DFLpred: High-throughput prediction of disordered flexible linker regions in protein sequences

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Abstract

Motivation: Disordered flexible linkers (DFLs) are disordered regions that serve as flexible linkers/spacers in multi-domain proteins or between structured constituents in domains. They are different from flexible linkers/residues because they are disordered and longer. Availability of experimentally annotated DFLs provides an opportunity to build high-throughput computational predictors of these regions from protein sequences. To date, there are no computational methods that directly predict DFLs and they can be found only indirectly by filtering predicted flexible residues with predictions of disorder.

Results: We conceptualized, developed and empirically assessed a first-of-its-kind sequence-based predictor of DFLs, DFLpred. This method outputs propensity to form DFLs for each residue in the input sequence. DFLpred uses a small set of empirically selected features that quantify propensities to form certain secondary structures, disordered regions and structured regions, which are processed by a fast linear model. Our high-throughput predictor can be used on the whole-proteome scale; it needs <1 h to predict entire proteome on a single CPU. When assessed on an independent test dataset with low sequence-identity proteins, it secures area under the receiver operating characteristic curve equal 0.715 and outperforms existing alternatives that include methods for the prediction of flexible linkers, flexible residues, intrinsically disordered residues and various combinations of these methods. Prediction on the complete human proteome reveals that about 10% of proteins have a large content of over 30% DFL residues. We also estimate that about 6000 DFL regions are long with ≥30 consecutive residues.

Availability and implementation: http://biomine.ece.ualberta.ca/DFLpred/.

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Supplementary information: Supplementary data are available at Bioinformatics online.

1 Introduction

Intrinsically disordered proteins (IDPs) lack stable tertiary structure under physiological conditions, either along their entire sequence or in localized regions. IDPs are abundant in eukaryotes (Peng et al., 2015; Ward et al., 2004) and are typically involved in signaling, regulation, control, storage of small molecules, sites for post-translational modifications (PTMs), transcription, translation and assembly of multi-protein complexes (Dunker et al., 2008; Dyson and Wright, 2005; Peng et al., 2014; Tompa, 2005; Wright and Dyson, 1999; Xie et al., 2007). Their functions complement functions of structured proteins, which include small molecule binding, transport and catalysis (Radivojac et al., 2007). The newest release of DisProt database (Sickmeier et al., 2007), the main source of functionally annotated IDPs, lists >30 functions (Dunker et al., 2002) that have been assigned to about 1200 disordered regions. About 74% of the functionally characterized disordered regions in DisProt concern binding to a variety of partners: proteins, DNAs, RNAs, metals and lipids. The most populated non-binding functions include flexible linkers (9%), sites for several types of PTMs (7%), transactivation (4%), nuclear localization signals (1%) and electron transfer (1%). Several methods have been developed for the prediction of binding disordered regions from protein sequences. They include methods that address protein binding (Disfani et al., 2012; Dosztanyi et al., 2009; Fang et al., 2013; Jones and Cozzetto, 2014;
Khan et al., 2013; Malhis and Gsponer, 2015; Meszaros et al., 2009; Peng and Kurgan, 2015; Yan et al., 2015) and RNA and DNA binding (Peng and Kurgan, 2015). However, methods for the prediction of the other functions of the intrinsically disordered regions are lacking.

The disordered flexible linkers (DFLs) are disordered regions that serve as linkers or spacers between domains in multi-domain proteins and between structured constituents in domains (Dunker et al., 2002). Experimental annotation of DFLs primarily relies on the X-ray crystallography, NMR spectroscopy and circular dichroism. We consider these regions for several reasons. First, this is the most annotated and not related to binding function of disordered regions. Second, DFLs are important for a variety of cellular processes. A few recent examples include formation of amyloid fibrils (Shvadchak and Subramaniam, 2014), linking multiple disordered protein binding regions (Oldfield and Dunker, 2014), and movement of structured domains between catalytic sites (Anand and Mohanty, 2012). Third, there is no computational methods that predict this class of disordered regions. DFLs are cousins of linkers, which are regions that connect domains and maintain inter-domain interactions (Chen et al., 2013; George and Heringa, 2002). A subclass of linkers are flexible linkers, defined as flexible inter-domain regions that allow two domains to move relatively to each other (Chen et al., 2013). DFLs differ from linker regions in two aspects: (1) DFLs are characterized by extreme level of flexibility and lack of defined structure (they form conformational ensembles) as compared with linkers and flexible linkers that have more defined structures; and (2) linkers are shorter (avg length of 10 residues) and localized between domains (George and Heringa, 2002), while DFLs tend to be longer (avg length of 25 residues in our dataset) and could be localized in domains, for instance to link structured elements in a domain; we show empirically that they are frequently localized in domains and give examples of intra- and inter-domain DFLs.

