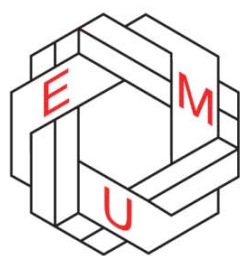


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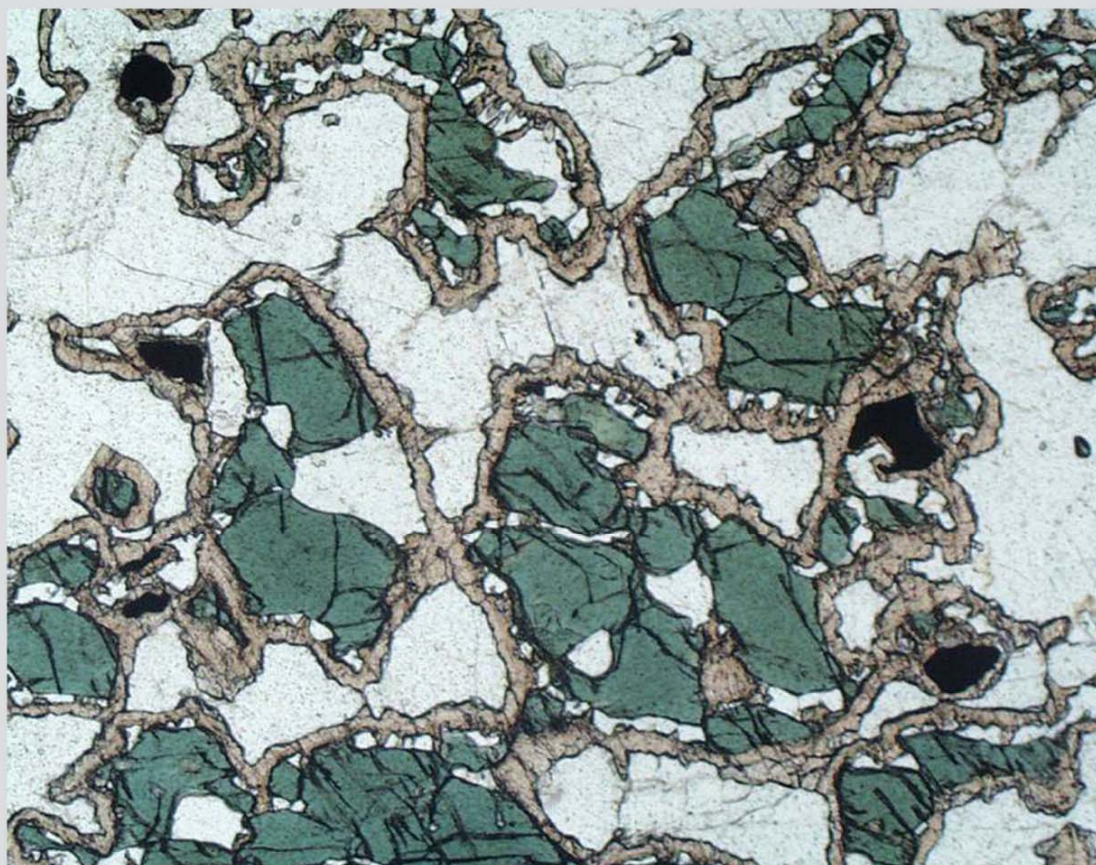
EMU NOTES IN  
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**16**

# Mineral reaction kinetics: microstructures, textures, chemical and isotopic signatures

Editors

WILHELM HEINRICH and RAINER ABART



THE MINERALOGICAL SOCIETY OF GREAT BRITAIN & IRELAND

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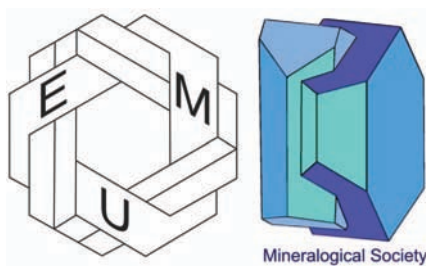
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Volume 16

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MICROSTRUCTURES, TEXTURES,  
CHEMICAL AND ISOTOPIC  
SIGNATURES**

UNIVERSITY TEXTBOOK

Edited by  
W. HEINRICH and R. ABART



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*On the front cover:* Transmitted-light image of coronitic metagabbro from the Precambrian crystalline basement complex of the Eastern Ghats in Orissa, India. During granulite-facies overprint of a gabbro protolith, (pinkish) garnet rims ~20 µm wide formed along the interfaces between pre-existing hedenbergite (green) and plagioclase (transparent) grains. Quartz is present as a discontinuous rim along garnet/hedenbergite interfaces. Sample and image courtesy of Prof. Michael Raith, University of Bonn, Germany.

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