Gene expression

Reference point insensitive molecular data analysis


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Abstract

Motivation: In biomedicine, every molecular measurement is relative to a reference point, like a fixed aliquot of RNA extracted from a tissue, a defined number of blood cells, or a defined volume of biofluid. Reference points are often chosen for practical reasons. For example, we might want to assess the metabolome of a diseased organ but can only measure metabolites in blood or urine. In this case, the observable data only indirectly reflects the disease state. The statistical implications of these discrepancies in reference points have not yet been discussed.

Results: Here, we show that reference point discrepancies compromise the performance of regression models like the LASSO. As an alternative, we suggest zero-sum regression for a reference point insensitive analysis. We show that zero-sum regression is superior to the LASSO in case of a poor choice of reference point both in simulations and in an application that integrates intestinal microbiome analysis with metabolomics. Moreover, we describe a novel coordinate descent based algorithm to fit zero-sum elastic nets.

Availability and Implementation: The R-package “zeroSum” can be downloaded at https://github.com/rehbergT/zeroSum. Moreover, we provide all R-scripts and data used to produce the results of this manuscript as Supplementary Material.

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1 Introduction

The emergence of novel technologies and experimental protocols for molecular and cellular profiling of biological samples is continuously gaining speed for at least one decade and there is no end in sight. Every technology brings new computational challenges in the normalization and interpretation of the data produced. Nevertheless, many of these data types share common computational challenges. For example, the high dimensionality of profiles has established machine learning techniques including penalized regression models (Efron et al., 2004; Hastie et al., 2009; Hoerl and Kennard, 1970; Tibshirani, 1996) as standard tools of genomic data analysis.

In contrast, little attention has been given to the choice of reference points for measurements. Exemplary reference points include for example one microgram of RNA, all mRNA from 1 million cells, all metabolites in 1 ccm of blood, just to name a few. In a typical biomedical protocol, DNA, RNA or proteins are extracted from
specimens such as blood, urine or tissue and a fixed size aliquot of these molecules is profiled. In intestinal microbiome sequencing, for instance, DNA encoding for 16S rRNA genes are extracted, a fixed size aliquot of DNA is sequenced and the reads are mapped to taxonomic units. Here, the reference point is a fixed size aliquot of DNA.

Also, the difference between profiles relative to two reference points is not always small. For example, Lin et al. (2012) and Nie et al. (2012) have shown that inducing the expression of the transcription factor MYC causes transcriptional amplification, a global increase in transcription rates of all currently transcribed genes by a factor of 2–3, which can only be detected using the number of cells rather than a fixed amount of RNA as reference point. Similarly in the context of epigenomics, Orlando et al. (2014) report global changes in ChIPseq signals across experimental conditions. Reference points for measurements in tissue specimens like the weight, the volume, or the DNA content can be greatly and differentially affected by the cellular composition of the specimen or even by disease state (Bittner, 1967). In all these instances, changing the reference point changes the data including the correlations between molecular features. This will affect both statistical analysis and biological interpretation.

Reference points are closely linked to data normalization and preprocessing. Normalization changes the reference point. For example, if we normalize profiles to a common mean, we generate a data internal reference point. In this case, the data becomes quasi compositional. If in contrast we normalize to a constant value for one or several housekeeping features we choose another data internal reference point. In this case, the data becomes quasi compositional, looses this property.

Finally, sometimes it might not be possible to generate profiles for the relevant reference point. For instance, one may be interested in the effect that disease exerts on the concentration of metabolites in an organ. Unless one were to take a biopsy from the organ, such changes can only be determined indirectly by measuring the metabolites in biomedical specimens more readily available, such as blood, urine, feces or breath. How much of the metabolites in the organ make it into these specimens might differ from patient to patient. In this case, the reference point is unknown.

In summary, even with meticulous experimental designs the reference point can remain suboptimal or even obscure. In such cases, statistical analysis and biological interpretation should not depend on it. Lin et al. (2014) pioneered zero-sum regression as a tool for feature selection in high-dimensional compositional data. However, zero-sum regression is not limited to compositional data. In contrast, it provides the framework for a reference point insensitive data analysis.

Extending the work of Lin et al. (2014), we here show that zero-sum regression yields reference point insensitive models. We extend zero-sum regression to elastic net models and contribute a fast coordinate descent algorithm to fit zero-sum elastic nets. This algorithm is implemented as an R-package with crucial functions written in C to further reduce computing time. To the best of our knowledge, our tool is the first freely available R-package for reference point insensitive data analysis using zero-sum regression. Finally, we demonstrate the use of a reference point insensitive data analysis in an application that integrates intestinal microbiome analysis with metabolomics.

