^{72} A_j^{(G,H)},$$

(6)

$$A_{\text{geometric}}^{(G,H)} = \left( \prod_{j=0}^{72} A_j^{(G,H)} \right)^{1/73}. \quad (7)$$

Now we give the rationale for designing the agreement measure in this way. There are many different ways to design a measure of agreement between two distributions. They are all heuristic, and thus one needs to examine the data to design the agreement measure that works best for a particular application. The justification of our choice of the graphlet degree distribution agreement measure can be illustrated by an example of two GDDs for the yeast high-confidence PPI network (von Mering et al., 2002) and the corresponding 3-dimensional geometric random networks presented in Figure 2. This figure gives an illustration of the GDDs of orbit 11 of the PPI and average GDD of orbit 11 in 25 model networks (panel A) being ‘closer’ than the GDDs of orbit 16 (panel B); this is accurately reflected by our agreement measure which gives an agreement of 0.89 for orbit 11 GDDs and of 0.51 for orbit 16. However, note that the sample distributions extend in the x-axis out to degrees of $10^4$ or even $10^5$; we believe that most of the ‘information’ in the distribution is contained in the lower degrees and that the information in the extreme high degrees is noise due to bio-technical false positives caused by auto-activators or sticky proteins (Han et al., 2005). However, without scaling by $1/k$ as in Equation (1), both the area under the curve (2) and the distance (4) would be dominated by the counts for large $k$. This explains the scaling in Equation (1). The ‘normalization’, Equation (3), is performed in order to force both distributions to have a total area under the curve of 1 before they are compared. We can now compute, for each value of $k$, the ‘distance’ between two distributions at that value of $k$. Formally, $k$ is unbounded but in practice it is finite due to the finite size of the graph. We then treat the vector of distances as a vector in the unit cube of dimension equal to the maximum value of $k$. We compute the Euclidean distance between two of these vectors, representing two networks, in Equation (4). Finally, we choose to switch from ‘distance’ to ‘agreement’ in Equation (5) simply because we feel agreement is a more intuitive measure.

To gauge the quality of this agreement measure, we computed the average agreements between various model (i.e. theoretical) networks. For example, when comparing networks of the same type (ER versus ER, ER-DD versus ER-DD, GEO-3D versus GEO-3D, or SF versus SF), we found the mean agreement to be 0.84 with a standard deviation of 0.07. To verify that our ‘agreement’ measure can give low values for networks that are very different, we also constructed a ‘straw-man’ model graph called a circulant (West, 2001), and compared it with some actual PPI network data. A circulant graph is constructed by adding ‘chords’ to a cycle on $n$ nodes (examples of cycles on 3, 4, and 5 nodes are graphlets $G_2$, $G_4$, and $G_5$, respectively) so that $i$-th node on the cycle is connected to the $[(i + j)\mod n] \text{-th}$ and $[(i - j)\mod n] \text{-th}$ node on the cycle. Clearly, a large circulant with an equal number of nodes and edge density as the data would not be very representative of a PPI network, and indeed we find that the agreement between such a circulant, with chords defined by $j \in \{6,12\}$, and the data is <0.08. Note that in most of the 14 PPI networks, the number of edges is about three times the number of nodes, so we chose circulants with three times as many edges as nodes; also, we
chose $j > 5$ to maximize the number of 3, 4, and 5-node graphlets that do not occur in the circulant, since all of the 3, 4, and 5-node graphlets occur in the data.

3 RESULTS AND DISCUSSION

We present the results of applying the newly introduced ‘agreement’ measure (Section 2.3) to 14 eukaryotic PPI networks and their corresponding model networks of four different network model types (described in Section 2.1). The results show that 3-dimensional geometric random graphs have exceptionally high agreement with all of the 14 PPI networks.

We undertook a large-scale scientific computing task by implementing the above described new methods and using them to compare agreements across the 4 random graph models of 14 real PPI networks. Using these new methods, we analyzed a total of 1414 networks: 14 eukaryotic PPI networks per random graph model corresponding to each of the 14 PPI networks, where random graph models were ER, ER-DD, SF, and GEO-3D (described in Section 2.1). The largest of these networks
had around 7000 nodes and over 20,000 edges. For each of the 14 PPI networks and each of the 4 random graph models, we computed averages and standard deviations of graphlet degree distribution (GDD) agreements between the PPI and the 25 corresponding model networks belonging to the same random graph model. The results are presented in Figure 3.

ER networks show ~0.5 agreement with each of the PPI networks whereas scale-free networks of type ER-DD and SF show a slightly improved agreement (ER-DD networks are random scale-free, since the degree distributions forced on them by the corresponding PPI networks roughly follow power law). Note that GEO-3D networks show the highest agreement for all but 1 of the 14 PPI networks (Fig. 3). For HS PPI network, it is not clear which of the GEO-3D, SF, and ER-DD models agrees the most with the data, since the average agreements of HS network with these models are about the same and within 1 SD from each other. GEO-3D and SF model are similarly tied for the FE network. Since networks belonging to the same random graph model have average agreement of 0.84 with a standard deviation of 0.07 (shown in Section 2.3), the agreements of >0.7, that most of the PPI networks have with the GEO-3D model, are very good. Note that 8 out of the 14 PPI networks have agreements with GEO-3D model of >0.75; since...
networks of the same type agree on average by 0.84 ± 0.07, we conclude that the agreements of 0.75 are exceptionally high and are unlikely to be seen by another network model under this measure. Also, it is interesting that GEO-3D model shows high agreement with PPI networks obtained from various experimental techniques (Y2H, TAP, HMP-PC) as well as from human curation (see Section 2.1). Note that this does not mean that GEO-3D is the best possible model. For example, it may be possible to construct a different ‘agreement’ measure that is more sensitive and under which a model better than GEO-3D may be apparent. However, we believe that the current ‘agreement’ measure is sensitive and meaningful enough to conclude that GEO-3D is a better model than ER, ER-DD, and SF.

4 CONCLUSION
We have constructed a new measure of structural similarity between large networks based on the graphlet degree distribution. The degree distribution is the first one in the sequence of graphlet degree distributions that are constructed in a structured and systematic way to impose a large number of constraints on the structure of networks being compared. This new measure is easily extendable to a greater number of constraints simply by adding more graphlets to those in Figure 1, although this would add significantly to the cost of computing agreements; the extensions are limited only by the available CPU. Based on this new network similarity measure, we have shown that almost all of the 14 eukaryotic PPI networks resulting from various high-throughput experimental techniques, as well as curated databases, are better modeled by geometric random graphs than by Erdős–Rényi, random scale-free, or Barabási–Albert scale-free networks. This suggests that a biological description of the (possibly metric) space of PPIs may help us to understand their evolution.

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