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# Teaching Computational Thinking

## An Integrative Approach for Middle and High School Learning

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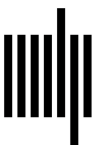
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## Appendix: Computer Programs

This chapter contains full versions of programs that appear throughout the text. Programs are presented in Processing (see [www.processing.org](http://www.processing.org)), Codesters, and Python.

### A.1 Drawing Cretan Labyrinths

The following Processing program draws a seven-circuit Cretan labyrinth on a computer screen, as shown in figure 4.7.

```
// file: labyrinth.pde
// Draws a seven-circuit Cretan labyrinth in two colors.
// Author: Robert R. Snapp

float t=0;
float dt=0.5;
Pvector last1;
Pvector last2;
Pvector pv1;
Pvector pv2;

void drawCross() {
  line(10, -80, 10, 0);
  line(-30,-40, 50, -40);
  arc(50,0,40,40, radians(180), radians(360));
  arc(-30,0,40,40, radians(180), radians(360));
  arc(-30,-80,40,40, radians(-90), radians(90));
  arc(50,-80,40,40, radians(90), radians(270));
}

void drawUpperArc(float r) {
  arc(0,0,r,r,0, radians(180));
}

void drawSWQuarter(float r) {
  arc(-30, 0, r, r, radians(180), radians(270));
}
```

```
void drawSEQuarter(float r){
    arc(50, 0, r, r, radians(270), radians(360));
}

void vbranch(float t, Pvector pv) {
    float rad=radians(t);
    if (t <= 0) {
        pv.x=50;
        pv.y=0;
    } else if (t <= 180) {
        pv.x=50*cos(rad);
        pv.y=50*sin(rad);
    } else if (t <= 360) {
        pv.x=20*cos(rad)-30;
        pv.y=20*sin(rad);
    } else if (t <= 540) {
        pv.x=-10*cos(rad);
        pv.y=10*sin(rad);
    } else if (t <= 630) {
        pv.x=10.0;
        pv.y=-40.0*(t-540)/90.;
    } else if (t <= 720) {
        pv.x=10.0;
        pv.y=-40*(t-630)/90.-40;
    } else if (t <= 810) {
        pv.x=-30+40*cos(rad);
        pv.y=-80-40*sin(rad);
    } else if (t <= 900) {
        pv.x=-30+120*cos(rad);
        pv.y=-120*sin(rad);
    } else if (t <= 1080) {
        pv.x=150*cos(rad);
        pv.y=-150*sin(rad);
    } else if (t <= 1170) {
        pv.x=50+100*cos(rad);
        pv.y=-100*sin(rad);
    } else if (t <= 1350) {
        pv.x=50+20*cos(rad);
        pv.y=-80-20*sin(rad);
    } else if (t <= 1440) {
        pv.x=50+60*cos(rad);
        pv.y=60*sin(rad);
    } else if (t <= 1620) {
        pv.x=110*cos(rad);
        pv.y=110*sin(rad);
    } else if (t <= 1710) {
        pv.x=-30+80*cos(rad);
        pv.y=80*sin(rad);
    } else {
```

```
        pv.x=-30;
        pv.y=-80;
    }
}

void hbranch(float t, Pvector pv) {
    float rad=radians(t);
    if (t <= 0) {
        pv.x=-30;
        pv.y=0;
    } else if (t <= 180) {
        pv.x=-30*cos(rad);
        pv.y=30*sin(rad);
    } else if (t <= 360) {
        pv.x=20*cos(rad)+50;
        pv.y=20*sin(rad);
    } else if (t <= 540) {
        pv.x=70*cos(rad);
        pv.y=70*sin(rad);
    } else if (t <= 630) {
        pv.x=40*cos(rad)-30;
        pv.y=40*sin(rad);
    } else if (t <= 720) {
        pv.x=40*(t-630)/90.-30;
        pv.y=-40;
    } else if (t <= 810) {
        pv.x=40*(t-720)/90.+10;
        pv.y=-40;
    } else if (t <= 900) {
        pv.x=50-40*cos(rad);
        pv.y=-40*sin(rad);
    } else if (t <= 1080) {
        pv.x=-90*cos(rad);
        pv.y=-90*sin(rad);
    } else if (t <= 1170) {
        pv.x=-30-60*cos(rad);
        pv.y=-60*sin(rad);
    } else if (t <= 1350) {
        pv.x=-30-20*cos(rad);
        pv.y=-80+20*sin(rad);
    } else if (t <= 1440) {
        pv.x=-30-100*cos(rad);
        pv.y=100*sin(rad);
    } else if (t <= 1620) {
        pv.x=-130*cos(rad);
        pv.y=130*sin(rad);
    } else if (t <= 1710) {
        pv.x=50-80*cos(rad);
        pv.y=80*sin(rad);
    }
}
```

```

    } else {
        pv.x=50;
        pv.y=-80;
    }
}

void setup() {
    size(900,900);
    frameRate(480);
    smooth();
    background(240);

    last1=new PVector(0,0);
    last2=new PVector(0,0);
    pv1=new PVector(0,0);
    pv2=new PVector(0,0);
    vbranch(1710, last1);
    hbranch(1710, last2);
    vbranch(1710, pv1);
    hbranch(1710, pv2);
}

void draw() {
    translate(width/2, height/2);
    scale(2.5,-2.5);

    vbranch(1710-t, pv1);
    hbranch(1710-t, pv2);

    strokeWeight(3);
    stroke(200,0,0);
    line(pv1.x, pv1.y, last1.x, last1.y);
    last1=pv1;

    stroke(150, 150, 255);
    line(pv2.x, pv2.y, last2.x, last2.y);
    last2=pv2;

    t += dt;
}