2 A strategy for reference point insensitive data analysis

Let $\mathbf{x}_i = (x_{i1}, \ldots, x_{ip})^T$ be data, where $i = 1, \ldots, N$ indicates the measurements and $\mathbf{x}_i$ the predictor variables. The corresponding responses are $y_i$ and $\mathbf{x}_i$ are conditionally independent. Changing the reference point from $\mathbf{x}_1$ to $\mathbf{x}_2$ yields the regression Equation (1). We call a regression model proportional reference point insensitive or PRP-insensitive, if the predictions $\hat{y}_i$ do not depend on the chosen reference point $r$. This is the case if the regression weights $\beta_j$ sum up to zero,

$$\sum_{j=1}^{p} \beta_j = 0 \, .$$

Note that the standard tool kit of linear regression analysis is sensitive to the reference point. This includes penalized methods like ridge regression (Hoerl and Kennard, 1970) or the LASSO (Tibshirani, 1996).

2.2 Zero-sum-regression is PRP-insensitive while the LASSO and the elastic net are not

The LASSO is a regularized linear regression model that still works for data with more features than samples where least squares estimates are no longer an option. It has the additional appeal that fitted models are sparse in the covariates. Covariates with non-zero coefficients can be interpreted as biologically important. Moreover, predictions can be calculated from only a few covariates. A LASSO model is estimated by minimizing

$$\frac{1}{2N} \sum_{i=1}^{N} (y_i - \beta_0 - \sum_{j=1}^{p} \beta_j x_{ij})^2 + \lambda \| \beta \|_1 \, ,$$

with respect to the coefficient vector $\beta = (\beta_1, \ldots, \beta_p)^T$ and the intercept $\beta_0$. Here $P(\| \beta \|_1)$ is a penalty term that implements a priori preference for sparse models. The tuning parameter $\lambda$ calibrates sparseness. If we replace the $L_1$ norm in the log-likelihood (4) by $P(\| \beta \|_1) = \sum_{j=1}^{p} (1 - x_j) / 2 |\beta_j|_1^2$, we have the log-likelihood of the elastic net (Zou and Hastie, 2005). For $x = 1$, this gives us the LASSO and for $x = 0$ the non-sparse ridge regression.
These models are only PRP-insensitive if the regression coefficients add up to zero. If the profiles are mean centered, the standard least squares estimates for \( \beta \) form a one dimensional subspace that includes the unique zero-sum estimate (see Supplementary Material). In other words, from all optimal solutions, we can simply choose one that is PRP-insensitive. Also ridge regression models automatically meet the zero-sum condition for centered profiles (see Supplementary Material). However, as we will see neither the LASSO nor the elastic net do.

Zero-sum regression (From now on we refer to an elastic-net fit with \( \alpha = 1 \) which respects the zero-sum constraint simply as zero-sum regression.) yields sparse PRP-insensitive models. For compositional high dimensional data, Lin et al. (2014) combined the zero-sum condition with the \( L_1 \) penalty of the LASSO. In their zero-sum regression, they minimize the penalized log-likelihood (4) under the constraint (3). Hence, unlike the standard LASSO or the elastic net, zero-sum regression models are always PRP-insensitive. Condition (3) uncouples \( \gamma_i \) from the reference points. Thus, the corresponding zero-sum estimates for \( \beta_0 \) and \( \beta \) are also reference point insensitive.

It is instructive to see that zero-sum models are driven by the ratios of features rather than the individual absolute features. In ratios, the reference points cancel. For illustration, consider a model with only two features \( x_1 \) and \( x_2 \) on log-scale. Then, the sum of squares becomes

\[
\sum_{i=1}^{N} (y_i - \beta_0 - \beta_1(x_1 - x_2))^2.
\]

Note that the zero-sum constraint turned \( x_1 - x_2 \) into the only predictor variable. Since \( x_1 - x_2 = \log(X_1/X_2) \), it is the ratio \( X_1/X_2 \) of the original data that drives the model.