Although there are no computational methods that directly predict DFLs in protein sequences, Udvary–Merski algorithm (UMA) (Udvary et al., 2002) can be used to predict flexible linker regions. It assumes that flexible linkers are less likely to be conserved in the sequence and secondary structure and to be depleted in hydrophilic residues. Thus, UMA quantifies every residue as a weighted sum of hydrophobicity score and conservation scores for sequence and secondary structure. The two conservation scores are derived using ClustalX (Thompson et al., 1997) and PHDsec (Rost and Sander, 1993; Rost and Sander, 1994), and the hydrophobicity score is assigned using the Kyte and Doolittle’s hydrophathy index (Kyte and Doolittle, 1982). A low UMA score indicates that a residue is more likely to be a flexible linker. Because flexible linkers are a subset of flexible residues, they could be also potentially identified with sequence-based predictors of flexible residues. These predictors include PROFbval (Schlessinger and Rost, 2005; Schlessinger et al., 2006), FlexPred (Kuznetsov and McDuffie, 2008; Kuznetsov, 2008), PredBF (Pan and Shen, 2009), PredFleXy (de Brevern et al., 2012) and DynaMine (Cilia et al., 2013, 2014). PROFbval predicts B-factors using a neural network model, where a low/high real B-factor value indicates a low/high propensity of a residue being flexible. PredBF also predicts B-factors but using a two-layer support vector regression model. FlexPred predicts conformationally variable positions in the input protein chain using a support vector machine model. PredFleXy classifies every input residue as rigid, intermediate or flexible and also outputs putative normalized B-factors and root mean square fluctuations, from molecular dynamic simulations. DynaMine quantifies backbone flexibility in terms of N-H $S^2$ order parameter values using regression where smaller $S^2$ means that a given residue is more likely to be flexible.

The UMA method and protein flexibility predictors predict flexible linkers/residues, but they do not accommodate for the disordered state of these residues. Moreover, UMA requires that the input sequence has homologous sequences to generate multiple sequence alignment profiles, which means that it may not generate predictions for some proteins, and is tedious to execute because its implementation requires manual processing. To this end, we have developed DFLpred, the first method that predicts DFLs. DFLpred does not need alignment profiles, is fast to execute and is provided to the end users as a fully automated webserver at http://biomine.ece.ualberta.ca/DFLpred/.

2 Materials and methods

2.1 Datasets

The functionally annotated data were collected from the newest release 6.0.2 of DisProt that includes 694 sequences. We excluded DP00688 sequence that was too long (>18 000 residues) to predict with the PSIPRED (Buchan et al., 2013) to generate secondary structure. We selected 204 sequences, which include 82 proteins that have annotations of DFLs and 122 proteins that do not have DFL annotations but for which all residues are annotated. This way we included all annotated DFLs and reduced the number of ambiguous (unannotated) residues.

We assumed that residues that are not annotated as DFLs but have other functional annotations are non-disordered flexible linker (NDFL) residues. The residues without functional annotations were excluded from the design and assessment. We divided the set of 204 proteins into five subsets and reduced sequence similarity between these subsets with BLASTClust (Altschul et al., 1990). First, we clustered the 204 sequences with sequence identity threshold at 25% and coverage of at least 10% of the sequence length. Second, the resulting 160 clusters that include similar sequences (>25% similarity) were divided at random between the five sub sets to ensure that each subset has similar number of sequences and similar ratio of DFL to NDFL residues. Four of these subsets were used in 4-fold cross-validation protocol to empirically design our predictor, i.e. to conceptualize and select inputs for the predictive model, and to select and parameterize this model. These data constitute the training dataset. The remaining fifth subset was used as an independent (never used in the design) test dataset. This way, sequences in the test dataset share low similarity with sequences in the training dataset, and also sequence in individual folds of the training dataset share low similarity with sequences in the other folds. The training and test datasets have 144 sequences and 60 sequences, respectively, and they are available at http://biomine.ece.ualberta.ca/DFLpred/.

2.2 DFLs and protein domains

We used Interpro (Mitchell et al., 2015) to annotate domains to empirically investigate whether DFLs are localized within or between domains. Interpro is a template-based method that integrates 11 databases including Pfam (Finn et al., 2014), PRINTS (Attwood et al., 2012), PROSITE (Sigrist et al., 2013) and ProDom (Servant et al., 2002) to provide prediction of proteins families and domains. The comprehensive coverage of the source databases, 15 years of history and high rate of updates make Interpro a mainstream tool for the annotation of domains (Goujon et al., 2010). The ratio of the number of intra-domain to inter-domain DFL residues in the training dataset is 905/1098 = 0.82. This indicates that a large
fraction of DFLs are localized in domains. The ratio of intra-domain DFL to NDFL residues is 905/7019 = 0.13 and for inter-domain is 1098/14 132 = 0.08. To sum up, our results suggest that DFLs are often localized in protein domains.