```

## A.2 Bumper Rocks

The following program is coded in Codesters to simulate elastic collision, as seen in figure 5.8.

```

# Author: Lisa Dion
# set the background image
stage.set_background("jupiter")

```

```
# create the rock with initial size and speed
rock=codesters.Sprite("rock")
rock.set_size(0.5)
rock.set_x_speed(2)
rock.set_y_speed(-3)

# create the asteroid with initial size, position, and speed
asteroid=codesters.Sprite("asteroid")
asteroid.set_size(0.5)
asteroid.go_to(-200, 0)
asteroid.set_x_speed(-1)
asteroid.set_y_speed(4)

# create a function for the "s" key to make the rock smaller
def s_key():
    # make the rock smaller
    rock.set_size(0.8)
# this line makes the code listen for the "s" key
stage.event_key("s", s_key)

# create a function for the "w" key to make the rock larger
def w_key():
    # make the rock bigger
    rock.set_size(1 / 0.8)
# this line makes the code listen for the "w" key
stage.event_key("w", w_key)

# create a function for collision of the objects
def collision(sprite, hit_sprite):
    # set variables
    size_sum=rock.get_size()+asteroid.get_size()
    x_vel_1=sprite.get_x_speed()
    x_vel_2=hit_sprite.get_x_speed()
    y_vel_1=sprite.get_y_speed()
    y_vel_2=hit_sprite.get_y_speed()
    rock_x=rock.get_x()
    rock_y=rock.get_y()
    asteroid_x=asteroid.get_x()
    asteroid_y=asteroid.get_y()
    # calculate the new velocities for 2-dimensional elastic collisions
    # the following 4 command lines are each on their own line
    sprite.set_x_speed(x_vel_1-((2*asteroid.get_size())/size_sum) *
((x_vel_1-x_vel_2)*(rock_x-asteroid_x) + (y_vel_1-y_vel_2)*(rock_y-
asteroid_y)) / ((rock_x-asteroid_x)*(rock_x-asteroid_x) + (rock_y-
asteroid_y)*(rock_y-asteroid_y)) * (rock_x-asteroid_x))
    sprite.set_y_speed(y_vel_1-((2*asteroid.get_size())/size_sum) *
((x_vel_1-x_vel_2)*(rock_x-asteroid_x) + (y_vel_1- y_vel_2)*(rock_y-
asteroid_y)) / ((rock_x-asteroid_x)*(rock_x-asteroid_x) + (rock_y-
asteroid_y)*(rock_y-asteroid_y)) * (rock_y- asteroid_y))
```

```

    hit_sprite.set_x_speed(x_vel_2-((2*rock.get_size())/size_sum) *
((x_vel_2-x_vel_1)*(asteroid_x-rock_x)+(y_vel_2- y_vel_1)*(asteroid
_y-rock_y)) / ((rock_x-asteroid_x)*(rock_x-asteroid_x)+(rock_y-
asteroid_y)*(rock_y-asteroid_y)) * (asteroid_x-rock_x))
    hit_sprite.set_y_speed(y_vel_2-((2*rock.get_size())/size_sum) * ((x
_vel_2-x_vel_1)*(asteroid_x-rock_x)+(y_vel_2-y_vel_1)*(asteroid_y-
rock_y)) / ((rock_x-asteroid_x)*(rock_x-asteroid_x)+(rock_y-asteroid
_y)*(rock_y-asteroid_y)) * (asteroid_y-rock_y))

# this line makes the program detect collision and
# call the function above
rock.event_collision(collision)

# create a function to move the objects and bounce off walls
def move(sprite):
    sprite.move_forward(1)
    if sprite.get_x() >= 250 or sprite.get_x() <= -250:
        sprite.set_x_speed(-sprite.get_x_speed())
    if sprite.get_y() >= 250 or sprite.get_y() <= -250:
        sprite.set_y_speed(-sprite.get_y_speed())

# have the program run forever
while True:
    move(rock)
    move(asteroid)