### 2.3 The zero-sum elastic net

We next describe an extension of the coordinate descent (CD) algorithm for the elastic net (Friedman et al., 2007, 2010) that preserves the zero-sum constraint. The challenge is to solve:

\[
\min_{(\beta_0, \beta) \in \mathbb{R}^{p+1}} R_\lambda(\beta_0, \beta)
\]

subject to:

\[
\sum_{j=1}^{p} \beta_j = 0.
\]

We replace \( \beta_s = -\frac{1}{2} \sum_{j=1}^{p} \beta_j \), yielding

\[
R_\lambda(\beta_0, \beta) = \frac{1}{2N} \sum_{i=1}^{N} \left( y_i - \beta_0 - \sum_{j=1}^{p} \beta_j x_j \right)^2 + \frac{1}{2} \lambda \left( \sum_{j=1}^{p} \beta_j^2 \right)
\]

\[
+ \frac{1}{2} \lambda \left( \sum_{j=1}^{p} \left| \beta_j \right| \right) + \frac{1}{2} \lambda \left( \sum_{j=1}^{p} \left| \beta_j \right| \right)
\]
iterated K times. In general, both diagonal updates and polishing can improve the computed coefficients at the cost of computing time.

3 Simulations

3.1 There is a trade-off between the zero-sum bias and the PRP-sensitivity of the LASSO

Zero-sum regression is PRP-insensitive, while standard regression is not. But does this make a relevant difference in practice? It turns out that the relative performance of zero-sum regression and the standard LASSO strongly depends on the correlation structure of the predictors $x\mathbf{1} = \{x_1, x_2, \ldots, x_{500}\}^T$. To illustrate this, we use the following simulation of high dimensional sparse regressions. From a standard linear regression model, employing the coefficients summarized in Table 1, we generated four data sets with $N = 100$ samples each (20 training samples and 80 test samples). Every data set includes 500 predictors $x_1$, and a response variable $y$ that only depends on three of them. The regression coefficients are shown in Table 1. Note that with the exception of data set (d), the models do not fulfill the zero-sum condition. The noise $\epsilon_i$ was sampled independently from a normal distribution with mean zero and standard deviation $\sigma = 0.1$. The predictors $x_1, x_2, \ldots, x_{500}$ where drawn independently from a normal distribution with mean zero and standard deviation 0.5. For the first three predictors—those that define $y$—we allowed for different correlation structures in the four data sets via a Cholesky decomposition of the correlation matrix. For simulations (a) and (c), we have chosen $\text{cor}(x_1, x_2) = 0.9$, $\text{cor}(x_1, x_3) = 0.9$ and $\text{cor}(x_2, x_3) = 0.8$. While for scenario (b) we have chosen $\text{cor}(x_1, x_2) = -0.9$, $\text{cor}(x_1, x_3) = 0.9$ and $\text{cor}(x_2, x_3) = -0.8$. Hence, in (a), we have correlated predictors, while in (b) predictor $x_2$ is anti-correlated to predictor $x_1$ and $x_3$. For scenario (d), we have not imposed any a priori correlation structure. We call the predictors of this data set $X$.

Next, we simulated a change in the reference point by drawing random shifts $\gamma_i$ from a centered normal distribution with standard deviation $\sigma$. The larger the $\sigma$ the more the two reference points differ. The responses $y_i$ remain unchanged. We call the sample-wise shifted predictors $X'$. Note that $y$ is computed from $X$ in both data sets. $X$ represents the data relative to the reference point that matters, like the absolute amount of metabolites in renal proximal tubule cells, while $X'$ represents the data relative to a reference point that was practical to measure, like metabolite concentrations in a fixed volume of urine. We run both LASSO and zero-sum regression on both $X$ and $X'$ to study the trade-off between the benefit of reference point insensitivity and the cost of introducing a bias by the zero-sum constraint. The sparseness parameter $\lambda$ was optimized via cross validation (Friedman et al., 2010). For obtaining the standard Lasso penalized models, we employed the well-established R-package glmnet (Friedman et al., 2010).