2.3 Evaluation procedures

The prediction of DFLs results in a numeric score in the range between 0 and 1 representing propensity of each residue in the input sequence being in a DFL. We used the receiver operating characteristic (ROC) curve and the area under ROC (AUC) to examine the predictive quality. To plot ROC curves and quantify AUC values, we calculated the true-positive rates (TPRs) and false-positive rates (FPRs) by comparing predictions with native annotations at different cutoffs imposed on the predicted scores. If a score is more than or equal to a given threshold, then the corresponding residue is assumed to be in DFL, otherwise it is assumed as NDFL. TPR and FPR are defined as:

\[
TPR = TP/(TP + FN) = TP/\text{number of DFL residues} \tag{1}
\]

\[
FPR = FP/(FP + TN) = FP/\text{number of NDFL residues} \tag{2}
\]

where \(TP\) is the number of true positives (correctly predicted DFL residues), \(FN\) is the number of false negatives (DFL residues that were predicted as NDFL residues), \(FP\) is the number of false positives (NDFL residues that were predicted as DFL residues), \(TN\) is the number of true negatives (correctly predicted NDFL residues). Given TPR and FPR values at different thresholds ranging between 0 and 1, we plotted the ROC curve and calculated the corresponding AUC value.

We also calculated \(AUC_{\text{lowFPR}}\), which is the AUC for low range of FPR values, between 0 and 0.1. This part at the beginning of the ROC curve reflects ability to predict a small number of high-quality DFL residues, i.e. only a relatively small portion of these predictions are FPs. We also compute Ratio = \(AUC_{\text{lowFPR}}/AUC_{\text{random}}\) where \(AUC_{\text{lowFPR}}\) is divided by the AUC of a random predictor (for which TPR always equals to FPR) computed for FPR values between 0 and 0.1. This Ratio reflects how much better a given predictor is when compared with a random prediction.

Following (Disfani et al., 2012; Peng and Kurgan, 2015; Yan et al., 2015), we tested statistical significance of differences in predictive quality offered by DFLpred and other methods, and between the selected design of DFLpred and other considered designs. This test investigates whether results on a given dataset are not biased by a subset of proteins by measuring whether the predictive performance is consistent over different subsets of the dataset. First, we randomly selected half of proteins from a given test dataset (test dataset or test folds from the cross validation on the training dataset) 10 times and we measured predictive performance of all considered methods on these 10 protein sets. We compared these 10 pairs of results between DFLpred and other methods. Given that measurements are normal, as assessed with the Anderson-Darling test (Anderson and Darling, 1952), we used paired \(t\)-test, otherwise we used the Wilcoxon signed-rank test (Wilcoxon, 1945). We considered a given difference to be significant if the \(p\)-value < 0.01.

2.4 Overall design

The architecture of DFLpred (Fig. 1) includes three layers:

1. Represent every residue of the input sequence with its amino acid (AA) type and information predicted directly from the sequence including propensity to form structured regions, intrinsically disordered regions and helical and coil conformations.

2. Convert this representation into empirically selected set of numeric features that are computed using sliding windows.

3. Input the selected features into an empirically selected and parameterized predictive model to generate propensity scores.

2.4.1 Sequence representation

In the first layer, we represented every residue by its AA type, its physicochemical properties estimated based on the AA indices from the AAindex database (Kawashima et al., 2008), secondary structure predicted with PSIPRED (Buchan et al., 2013), intrinsically disordered and structured regions predicted with IUPred (Dosztányi et al., 2005) and sequence complexity computed with SEG (Wootton, 1994). Supplementary Figure S1 summarizes enrichment and depletion of the 20 AA types in DFL regions. We note a clear pattern where DFLs are significantly enriched in the disorder-promoting residues, such as Q, S, E and P, and depleted in the order-promoting residues, including F, Y, I, M, L and V; details are discussed in Supplementary Section 1.

2.4.2 Considered features

In the second layer, we generated numerical features that quantify the considered structural and sequence-based properties for each residue of the input AA sequence. We represented every residue by a feature vector calculated from a sliding window centered on that residue. The sliding window aggregates structural and sequence-based information by considering characteristics of AAs adjacent in the sequence. The concept of the sliding window has been adopted in other relevant predictors such as MoRFpred, fMoRFpred, DisoRDPbind, PROFbval, FlexPred, PredBF, PredyFlexy and DynaMine. We set the length of the sliding window to 17, which is the median value of the length of longest per protein DFLs in our dataset. This way the selected window size covers the full length of at least half of DFLs without recruiting much of potential noise (NDFL residues) when used to predict shorter regions. We did not pad the window for the residues located at either terminus of the sequence, and correspondingly the length of the sliding window is reduced on one of its sides, i.e. window size is 8 for the first and last residues in the sequence. Consequently, we normalize values of features computed over the residues in the window by the size of the window. In total, we considered 2236 features including 40 features derived directly from the sequence, 2124 features derived from physicochemical properties of AAs quantified based on the AAindex database, 22 features generated from the putative secondary structure, 40 features from putative intrinsic disorder and structured regions and 10 features from the sequence complexity. These features quantify composition of AAs; composition, counts and length of
putative secondary structures, intrinsically disordered regions, structured regions and high sequence complexity regions in the sliding window; average physicochemical properties of residues in the sliding windows; and AA type, secondary structure, disorder status, sequence complexity status and physicochemical properties of the residue in the center of the window. We decided to use all physicochemical properties from AAnindex (thus the large number of these features) and our empirical feature selection to remove irrelevant and redundant features because there are no prior results that we could use to pre-select a subset of these properties. Detailed list and description of the considered features are included in Supplementary Section 2.

