Estimating differential expression from multiple indicators

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ABSTRACT

Regardless of the advent of high-throughput sequencing, microarrays remain central in current biomedical research. Conventional microarray analysis pipelines apply data reduction before the estimation of differential expression, which is likely to render the estimates susceptible to noise from signal summarization and reduce statistical power. We present a probe-level framework, which capitalizes on the high number of concurrent measurements to provide more robust differential expression estimates. The framework naturally extends to various experimental designs and target categories (e.g. transcripts, genes, genomic regions) as well as small sample sizes. Benchmarking in relation to popular microarray and RNA-sequencing data-analysis pipelines indicated high and stable performance on the Microarray Quality Control dataset and in a cell-culture model of hypoxia. State-of-the-art high-density microarrays such as Affymetrix GeneChip® and Exon arrays produce millions of probe-level signals representing most of the transcriptome. Although it is desirable to make optimal use of this rich information, the appearance of modern high-density microarrays has not led to the establishment of dedicated analysis methodologies. On one hand, thousands of genes are interrogated simultaneously making it possible to ‘borrow’ information across genes when estimating differential expression (DE) (5). On the other hand, as each gene is interrogated dozens of times replicated measurements can be integrated to yield a more robust DE estimate. As a novel insight, hypothermia-dependent up-regulation of multiple genes of two major antioxidant pathways was identified and verified by quantitative real-time PCR.

INTRODUCTION

Regardless of the advent of high-throughput sequencing, microarrays remain central in current biomedical research, as their maturity arguably enables more accurate transcriptional profiling in some situations (1,2) and facilitated analysis due to lower data volume. As microarrays continue to be a cost-effective tool for probing large-scale gene expression, they are likely to remain the method of choice in focused clinical and diagnostic settings not seeking to identify novel sequence variants. Moreover, public databases such as ArrayExpress and Gene Expression Omnibus (3,4) contain microarray data from tens of thousands of experiments and this vast data source will remain uncontested by sequencing datasets in the coming years. State-of-the-art high-density microarrays such as Affymetrix GeneChip® and Exon arrays produce millions of probe-level signals representing most of the transcriptome. Although it is desirable to make optimal use of this rich information, the appearance of modern high-density microarrays has not led to the establishment of dedicated analysis methodologies. On one hand, thousands of genes are interrogated simultaneously making it possible to ‘borrow’ information across genes when estimating differential expression (DE) (5). On the other hand, as each gene is interrogated dozens of times replicated measurements can be integrated to yield a more robust DE estimate. As a rule, however, probe-level information is summarized into probe-set values precluding its use directly in computing DE estimates (6). Such practice is not optimal as the number of variables available for inferring DE is reduced, which, in turn, can lead to the reduction in statistical power. This issue can become critical when the number of replicates per treatment is small as in most microarray experiments.

Here, we introduce a novel DE analysis methodology designed to take advantage of the high number of concurrent measurements provided by high-density microarrays. The estimation of DE is central to the study of gene expression and, usually, the term is used to refer to a statistically significant difference in the experimentally
determined abundance of an mRNA species between two treatments (7,8). We propose a generalized framework, which naturally extends to many target categories (e.g. transcripts, genes, genomic regions, etc.) with DE referring to any statistically significant response of interest. We demonstrate that the proposed methodology is robust and versatile in terms of handling small sample sizes and different experimental designs.

Given multiple probes per target, an intuitively appealing approach would be to treat probes as voters. As a result, each target can receive between \( n_i \) and 0 votes in favor of DE, where \( n_i \) is the number of probes specific to target \( i \). As \( n_i \) varies substantially, a practical measure of DE would be \( r_i = \frac{X_i}{n_i} \), where \( X_i \) is the number of differentially expressed probes specific to target \( i \). Testing for the alternative hypothesis \( r_i > r_{\text{reference}} \) where \( r_{\text{reference}} = \frac{X-X_i}{n-n_i} \) with \( X \) and \( n \) representing the total number of differentially expressed probes and the total number of probes on the array, respectively, involves the pooling of information from all probes to produce a target-specific estimate of DE. A test for the enrichment of target-specific DE is robust and versatile in terms of handling small sample sizes and practical as the user is more likely to be interested in small differences when comparing inherently similar samples. For example, as DEMI was designed specifically for estimating DE, currently, the accompanying software does not produce target-specific estimates of expression level.

**MATERIALS AND METHODS**

**DEMI software**

The accompanying software is available at http://biit.cs.ut.ee/demi.