We first compare zero-sum regression and the LASSO with respect to the accuracy of predictions (Fig. 1). Every plot shows the coefficient of determination $R^2$ as a function of $\sigma$, cf. Supplementary Material Figure S1 for the corresponding mean-squared errors (MSE). Hence, on the left, we compare the performance of the LASSO and zero-sum regression for small changes of reference point, while on the right we compare it for large changes. Zero-sum regression is not affected by the change in reference point. Its performance is shown by the dashed horizontal lines. In contrast, LASSO is sensitive to the choice of $\gamma_i$ and yields different performances for each simulation run. The median of this distribution is shown by the solid lines while the 25–75%, 5–95% and 1–99% percentiles of the distribution are shown by dark, medium and light bands, respectively. Depending on the correlation structure and the choice of the $\gamma_i$ zero-sum or the standard LASSO are more accurate. (a) In these simulations, the three relevant predictors, $j = 1, \ldots, 3$, are highly correlated, the coefficients $\beta_j$ do not fulfill the zero-sum condition but vary in sign and size. For small $\sigma$, zero-sum regression is inferior to the LASSO, but with increasing $\sigma$ zero-sum regression outperforms the LASSO. We also observed several simulations where the classical LASSO breaks down completely yielding $R^2$ values nearly zero. (b) This simulation is based on the same set of coefficients as scenario (a), but now the predictor $x_2$ is anti-correlated to $x_1$ and $x_3$. In spite of the change of reference point and the unbalanced coefficients both the LASSO and zero-sum regression work accurately. However, for large $\sigma$ the classical LASSO frequently looses predictive power and zero-sum regression is more reliable, even if the differences between the methods is much smaller than for scenario (a). (c) Here, we have only positive coefficients $\beta_j > 0$, which potentially spoils the zero-sum constraint. Note that the correlations are imposed as in scenario (a). Thus, we can directly study the consequences of changing the constants $\beta_j$ to a scenario which more substantially violates the zero-sum condition. Interestingly, we qualitatively observe a similar trade-off between zero-sum bias and PRP-sensitivity as in the previous scenarios. (d) Here, the $\beta_j$ add-up to zero and no correlations are imposed on the predictor variables. Thus, for this scenario, the zero-sum constraint is not a bias. Clearly, zero-sum works perfectly, while the LASSO breaks down rapidly in many of the simulations. In summary, zero-sum regression tends to outperform the LASSO for $\gamma$ that are relatively large. More importantly, in several scenarios, we observed a complete breakdown of the LASSO but never for zero-sum regression.

Table 1. Summary of the simulation scenarios (a) to (d). Shown are the coefficients $\beta_j$ for $j = 1, \ldots, 500$ and the imposed correlations.

<table>
<thead>
<tr>
<th>Sim.</th>
<th>$\beta_1$</th>
<th>$\beta_2$</th>
<th>$\beta_3$</th>
<th>$\beta_4 \cdot \beta_500$</th>
<th>$\text{cor}(x_1, x_2)$</th>
<th>$\text{cor}(x_1, x_3)$</th>
<th>$\text{cor}(x_2, x_3)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a)</td>
<td>1</td>
<td>-1</td>
<td>3</td>
<td>0</td>
<td>0.9</td>
<td>0.9</td>
<td>0.8</td>
</tr>
<tr>
<td>(b)</td>
<td>1</td>
<td>-1</td>
<td>3</td>
<td>0</td>
<td>-0.9</td>
<td>0.9</td>
<td>-0.8</td>
</tr>
<tr>
<td>(c)</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>0</td>
<td>0.9</td>
<td>0.9</td>
<td>0.8</td>
</tr>
<tr>
<td>(d)</td>
<td>1</td>
<td>-2</td>
<td>1</td>
<td>0</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

Fig. 1. Shown are the coefficients of determination, $R^2$ between observed and predicted responses, for the simulation studies (a) to (d) as a function of $\sigma$, where $\sigma$ is the standard deviation of the sample-specific shifts $\gamma_i$. The median over all simulation runs is the dashed line for zero-sum regression and the solid line for LASSO. The dark, medium and light bands correspond to the LASSO and represent the 25–75%, 5–95% and 1–99% percentiles of the $R^2$ distribution obtained from drawing 1000 sets of $\gamma_i$. The very narrow zero-sum bands are only visible as a line.
3.2 LASSO predictions change, if the reference point changes. Zero-sum predictions do not
While it is a priori not clear, whether a zero-sum or a LASSO model is more accurate, zero-sum models always have the advantage that predictions are reference point insensitive. In contrast, a LASSO model can be dominated by the reference point. To show the extend of PRP sensitivity of the LASSO, we compared predictions before and after changing the reference point ($\sigma = 0$ versus $\sigma \neq 0$), i.e. we compare $\hat{y}_{\sigma=0}$ to $\hat{y}_{\sigma\neq0}$, while in the previous section we compared $\hat{y}_{\sigma=0}$ to $\hat{y}$.

We used the same four simulation scenarios as in the previous section. Figure 2 summarizes the results. By definition, both predictions agreed for zero-sum regression, yielding a mean-squared error of 0, or perfect reproducibility. In contrast, for the LASSO we saw several simulations in all four scenarios where predictions vastly diverge upon changing the reference point.