2.4.3 Selected features and predictive model

Our vector of 2236 features likely includes features that are irrelevant to the prediction of DFLs and features that have high mutual correlations. We used a two-step empirical feature selection to select a subset of features characterized by high predictive value and low mutual correlations. In the first step we removed low-quality features that have low correlation with the annotation of the DFLs. We have two types of features: real-valued (e.g. features computed as an average over the sliding window) and binary (e.g. disordered versus ordered status of the residue in the center of the window). Inspired by (Disfani et al., 2012; Yan et al., 2015), we used point-biserial correlation coefficient \( r_{pb} \) and \( \varphi \) coefficient, respectively, for these two feature types:

\[
r_{pb} = \frac{M_{DFL} - M_{NDFL}}{S_u} \times \sqrt{\frac{n_{DFL} \times n_{NDFL}}{n^2}}
\]

\[
\varphi = \frac{\text{count}_{[A]_{DFL}} \times \text{count}_{[A]_{NDFL}} - \text{count}_{[A]_{DFL}} \times \text{count}_{[A]_{NDFL}}}{\text{count}_{[A]_1} \times \text{count}_{[A]_0} \times \text{count}_{[A]_{DFL}} \times \text{count}_{[A]_{NDFL}}}
\]

In formula (3), \( M_{DFL} \) and \( M_{NDFL} \) (\( n_{DFL} \) and \( n_{NDFL} \)) are the means (numbers) of values given real-valued feature for the residues annotated as DFLs and NDFLs, respectively; \( n = n_{DFL} + n_{NDFL} \) and \( S_u \) is the standard deviation of all values of that feature. In formula (4), \( \text{count}_{[i]_{AB}} \) is the number of values \( i = 0, 1 \) of binary feature \( F \) corresponding to residues with values \( k = \{ \text{NDFL, DFL} \} \) of the annotation \( A \); \( \text{count}_{[i]} \) and \( \text{count}_{[A]} \) are the number of values \( i = 0, 1 \) of binary feature \( F \) and the number of residues with values \( k = \{ \text{NDFL, DFL} \} \) of the annotation \( A \), respectively. We calculated average \( r_{pb} \) (for the real-valued features) and \( \varphi \) (for the binary features) for all considered features from four correlations computed on the training folds from the 4-fold cross-validation on the training dataset. We normalized the values of the average \( r_{pb} \) and \( \varphi \) correlations to the \(-1\) to \(1\) range using min-max normalization, and removed the features for which the absolute normalized \( r_{pb} \) or \( \varphi \) value is less than threshold \( T_{\text{step1}} \). Next, we ranked the remaining features by their absolute normalized \( r_{pb} \) or \( \varphi \) values.

In the second step, inspired by (Disfani et al., 2012; Yan et al., 2015), we eliminated mutually correlated features using the Pearson correlation coefficient \( r_{pc} \). First, a set of selected features is initialized with the top-ranked in the first step feature. Next, we calculated \( r_{pc} \) between the next-ranked feature and all selected features. If the absolute value of this \( r_{pc} \) is less than threshold \( T_{\text{step2}} \), then we add this next-ranked features into the set of selected features, otherwise we do not add it. We apply this procedure through the entire list of ranked features passed from the first step.

We vary values of each of the two thresholds, \( T_{\text{step1}} \) and \( T_{\text{step2}} \) between 0.1 and 0.9 with step of 0.05, to obtain \( 17 \times 17 = 289 \) different feature sets. The corresponding feature sets vary in size between 1 and 884 features. Each feature set is used with three classifiers: logistic regression, naive Bayes and k-nearest neighbor, in the 4-folds cross-validation on the training dataset to select the design that offers the highest AUC value. We also parameterized logistic regression and k-nearest neighbor classifiers for each of these experiments by selecting their parameters that correspond to the highest AUC in the 4-folds cross-validation on the training dataset. Naive Bayes has no parameters. For the logistic regression, we considered \( \text{ridge} = 10^6 \), where \( x \) ranges from \(-4\) to \(4\) with step of \(1\). For the k-nearest neighbor, we consider the number of neighbors \( k \) ranging from \(50\) to \(800\) with the step of \(50\). Supplementary Table S1 summarizes results with the highest AUC value for each of the three classifiers, which are selected from across the experiments that correspond to 7514 combinations of the two thresholds and different parameters of classifiers (289 combinations for Naïve Bayes + \(9^2\) for logistic regression + \(16^2\) for k-nearest neighbor).