**DEMI algorithm**

DEMI is a probe-level framework to test for DE in microarray data. By design, it takes advantage of the fact that modern high-density microarray platforms each target sequence is interrogated by many complementary probe sequences. The workflow consists of three-steps: (i) normalization of raw signal intensities, (ii) evaluation of probe-level signal dynamics and (iii) estimation of DE of the target in question. Normalization is necessary to render the signal distributions of individual arrays comparable and there are several ways to do it (e.g. ranking procedures, quantile normalization, etc.). Here, we have used relative ranking, because it provides an intuitive measure of gene expression by referring to its magnitude in relation to all other signals on the array (e.g. with 0 and 100 corresponding the weakest and strongest signals, respectively). In the second step, the evaluation of probe signal will establish whether the effect of the experimental treatment(s) is statistically significant on the probe level. Naturally, the choice of the test depends on the experimental design and the research question. In this study, for example, we have used Wilcoxon–Mann–Whitney test to establish DE between two experimental conditions and Kendall’s tau statistic to evaluate the departure of temporal expression dynamics from monotonicity. The final step, estimation of DE on the target level, is based on the hypergeometric probability for the enrichment of differentially expressed probes among target-specific probes (referred to as on-target probes) relative to the complement (i.e. off-target probes). Fundamentally, instances of different target categories such as exons, transcripts, genes and genomic regions are represented by proper subsets of the probes included on the array. Consequently, testing for the enrichment of differentially expressed probes among on-target probes as opposed to the off-target probes will correspond to the degree of DE of the target in question.

As an example of how the framework can be applied to the study of differential gene expression we present a non-parametric workflow identifying differentially expressed targets between a test sample (TEST) and a reference sample (REFERENCE). Given a dataset of \( m \) TEST and \( n \) REFERENCE individuals, each represented by an array of \( q \) independent gene-expression measurements...
(m, n > 0; q ≫ 0; m, n, q ∈ N) an input matrix \( X = (x_{ij}) \) is constructed where \( i = 1 \ldots q \) and \( j = 1 \ldots m+n \). The rows of \( X \) correspond to independent measurements (equivalent to oligonucleotide probes on the array) and the columns correspond to individuals. In the first step, a normalizing transformation is applied column-wise to \( X \) whereby the signal distribution in each individual is normalized by converting the \( q \) signals into relative ranks

\[
X_{\text{norm}} = \frac{1}{q} \times (R_{si}||R_{s2}|| \ldots ||R_{sn+i}) \times 100
\]

where \( X_{\text{norm}} \) is the normalized input matrix, \( R_{si} \) is a vector of ranks corresponding to column \( i \) of the input matrix and \( || \) is the concatenation operator for column vectors.

Relative ranking was chosen as the preferred method over other popular normalizing transformations such as quantile normalization and absolute ranking, because we find relative ranks to be intuitively easier to interpret and, hence, more meaningful to the end-user. Unlike quantile-normalized signals, the median relative rank is independent of the median signal intensity (it is always located \( \sim 50 \)) and, unlike absolute ranks, relative ranks are independent of the number of probes \( q \) (the normalized signal is always located between 0 and 100). For example, a relative rank of 25 indicates an expression level coinciding with the first quartile of the observed intensities.

In the second step, a statistical test is applied row-wise to \( X_{\text{norm}} \) in order to classify probes as expressed higher or lower in TEST in relation to REFERENCE.
Wilcoxon–Mann–Whitney rank sum test was chosen as the method, because it makes fewer assumptions about the signal distribution than \( t \)-test and it is less sensitive to outliers. Given the set of probes \( Q = \{q_1, \ldots, q_n\} \), vectors of equivalent normalized measurements \( X_{\text{norm}}^i \) and the sets \( M = \{m_1, \ldots, m_m\} \), \( O = \{o_1, \ldots, o_n\} \) of column indices corresponding to \( \text{TEST} \) and \( \text{REFERENCE} \) individuals, respectively, we will define the set of up-regulated probes \( H \) and the set of down-regulated probes \( L \). For \( m, n > 3 \), the sets are defined as

\[
H = \{q_i : P_{\text{higher}}(r_i) < 0.05\} \tag{2}
\]

\[
L = \{q_i : P_{\text{lower}}(r_i) < 0.05\} \tag{3}
\]

where \( r_i \) is a vector of ranks corresponding to row \( i \) of the normalized input matrix and \( P_{\text{higher}} \) and \( P_{\text{lower}} \) correspond to the \( H \) probability of obtaining a sum of ranks equal to and higher or lower, respectively, than the observed rank sum of \( \text{TEST} \). In situations where \( m \leq 3 \) or \( n \leq 3 \), the following heuristic was used:

\[
H = \{q_i : r_j > r_k\} \tag{4}
\]

\[
L = \{q_i : r_j < r_k\} \tag{5}
\]

where \( r_k \) is a vector of ranks corresponding to row \( i \) of the normalized input matrix, \( j \in M \) and \( k \in O \). Accordingly, when one of the sample sizes was \( \leq 3 \), a probe was labeled as differentially expressed only if all \( \text{TEST} \) ranks were either lower or higher than \( \text{REFERENCE} \) ranks. The heuristic is useful in situations where a \( P \)-value below 0.05 is theoretically unobtainable (e.g. \( \frac{m+n}{m+n+1} > 0.05 \)) and a probe is to be classified as higher or lower in \( \text{TEST} \) if the sum of ranks in \( \text{TEST} \) individuals equals the maximum or the minimum, respectively.

Finally, in step 3, our aim is to identify the targets expressed higher or lower in \( \text{TEST} \) in relation to \( \text{REFERENCE} \). Here, the targets refer to genes, transcripts or genomic regions. Following the core principle of oligonucleotide microarray design, the \( t \) targets (\( 0 \ll t \ll q; \quad t \in \mathbb{N} \)) were related to the \( q \) independent expression measurements by a 100% identity between the nucleotide sequences of the probe and the target. Given a set of targets \( T = \{t_1, t_2, \ldots, t_m\} \) with target \( t_i \) relating to a predetermined subset of probes \( Q_i \in Q \) based on sequence identity and given sets of distinct probe expression profiles \( H_i, L_i \in Q \) two complementary DE estimates can be obtained for each target. Since the situation can be conceptualized as a sampling without replacement problem, the hypergeometric probability distribution was used to obtain estimates under the null hypothesis of making \( |Q_i| \) draws randomly:

\[
P_{\text{higher}}(t_i) = \sum_{k=|Q_i|}^{|Q|} P_{\text{hg}}(k_i | H_i, | Q \setminus H_i |, | Q_i |) \tag{6}
\]

\[
P_{\text{lower}}(t_i) = \sum_{k=|Q_i|}^{|Q|} P_{\text{hg}}(k_i | L_i, | Q \setminus L_i |, | Q_i |) \tag{7}
\]

where \( P_{\text{hg}} \) is the hypergeometric distribution function. When targets are exons in the context of a gene, the formulas above are modified to yield the following:

\[
P_{\text{higher}}(t_i) = \sum_{k=|Q_i|}^{|Q|} P_{\text{hg}}(k_i | G_{t_i} \cap H_i, | G_{t_i} \setminus H_i |, | Q_i |) \tag{8}
\]

\[
P_{\text{lower}}(t_i) = \sum_{k=|Q_i|}^{|Q|} P_{\text{hg}}(k_i | G_{t_i} \cap L_i, | G_{t_i} \setminus L_i |, | Q_i |) \tag{9}
\]

where \( G_{t_i} \) is the set of probes targeting the gene corresponding to target \( t_i \). Of note, there is no need to calculate \( P_{\text{higher}} \) for \( t_i \) if \( |Q_i \cap H| = 0 \) and the same applies for \( P_{\text{lower}} \) if \( |Q_i \cap L| = 0 \) as the result is by Definition (1). If \( Q \) is taken to represent the set of genes targeted by the array with \( H \) and \( L \) being the up- and down-regulated genes, respectively, and \( T \) is a collection of gene ontologies each represented by a gene set \( Q_i \) then Equations (6) and (7) yield gene ontology (GO)-level DE estimates. This methodology is well known and it belongs among the Class I gene-category tests defined in (11) which have been criticized for the increased incidence of Type I errors due to correlations between gene-expression profiles (12,13). However, this problem can be ameliorated by using a more stringent FDR procedure, which is the solution opted below. Furthermore, in the context of functional annotation analysis, Type II errors have much more serious consequences (e.g. failure to detect a differentially expressed pathway) than labeling a fraction of negatives as positives.

After adjusting the \( P \)-values for multiple hypotheses testing by the FDR procedure (14), the resulting estimates \( <0.05 \) were considered statistically significant. For target categories where a substantial overlap of targets in terms of on-target probes is anticipated (transcripts, genomic regions and functional categories) a modified version of the FDR procedure under dependency (15) is used to control Type I error rate.