3.3 Zero-sum regression facilitates reference point independent feature selection more reliably than the LASSO
Besides prediction, feature selection is an important application of sparse regression models. If we use the LASSO, selected features depend on the reference point, if we use zero-sum they do not. In Figure 3, we show areas under the receiver operating characteristic (ROC) curve versus $\sigma$. Again we used the scenarios (a) to (d) described above. In scenarios (b) to (d), zero-sum recovered the three driving features perfectly and so did the LASSO for the majority of simulations. However, in few simulations, the LASSO picked incorrect features. In scenario (a), we never reached perfect feature selection. Nevertheless, zero-sum regression proved again to be more reliable. Note that an area under the curve (AUC) of 0.5 corresponds to random feature selection and in a few simulations the LASSO was not better than that. In summary, zero-sum regression selected relevant features as accurate as the LASSO. In few simulations, the LASSO broke down due to change of reference point.

4 An application of zero-sum regression to genomic data integration: identifying intestinal bacterial communities associated with indole production
In this section, we show reference point insensitive data analysis at work. We chose a study that combined intestinal microbiome sequencing with metabolome analysis of urine in patients undergoing bone marrow transplantation. Different reference points apply to the intestine, the stool and the urine of patients.

About 40% of patients receiving allogeneic stem cell transplants (ASCT) develop a systemic acute graft versus host disease (Ferrara et al., 2009). About 54% of these diseases affect the gastrointestinal tract (Martin et al., 1990). This complication was associated with the intestinal microbiome composition (Holler et al., 2014; Taur et al., 2012) and with the presence of toxic or the absence of protective microbiota born metabolites in the gut (Murphy and Nguyen, 2011). A candidate protective substance is the tryptophan microbial fermentation product indole (Weber et al., 2015). It reduces epithelial attachment of pathogenic bacteria, promotes epithelial restitution and, simultaneously, inhibits inflammation (Bansal et al., 2010; Zelante et al., 2013).

Weber et al. (2015) studied associations between the microbiome composition of ASCT patients during treatment and urinary 3-indoxyl sulfate (3-IS) levels. 3-IS is a metabolite of indole produced in the colon and liver. In this study, it was quantified in patient urine by liquid chromatography/tandem mass spectrometry. The intestinal microbiomes of the same patients were profiled by sequencing the hypervariable V3 region of the 16S ribosomal RNA gene in patient feces and mapping the sequences to operational taxonomic units (OTUs). ASCT patients receive antibiotics, which might kill indole producing bacteria thus damaging the intestine. If one identified the indole producing bacteria in the gut, one could choose antibiotics that spare them. As a first step towards this goal, we strive to identify a small set of OTUs that are jointly associated with 3-IS levels.

This biomedical challenge defines a sparse high dimensional regression problem. And, it is a regression problem where the choice of reference points matters. The reference point of the microbiome profiles is a fixed size aliquot of 16S rDNA obtained from bacteria in patient feces. The reference point that links the microbiome to 3-IS levels is patient intestines. If there are more indole secreting bacteria in the intestine, we expect more 3-IS in the urine. The total number of microbiota in patient intestines vary strongly due to diet and treatments including antibiotics. We thus expect that compositional microbiome data poorly reflects absolute microbiota abundances in the intestines. In summary, the regression problem calls for absolute bacterial abundances in patient intestines, while the available profiles provide only relative abundances. Obviously, the reference points do not match.

In total, we analyzed 37 matched pairs of stool and urine specimens. Urinary 3-IS was quantified by liquid chromatography tandem mass spectrometry (LC-MS/MS). To control for variations in
urine flow rate, we normalized the measured concentration of 3-IS against the measured urinary concentration of creatinine (Waikar et al., 2010), which was also determined by LC-MS/MS. The intestinal microbiome was profiled by next-generation sequencing of the V3 hypervariable region of the 16S rRNA gene. Prior to DNA extraction of the stool samples, three exogenous bacteria (Salinibacter ruber, Rhizobium radiobacter and Alicyclobacillus acidiphilus) were spiked into crude specimens as external controls. Subsequently, a constant aliquot of PCR amplified 16S rDNA was sequenced. Reads were assigned to 160 bacterial genera, one pseudo count was added and the counts were log2 transformed. Finally, the genera where quantified relative to two different reference points:

i. We normalized the data sample-wise to a constant average of all genera. This is equivalent to centering the data, cf. supplement.

ii. We normalized the data to a constant average value of the 3 external standards.