We selected the logistic regression classifier with four features that gives the highest values of AUC, AUC\_lowFPR and ratio. The differences in these three measures of predictive quality between the logistic regression and the other two classifiers are statistically significant. The ratio reveals that the selected design is 3.3 times better than a random predictor when predicting with low FPR, i.e. when a high fraction of predictions of DFL residues (predicted positive residues) is correct. The architecture of this model is shown in Figure 1. Given an AA sequence, it uses putative annotations of structured and long disordered regions generated with IUPred and two physicochemical properties of residues that quantify propensity for formation of helices and turns.

3 Results

3.1 Analysis of the DFLpred’s predictive model

DFLpred’s model combines values of four empirically selected features using a linear function to generate the output propensities. These features were computed from the sequence using sliding windows on putative annotations generated with IUPred and two AA indices; their details are summarized in Table 1. Figure 2 compares values of the four features between the native DFL and NDFL residues in the test dataset (these results were not used to design the model, which is based on the training dataset).

The WIN\_IUP\_fraction feature quantifies fraction of residues predicted with IUPred\_struct not to be in structured regions in a window centered on the predicted residue. Its average for DFL residues is 0.29, for the NDFL residues is 0.60 and for the NFDFL residues annotated as structured is 0.11. The structured residues have the lowest value because they should be primarily predicted to be in structured regions; the value > 0 because some of the residues in the surrounding window could lack structure. The high value of mean for NFDFL residues is driven by the fact that these residues include disordered residues that are not DFLs which have a large number of nearby (in the sequence) unstructured residues. The average for DFLs is in between the other two averages. This reveals that propensity of these residues to be nearby putative structured regions is lower than for other disordered regions but higher than for structured regions. This makes sense because residues in DFLs link primarily structured domains, and thus their neighbors in the sequence should include a sizable fraction of structured residues, but not as large as for the structured residues.

The plot of the WIN\_IUP\_std feature in Figure 2 suggests that putative propensities for disorder of residues in DFLs have
higher standard deviation in the window compared with the other residues. This means that these propensities fluctuate more in residues adjacent to DFL residues. This is reasonable given that DFLs link structured domains where propensity for disorder should be substantially lower compared with DFLs. In contrast, residues located in structured or in disordered regions would experience less variability in the propensities for disorder in these regions.

The last two features are computed by averaging values of the selected two AA indices in the sliding window. Higher values of the AURR980118 index (Aurora and Rosee, 1998) indicate higher likelihood of a given residue to be included in a helical conformation. Thus, the corresponding feature can be used as a proxy to quantify likelihood of helical conformations in the window. Figure 3 shows that residues in DFLs have lower values of this feature, which suggests that they are less likely to include helices nearby in the sequence compared with NDFLs. This again is rational because DFLs are unstructured. The second, PALJ810114 index (Pal et al., 1982), quantifies likelihood of forming turns. Here, DFLs have higher values compared with the other residues, which is sensible given that turns are relatively flexible, which is also characteristic for DFLs.

We also investigated predictive quality of these features individually and in different sets to find out how much they contribute to the predictive model and whether they complement each other. The AUC values based on the 4-fold cross-validations on the training dataset for the individual features sorted in the order shown in Table 1 are 0.599, 0.604, 0.584 and 0.580. The fact that AUC values are similar suggests that these features contribute equally to our model. When we use the top \( n = 1, 2, 3, 4 \) features (ranked as in Table 1, which is based on the normalized point-biserial correlation \( r_{pb} \)), the corresponding AUC values are 0.599, 0.646, 0.672 and 0.702. This means that each feature adds to the model and demonstrates that they complement each other.

Overall, we demonstrated that the four features are meaningful markers of DFLs. They complement each other by using a different type of information to pinpoint location of DFLs. This agrees with our empirical approach to design DFLpred in which we explicitly selected highly predictive features (first step of feature selection) that are characterized by low mutual correlation (second step of feature selection).

<table>
<thead>
<tr>
<th>Feature name</th>
<th>Description</th>
<th>( r_{pb} )</th>
<th>Coeff</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \text{WIN}<em>{\text{IUP}}</em>{\text{ fraction D}} )</td>
<td>Number of residues predicted with IUPred_struct not to be in structured regions in a sliding window divided by the window length.</td>
<td>-1.00</td>
<td>-1.10</td>
</tr>
<tr>
<td>( \text{WIN}<em>{\text{IUP}}</em>{\text{ std d}} )</td>
<td>Standard deviation of propensity scores from IUPred_long for residues in the sliding window.</td>
<td>0.70</td>
<td>6.60</td>
</tr>
<tr>
<td>( \text{WIN}_{\text{AA ind avg AURR980118}} )</td>
<td>Average value of AURR980118 AA index for all residues in the sliding window.</td>
<td>-0.66</td>
<td>-4.58</td>
</tr>
<tr>
<td>( \text{WIN}_{\text{AA ind avg PALJ810114}} )</td>
<td>Average value of PALJ810114 AA index for all residues in the sliding window.</td>
<td>0.57</td>
<td>3.32</td>
</tr>
<tr>
<td>Intercept of the linear function</td>
<td>N/A</td>
<td>-0.92</td>
<td></td>
</tr>
</tbody>
</table>

\( r_{pb} \): Normalized point-biserial correlation coefficient of a given feature with the annotation of DFLs in the training dataset; Coeff: coefficient of a given feature in the linear model generated with logistic regression using training dataset.
The methods were ranked by AUC value in each category.