**Microarray and Taqman® datasets**

Datasets based on MicroArray Quality Control (MAQC) project’s samples of Human Brain Reference RNA, HBR (Ambion) and Universal Human Reference RNA, UHR (Stratagene) were obtained for the following platforms: GeneChip® Human Genome U133 Plus 2.0 (Affymetrix), GeneChip® Human Gene 1.0 ST Array (Affymetrix), GeneChip® Human Exon 1.0 ST (Affymetrix), Taqman® (Applied Biosystems) (Table 1). Four technical replicates were used for the subsequent analysis in all platforms.

**Analysis of RNA-seq datasets**

Two different RNA-seq datasets (Table 2) based on HBR and UHR samples were obtained from the NCBI’s Gene Expression Omnibus database (GSE12946, GSE24283). The reads were mapped with TopHat (19) (version 1.3.3) that uses Bowtie (20) (version 0.12.7) to obtain the alignments. Annotation information and the indices were built on the data downloaded from the Ensembl database (build GRCh37.p12). The mapped reads were used to
DE estimates from Taqman® assays in MAQC data

Gene-expression data from Taqman® assays pertaining to Human Brain Reference RNA and Universal Human Reference RNA samples was retrieved from Gene Expression Omnibus (GEO:GSE5350). In the dataset, normalized gene expression levels were obtained by the MAQC consortium using the formula $2^{CT_{PRL2A}-CT}$, where $CT_i$ refers to the cycle threshold of the gene of interest and PRL2A gene is the reference. We estimated DE between the two RNA samples by comparing normalized expression values from replicate assays using Student’s $t$-test followed by Bonferroni correction using R software (www.r-project.org). Genes with adjusted $P$-value < 0.05 were labeled as differentially expressed. The list of differentially expressed genes based on Taqman assays was used as the reference during benchmarking.

Performance evaluation of DE estimation in MAQC data

DE estimates from microarray data were obtained by Limma (28), RankProd (29,30) and DEMI while the estimates from Taqman® assays were used as the reference when evaluating performance. The number of true positives (TP), false positives (FP), true negatives (TN) and false negatives (FN) were calculated on the intersection of gene identifiers in the prediction and reference datasets. A prediction was labeled as TP if the corresponding adjusted $P$-values were significant in both datasets and there was an agreement in the direction of DE (i.e. higher/lower expression in the Human Brain Reference RNA when compared to Universal Human Reference RNA in both datasets). A prediction was labeled as TN if the corresponding adjusted $P$-values were insignificant in both datasets. A prediction was labeled as FP if the corresponding adjusted $P$-value was significant in both datasets and there was no agreement in the direction of DE; this was considered an FDR. Finally, a prediction was labeled as FN if the corresponding adjusted $P$-value was insignificant in both datasets. A prediction was labeled as TP if the corresponding adjusted $P$-value was significant in both datasets.

Table 1. Microarray and Taqman® datasets representing MAQC reference samples in this article

<table>
<thead>
<tr>
<th>Platform</th>
<th>Accession</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Human Genome U133 Plus 2.0</td>
<td>GEO:GSE9819</td>
<td>(16)</td>
</tr>
<tr>
<td>Human Gene 1.0 ST</td>
<td>GEO:GSE9819</td>
<td>(16)</td>
</tr>
<tr>
<td>Human Exon 1.0 ST</td>
<td>GEO:GSE13069</td>
<td>(17)</td>
</tr>
<tr>
<td>Taqman®</td>
<td>GEO:GSE5350</td>
<td>(18)</td>
</tr>
</tbody>
</table>

Table 2. Number of spots per sample for RNA-seq datasets representing MAQC reference samples in this article

<table>
<thead>
<tr>
<th>Dataset</th>
<th>HBR</th>
<th>UHR</th>
</tr>
</thead>
<tbody>
<tr>
<td>GEO:GSE12946</td>
<td>17246957</td>
<td>8069964</td>
</tr>
<tr>
<td>GEO:GSE24283</td>
<td>53238798</td>
<td>59461348</td>
</tr>
</tbody>
</table>

Processing of microarray data

To compare DEMI with state-of-the-art workflows for DE analysis four different probe set summarization methods were used: RMA (25), FARMS (26), DFW (27) and PLIER (http://media.affymetrix.com/support/technical/technotes/plier_technote.pdf). RMA, FARMS and DFW were applied using the implementation provided in the xps package (http://www.bioconductor.org/pack ages/devel/bioc/html/xps.html) and PLIER was applied using Affymetrix Power Tools (http://www.affymetrix.com/estore/partners_programs/programs/developer/tools/power tools.affx). All methods were applied with default parameters. Probe sets were mapped to the corresponding Ensembl gene ID’s based on annotation data downloaded from Ensembl’s BioMart.