```

### A.3 Basketball

The following program is coded in Codesters to simulate the physics involved in shoot-  
ing a basketball, as seen in figure 5.9.

```

# Author: Lisa Dion
# set gravity's strength
stage.set_gravity(10)
stage.set_background("halfcourt")
net=codesters.Sprite("basketballnet", 200, 100)
# we do not want the net to fall
net.set_physics_off()
net.set_gravity_off()
player=codesters.Sprite("player3", -180, -130)
# we do not want the player to fall
player.set_physics_off()
player.set_gravity_off()
ball=codesters.Sprite("basketball", -150, -130)
# we do not want the ball to fall yet
ball.set_physics_off()
ball.set_gravity_off()
# create a rectangle along the floor

```

```

floor=codesters.Rectangle(0, -250, 500, 10, "red")
# create a function called shoot
def shoot(x_speed, y_speed):
    # set the ball's speed to make it move
    ball.set_x_speed(x_speed)
    ball.set_y_speed(y_speed)

# create a function for collisions
def collision(sprite, hit_sprite):
    # check for a score
    # the next two lines should be on one line of code
    if sprite.get_x() >= 165 and sprite.get_x() <= 215 and sprite.
get_y() >= 75 and sprite.get_y() <= 100 and sprite.get_y_speed() < 0:
    # stop the ball
    sprite.set_x_speed(0)
    sprite.set_y_speed(0)
    sprite.set_physics_off()
    sprite.set_gravity_off()
    # create a win message
    message=codesters.Text("You scored!", 0, 0, "white")
# check if the ball hit the red floor
elif hit_sprite.get_color() == "red":
    # stop the ball
    sprite.set_x_speed(0)
    sprite.set_y_speed(0)
    sprite.set_physics_off()
    sprite.set_gravity_off()
    # create a lose message
    message=codesters.Text("Try again!", 0, 0, "white")

ball.event_collision(collision)

# prompt the player for inputs
x_vel=int(player.ask("Enter an x-velocity:"))
y_vel=int(player.ask("Enter a y-velocity:"))
# now we want the ball to fall
ball.set_physics_on()
ball.set_gravity_on()
# this calls the function above
shoot(x_vel, y_vel)

```

#### A.4 Ping-pong

The following program is written in Codesters to demonstrate reflection, as discussed in section 5.3.

```

# Author: Lisa Dion
# import the random number generator library module
import random