<Denotes that difference in predictive quality when compared with DFLpred is significant at \( p < 0.01 \).

### 3.2 Comparison of predictive performance with closest alternative methods

We compared the predictive performance of DFLpred with closest alternative methods that could be used to find DFLs. These approaches include the UMA method that finds flexible linkers, predictors of flexible residues and disordered residues, and a domain predictor given the fact that classical linkers are localized between domains. We also combined the results of UMA with the results of the disorder predictors and the results of the flexibility predictors with the disorder predictors. This was motivated by the fact that these combinations could potentially find flexible linkers or flexible residues localized in disordered regions, which is the hallmark of the DFLs. We used two ways to combine their predictions, by multiplying the scores predicted with UMA and flexibility predictors by the binary disorder predictions and by the predicted real-valued propensity for the disorder. In the first case, the UMA and flexibility scores remain the same for the predicted disordered residues and are set to zero for the residues that are not predicted to be disordered. In the second scenario, the UMA and flexibility scores are scaled by the predicted propensity for disorder. We used a comprehensive set of predictors of flexible residues including PROFbval, FlexPred, PredBF, PredyFlexy, and Dynamine. We also considered several predictors of disorder including two versions of IUPred (short and long), MFDp (Mizianty et al., 2010) and three versions of Espritz (NMR, X-Ray and DisProt; Walsh et al., 2012). We applied ThreaDom (Xue et al., 2013) to predict domains, given its strong predictive performance and availability of a webserver. Details on the computation of predictions with the other methods are given in Supplementary Section 3.

Table 2 summarizes results of DFLpred and the other methods on the test dataset. We show results for DFLpred, UMA, five methods for prediction of flexible residues, three methods for prediction of disordered residues (we show results for one version of IUPred and Espritz that secures the highest AUC) and ThreaDom for the prediction of domains. We also include result for each of the two ways to combine these methods, as described above, which secured the highest AUC value. DFLpred secures the highest AUC, AUC\textsubscript{lowFPR} and Ratio values. The improvement offered by DFLpred are significant at \( p\)-value \( < 0.01 \) when compared with all considered methods. The Ratio indicates that DFLpred is 3.3 times better than a random predictor in AUC for the low values of FPR \( \leq 0.1 \). The inset in Figure 3 visualizes this difference between this AUC of a random predictor (thin diagonal line) and DFLpred (thick black line).

We use two proteins from the test dataset to visualize prediction of DFLs localized between domains (chemotaxis cheA protein; Supplementary Fig. S2A) and inside of a domain (troponin I protein; Supplementary Fig. S2B). CheA includes five domains and we focus on the C-terminus that includes Hpt, CheY binding and signal transducing H kinase domains that are connected by two inter-domain DFLs. Troponin I includes two domains: troponin I N-terminus domain, which is disordered, and troponin I domain, which is composed of two sub-domains: IT arm and regulatory head. The IT arm sub-domain has DFL, which links two of its helices that interact with troponins T and C that compose the troponin complex. The second DFL links the two sub-domains. Both of these intra-domain DFLs enable movement of several structural elements of the troponin I domain, allowing it to interact with the other members of the troponin complex (Takeda et al., 2003). The figures show predictions from DFLpred, UMA, domain predator ThreaDom and the best-performing (based on Table 2) disorder predictor Espritz and flexibility predictor PredyFlexy. DFLpred generates higher propensities in the vicinity of the two inter-domain DFLs in CheA, with the second one predicted less accurately. It also finds the first intra-domain DFL and to some extent, given the lower values of propensity, the second intra-domain DFL in troponin I. ThreaDom accurately finds the inter-domain residues that overlap with the two DFLs in CheA, but its prediction also includes residues at the N-terminus that are not DFLs. This method finds the inter-domain region in troponin I, which is not a DFL, and has difficulty with the troponin I domain, given it is fragmented into sub-domain compositions. Espritz accurately predicts the disordered residues, which coincide with the inter-domain DFLs in CheA, but it also finds disorder at the N-terminus. It correctly finds the first two disordered regions in troponin I but it misses the second intra-domain DFL and predicts the disordered region at the N-terminus the highest propensity while this region is not a linker. UMA finds three flexible linkers (residues with high scores) in CheA and only the last one coincides to some extent with the second DFLs. For the second protein, this method annotates only the N-terminus as a flexible linker and fails to identify the intra-domain DFLs. Finally, PredyFlexy does not find inter-domain residues, DFLs or disordered regions, but rather it estimates local flexibility, which fluctuates widely along the sequence of both proteins. These observations provide context to interpret results of the other methods in Table 2.