Data (i) is library-size normalized (on log scale) and is thus the standard compositional microbiome. The reference point is a fixed size aliquot of 16S rDNA. This data does not reflect changes in the total microbial load of the stool. Data (ii), in contrast, is sensitive to changes in microbial load because in a fixed aliquot of 16S rDNA more endogenous sequences lead to proportionally less spike-in sequences. Here the reference point is a fixed size aliquot of stool.

We run the LASSO and zero-sum regression on both microbiome data sets with log2 transformed urinary creatinine normalized 3-IS values as response variable y. 3-IS levels were predicted in leave one out cross validation and the predictions were compared to the measured values. By definition, zero-sum produces the same predictions for both datasets because of its PRP insensitivity.

Figure 4 compares cross validated mean-squared errors of zero-sum regression with that of the LASSO for library-size normalized data and spike-in calibrated data as a function of the LASSO sparsity parameter λ. The optimal mean-squared errors are similar with zero-sum regression yielding the smallest error. More important in this application is the selection of features. Figure 5 summarizes our results, i.e. the selected features and the corresponding coefficients obtained in 37 models learned in a leave-one-out cross validation. Figure 5a shows how often a feature was selected. Features selected by the LASSO depended on the chosen reference point. For example, Bifidobacterium was frequently selected when the reference point was the library size but hardly ever, when the reference point was an external standard. Also when a feature was reproducibly selected for both reference points like the genus Staphylococcus, its regression coefficients can drastically differ depending on the reference point. Figure 5b shows the difference of regression weights for the two reference points. In theory, zero-sum regression should not be affected at all by the change in reference point. Indeed, this is observed in Figure 5c. Finally, Figure 5d contrasts the regression coefficients of the LASSO with that of zero-sum regression. Interestingly unlike the LASSO, zero-sum regression picked the genus of one of the external standards, Alicyclobacillus, with a high negative weight. It thus automatically built its own reference point.

We tested if zero-sum regression retains its predictive power in the absence of external reference points. To this end we removed the three reference bacteria, Salinibacter ruber, Rhizobium radiobacter and Alicyclobacillus acidiphilus, from the dataset and re-performed our analysis, cf. Supplementary Figures S2 and S3. The lowest MSE observed in leave-one-out cross validation was 10.86. This error is again lower for zero-sum regression than for the two LASSO models. In fact, it is even slightly lower than the error of the zero-sum regression with the spike-ins.

In summary, zero-sum regression stabilized feature selection compared to the LASSO. LASSO features greatly depended on the chosen reference point, zero-sum features did not. Zero-sum regression selects features that are predictive of urinary 3-IS independent of the reference point.

5 Discussion
Here, we discussed the problem of reference point dependence in the analysis of omics data and exemplified its relevance both in a simulation study and in an application on integrating urinary metabolome data with intestinal microbiome compositions. We recommend zero-sum regression as a method that can overcome the problem. In this context, we contribute a coordinate descent algorithm for fitting zero-sum regression models and provide the first R-package for this type of analysis.

Our theoretical analysis is restricted to reference point changes that yield proportional data. On log-transformed data these proportional reference point changes are fully described by the sample specific shifts we discussed. Of course a reference point change can be more complicated leading to non-linear distortions. In this case, zero-sum regression is no longer reference point independent. However, it might nevertheless be worth testing its performance, since it can still cushion the reference point, if the transformation systematically affects the sample mean.

We believe that there is a wide spectrum of high content profiling methods where changes or ambiguities of reference points exist and matter. It ranges from gene and protein expression, via metabolomics, epigenetic readouts, microbiome sequencing and metagenomics, to very recent advances in digital immune cell quantifications. More and more studies integrate several of these data types. Likely, the reference points differ between them. Also, the integration of new data with published data that can be downloaded from public repositories can greatly enhance analysis and interpretation. However, the reference points of the published data might not even be sufficiently clear from the documentation of the data files. We believe that in all these scenarios a reference point insensitive analysis is called for.
Finally, what does it mean, when we routinely say that a gene is up-regulated between control and treatment? These genes can be up-regulated with respect to one reference point but down-regulated with respect to another. A reference point insensitive analysis cannot resolve this question, only meticulous distinction between reference points can. However, if we strive for more general statements like: ‘Gene A is up-regulated’, we argue that these statements should at least be supported by a reference point independent analysis.

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Conflict of Interest: none declared.

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