```



```
# set a list of speeds that we will choose from
speeds = [-4, -3, 3, 4]
# create the ball and set initial values
ball = codesters.Circle(0, 0, 50, "green")
ball.set_size(0.5)
# set the ball velocity in x and y components
ball.set_x_speed(speeds[random.randint(0, len(speeds)-1)])
ball.set_y_speed(speeds[random.randint(0, len(speeds)-1)])
# create rectangles for the paddles
# sprite=codesters.Rectangle(x, y, width, height, "color")
player1 = codesters.Rectangle(-230, 0, 10, 50, "yellow")
player2 = codesters.Rectangle(230, 0, 10, 50, "gray")
# create rectangles against the left and right walls
left_wall = codesters.Rectangle(-250, 0, 10, 500, "red")
right_wall = codesters.Rectangle(250, 0, 10, 500, "red")

# create a function for when "w" is pressed
def w_key():
    # make sure there is room to move up
    if player1.get_y() < 220:
        player1.move_up(20)

# create a function for when "s" is pressed
def s_key():
    # make sure there is room to move down
    if player1.get_y() > -220:
        player1.move_down(20)

# create a function for when up is pressed
def up_key():
    # make sure there is room to move up
    if player2.get_y() < 220:
        player2.move_up(20)

# create a function for when down is pressed
def down_key():
    # make sure there is room to move down
    if player2.get_y() > -220:
        player2.move_down(20)

# make the program listen for the keys
stage.event_key("s", s_key)
stage.event_key("w", w_key)
stage.event_key("up", up_key)
stage.event_key("down", down_key)

# create a function to detect collision
def collision(sprite, hit_sprite):
    # make ball bounce off paddles by changing its x-direction
```

```

ball.set_x_speed(-ball.get_x_speed())
# check if the ball hit the left or right wall
if hit_sprite.get_color() == "red":
    # stop the ball
    ball.set_x_speed(0)
    ball.set_y_speed(0)
    if hit_sprite.get_x() < 0:
        # ball hit left wall.
        msg=codesters.Text("Player 2 wins!", 0, 0, "red")
    else:
        # ball hit right wall.
        msg=codesters.Text("Player 1 wins!", 0, 0, "red")
# make the program listen for collisions
ball.event_collision(collision)

```

### A.5 Reading Temperatures from a File

The following program is written in Python to read from a file and graph average January temperatures for Burlington, Vermont, as seen in figure 6.19.

```

# Author: Lisa Dion
# Import the csv library so we can read in from a csv file
import csv
# Import matplotlib so we can graph the data
import matplotlib.pyplot as plt
# Import numpy so we can fit a line to the data
from numpy.polynomial.polynomial import polyfit

# Use January as the month to graph
month_string='01'

# Open the csv file
with open('BurlingtonVTData.csv') as csv_file:
    # Use the reader from the csv library
    reader=csv.reader(csv_file, delimiter=',')
    # Declare an empty list for all the months' temps for
    # the best fit line
    all_avg_month_temps=[]
    # Declare empty lists to hold what will be the x and y
    # values to graph
    years=[]
    graph_temps=[]
    # Skip the header line
    next(reader)
    # For each line of data in the file
    for row in reader:
        # Add the average temperature to the list
        all_avg_month_temps.append(float(row[3]))
        # If the month matches the month to graph

```

```

    if row[2][-2:] == month_string:
        # Add the year and the average temperature to the
        # lists to graph
        years.append(int(row[2][0:4]))
        graph_temps.append(float(row[3]))

# Use matplotlib to graph the data
ax=plt.subplot(111)
ax.plot(years, graph_temps)
# Only print every tenth year on x-axis
ax.xaxis.set_major_locator(plt.MaxNLocator(10))
# Make sure y-axis starts at 0
ax.set_ylim(bottom=0)
ax.hlines([5, 10, 15, 20, 25, 30], 1940, 2019)
# Label graph and axes
plt.gcf().canvas.set_window_title('BVT January Temperatures')
plt.title('Average January Temperatures for Burlington, VT')
plt.xlabel('Year')
plt.ylabel('Average January Temperature (F)')

# Use numpy to calculate the best fit line to graph
b_graph, m_graph=polyfit(years, graph_temps, 1)
# Calculate coordinates from the line's y and b values
line_y_values=[]
for value in years:
    line_y_values.append(value * m_graph+b_graph)
# Plot the line on the graph
plt.plot(years, line_y_values, '-')

# Use numpy to calculate the best fit line on all the data
# The next command should be on one line
b_all, m_all=polyfit(range(len(all_avg_month_temps)),
all_avg_month_temps, 1)
# Calculate the temperatures of the first and last month
print('First month temp (F):', b_all)
# The next command should be on one line
print('Last month temp(F):', (len(all_avg_month_temps)-1)
* m_all+b_all)
print ('Slope of best fit line:', format(m_all, '.5f'))

# Display the graph in a new window
plt.show()

```

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