The UMA method secures low AUC and this could be explained by the fact that UMA predicts flexible linkers that likely exclude linkers located in disordered regions; the latter stems from the low value of AUC\textsubscript{lowFPR} and is confirmed by our examples. The low AUC of UMA is owing to a concave shape of ROC curve that in turn results from high levels of false positives on the left side of the curve. These false positives are the residues predicted as DFLs for the purpose of our evaluation but which in fact correspond to the putative flexible linkers predicted by UMA with the highest values of propensity. The predictors of disordered residues have similar weakness. They predict all disordered residues, irrespective of their function, while most of them are not DFLs. Their low values of AUC\textsubscript{lowFPR} and our troponin I example suggest that propensities generated for DFLs are lower than the propensities for other disordered regions. This results in high
FPRs, concave shapes of ROC curves and consequently low AUC values. Predictors of flexible residues also secure relatively low AUC values. These methods were built using crystallographic data that exclude disordered residues and thus they cannot accurately find disordered residues, which was shown in (Peng and Kurgan, 2012). Our example reveals that they focus on local, in the sequence, flexibility that does not correlate with the localization of DFLs. ThreaDom finds the inter-domain regions but only some of them are DFLs and it in general fails to find the intra-domain DFLs. Consequently, its AUC value is relatively low. Interestingly, combining UMA/flexibility predictors with the disorder predictors also does not produce high-quality predictions. This is likely because neither UMA nor predictors of flexibility provide accurate estimates for the disordered regions. Overall, we conclude that while currently there are no approaches that can accurately predict DFLs, our DFLpred offers such accurate predictions.

We also evaluate the considered methods separately for inter- and intra-domain residues, see Supplementary Table S2. DFLpred can accurately predict DFLs both inside and outside of domains, with AUC = 0.72 and 0.73 and Ratio = 3.3 and 3.8, respectively. These results are significantly better than the results of all other considered methods. The UMA method has substantially higher AUC for prediction of DFLs outside of domains compared with the results for residues localized inside the domains. This difference reflects the fact that flexible linkers that are targeted by UMA are localized between domains. On the other hand, flexibility predictors secure slightly better predictive quality for residues in domains compared with the residues outside the domains. Finally, disorder predictors are equally inaccurate for both inter- and intra-domain residues and the best combinations of flexibility predictors and disorder predictors work better inside the domains. The latter is perhaps because these combinations use PredyFlexy predictors that perform better inside the domains.

We plot ROC curves for all methods for which the AUC > 0.52 based on the evaluations on the entire test dataset and separately for the inter- and intra-domain residues, see Figure 3. Supplementary Figure S3 shows the ROC curves in larger format for methods with the AUC > 0.5. We also include the result when using sequence alignment. The alignment-based predictor copies DFL annotations of aligned residues from the most similar sequence in the training dataset based on its alignment to a query sequence from the test dataset. The alignment is done with PSI-BLAST using default parameters (Altschul et al., 1997). Because alignment transfers binary annotations of DFLs from the training proteins, we can show only one point for the ROC curve for this simple predictor. The FPR and TPR values of alignment-based predictors equal 0.039 and 0.014, respectively. In other words, it predicts only 1.4% of DFL residues with the cost of predicting 3.9% of NDFL residues as DFL residues. This is because our test dataset is designed to share low (25% or lower) sequence similarity with the training dataset. In contrast, DFLpred can produce high-quality results even in the absence of sequence similarity. When considering the same FPR = 0.039, DFLpred’s TRP is 10 times higher and equals 0.148. Moreover, DFLpred’s ROC curves are substantially above the curves of other methods over the entire range of FPR values. We also note a large improvement for the low FPR values (see insert in Fig. 3).

3.3 Relation between predicted propensity and predictive quality

DFLpred outputs real-valued propensities for each residue in the input protein chain where higher values of propensity denote higher likelihood that a given residue is a part of a DFL. Figure 4 shows relation between the values of propensity and the predictive quality by calculating fraction of residues in native DFLs (black line) and native NDFLs (gray line), which are predicted with propensities below a value shown on the x-axis. Larger vertical separation between the two lines corresponds to a better separation between DFLs and NDFLs by outputs produced with DFLpred. The propensities generated by DFLpred are constrained to the 0–0.3 range and offer a large separation. We picked two representative values of propensities (vertical dotted lines in Fig. 3) to demonstrate how to interpret DFLpred’s predictions. Half of the NDFLs are found among the residues predicted with propensity < 0.07, while these residues include only about 20% of DFLs. Similarly, half of DFLs and only 20% of NDFLs are found among the residues for which the predicted propensity >0.12.

3.4 Runtime

DFLpred is implemented as a linear function of features computed directly from sequence and from sequence-derived predictions generated with IUPred. IUPred’s predictions are calculated from pairwise energy profile without a time-consuming alignment or predictive model. Consequently, DFLpred is fast.

We quantify and compare DFLpred’s runtime with the runtime of UMA and all individual methods that obtained AUC > 0.5 in Table 2 or Supplementary Table S2. The predictions were run on the same 64-bit computer with 3.5 GHZ CPU and 4 GB of RAM running Ubuntu operating system. UMA is run manually and requires computation of hydrophobicity, finding homologous sequences and prediction of secondary structure. We estimate a lower bound on the UMA’s runtime by computing time to complete the most time-consuming finding of homologs. This is based on executing BLAST against the NR database using the suggested by the author e-value = 1e-20. We used stand-alone version of PredyFlexy that was provided by the authors. FlexPred and PredBF do not provide stand-alone versions but both methods use PSI-BLAST to generate position-specific scoring matrix against the NR database. We use this calculation to estimate lower bounds of their runtime. As suggested by the authors, we compute the runtime of running PSI-BLAST with five iterations and default e-value for FlexPred, and with three iterations and e-value = 0.001 for PredBF. We did not include ThreaDom because it requires running LOMETS (Local Meta-Threading-Server) framework, which takes substantially longer time than the other methods. We collected the runtime of the considered methods for 204 proteins from the training and test datasets. We sorted the proteins by their...
size quantified with the sequence length, divided them into 10 equally sized groups based on the size and computed average runtime for each group.

Figure 5 compares the average runtime against the average length of sequences for the five methods. The runtime of DFLpred, Espritz_NMR, PredyFlexy, UMA, FlexPred and PredBF is in the range of $10^2$, $10^3$, $10^4$ to $10^5$, $10^5$ to $10^6$ and $10^6$, respectively, measured in milliseconds. DFLpred is up to 4 orders of magnitude faster than the alternatives, which is a significant advantage. To put this into perspective, if these methods would be used to predict the complete reviewed human proteome from UniProt (20 193 sequences with an average length of 561), DFLpred, Espritz, PredyFlexy, UMA, FlexPred and PredBF would take about 40 min, 80 min, 11.5 days, 185 days, 231.5 days, and 231.5 days, respectively. This estimate is based on a linear fit into the measured data that are shown using markers and length (panel B) and lines show the cumulative fraction for a given range of the content (panel A) and length (panel B).

**Table 5** shows the average runtime (logarithmic scale) for each group.

![Figure 5.](https://example.com/figure5.png)

**Figure 6A** shows a histogram of the length of putative DFLs. Most of these regions are relatively short, with about 80% of them being shorter than 10 residues; some of them could be spurious predictions given the assumed 5% FPR. However, about 7% and 2.6% of these regions span at least 20 and 30 consecutive residues, respectively. We found 6029 DFL regions that that are at least 30 residues long.

### 3.6 Webserver
DFLpred is freely available as a webserver at [http://biomine.ence.ualberta.ca/DFLpred](http://biomine.ence.ualberta.ca/DFLpred). It requires the end user only to provide the input protein sequence(s) in FASTA format and email address. The email is used to deliver a notification of the finished prediction and URL results that are available for download. The same information is available in the browser window given that this window will not be closed until the prediction is finished. The server automatically generates the corresponding propensities and binary predictions (DFL versus NDFL residue). The binary predictions are computed from the propensities using the cutoff $= 0.18$ (residues with propensity $>0.18$ are assumed to form DFLs), which corresponds to the 5% FPR. The webserver allows for batch predictions of datasets with up to 5000 proteins.

### 4 Summary
We conceptualized, designed, tested and deployed a novel computational method, DFLpred, for the prediction of the DFLs from protein sequences. We developed four strong and complementary sequence-derived markers of DFLs and combined them using a linear function to build DFLpred. Empirical tests on independent
(blind) test dataset demonstrated that our method provides relatively accurate predictions even for proteins that share low sequence identity. DFLpred outperformed the closest related methods including UMA, which predicts flexible linkers, several protein flexibility predictors and their combinations with disorder predictors. We note that the value of AUC = 0.72 secured by DFLpred is affected by the challenging nature of the dataset (proteins in this dataset share low, <25%, identity with the training sequences) and the fact that the annotations of DFLs could be incomplete. In other words, results on proteins that share larger sequences similarity with our training dataset should be better and some of the false positives in our test dataset could in fact corresponds to DFLs that are yet to be annotated. Another potential issue is the precision with which the boundaries of DFLs are annotated. This is shown in our first example (Supplementary Fig. S2A) where the boundaries of domains are slightly misaligned with the boundaries of DFLs. This will result in annotation noise that reduces the achievable limit of predictive performance. Our prediction is also characterized by a low runtime, slightly misaligned with the boundaries of DFLs. This will result in residue positions involved in conformational switches in proteins. Bioinformation, 3, 134–136.