Sequence retrieval and annotation

Probe sequences of Affymetrix gene-expression arrays were downloaded from the company’s website (www. affymetrix.com). Genome and transcriptome sequences corresponding to release 73 of Ensembl were downloaded from Ensembl’s public FTP site (ftp.ensembl.org), annotation tables for matching identifiers were downloaded from Ensembl’s BioMart using biomaRt package (http://www. ensembl.org/info/data/api.html). Genomic karyotype information was obtained from Ensembl databases using bioperl-1.2.3 (http://www. bioperl.org) and Ensembl Perl API (http://www.ensembl. org/info/data/api.html).

Probes were aligned to the genome, transcriptome and exome using the Blat application (24). An ungapped alignment of at least 23 nucleotides was required to produce a hit. Probe annotations are summarized in Supplementary Table S1.

Analysis of array permutations

For comprehensive testing of performance on sample sizes $n \in \{3, 2\}$, all $m$ by $n$ permutations of the $m = 4$ original arrays were created. Each permutation of the test sample was compared against all permutations of the reference. For each comparison, the performance indicators were obtained by calculating the mean value across the selected FDR cutoffs. The performance indicator for each analysis workflow was obtained by averaging

estimated differential gene expression between HBR and UHR samples using three state-of-the-art methods: EdgeR (21) (R package, version 3.0.8), DESeq (22) (R package, version 1.10.1) and Cuffdiff2 (23) (stand-alone, version 2.0.2). EdgeR and DESeq estimates were based on gene-level read counts produced by HTSeq (http://www.huber.embl.de/users/anders/HTSeq/) version 0.5.3p9, using flags ‘–stranded=no –mode=union –type=exon’.

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across all comparisons. Significance analysis of MCC values obtained for various workflows under identical conditions was performed using paired t-test.

Retrieval of GO information

The child categories of all GO terms were retrieved using Ensembl Perl API. Ensembl gene identifiers corresponding to each GO category were downloaded using biomart package providing programmatic access to the Ensembl’s Biomart database. Gene list corresponding to a GO category was compiled from gene identifiers associated with the category and its children.

Analysis of long-range epigenetic silencing data

The dataset (GEO:GSE19726) contained two replicate gene-expression measurements by Human Gene 1.0 ST array (Affymetrix) of normal prostate epithelial cells (PrEC) and the prostate cancer cell line LNCaP. A list of putative candidate regions subject to long-range epigenetic silencing (LRES) in prostate cancer was obtained from Table 1 of the original study (31). DEMI was used to estimate DE in 0.5-Mbp genomic windows overlapping by 50%. The original comparison and the two null permutations of the arrays were analyzed. Due to overlap in the genomic windows, P-values were adjusted for multiple testing using the method by Benjamini and Yekutieli (15), a default setting in DEMI when genome is the target. Adjusted P-values < 0.05 were considered statistically significant. Minimally, a 0.25-Mbp overlap between a down-regulated genomic window and a candidate LRES locus was required to label the LRES locus as detected by DEMI.

Enrichment analysis of differential epigenetic modification

The ChIP-chip data from (31) (MAT scores from two arrays per cell line and histone modification type) representing H3K9 acetylation and H3K27 tri-methylation in LNCaP and PrEC cells were downloaded from Gene Expression Omnibus (accession no. GSE19726). Before statistical testing, the MAT scores were quantile normalized in R (package preprocessCore) to ensure comparable signal distributions between the arrays. Differential chromatin modification was estimated in the same genomic regions as analysed for DE by DEMI. All probes mapping to the genomic region of interest were included in the analysis. Differential chromatin modification of a genomic region was estimated using probe-wise paired t-test between LNCaP and PrEC arrays followed by Bonferroni correction. Enrichment of regions exhibiting differential chromatin modification was estimated among differentially expressed genomic regions using the hypergeometric probability distribution.

Primary cell culture model of hypoxia

Around 1 million primary mouse embryonic fibroblasts (Millipore) were seeded onto 100-mm culture dishes and were grown in DMEM (high glucose 4.5 g/l, supplemented with 10% FBS and L-glutamine, PAA) in normal conditions (atmospheric oxygen, 5% CO2 at 37°C) until 60–70% confluent. Hypoxia was initiated by lowering the oxygen concentration to 1% in a multi-gas incubator (Sanyo). The experiment was carried out in five biological replicates per experimental condition. After 24 h, RNA was extracted from the hypoxic and normoxic cells by Trizol® (Life) followed by large scale gene expression profiling with Mouse Exon 1.0 ST array (Affymetrix) according to manufacturer’s protocols. Briefly, 50 ng of total RNA from each sample was amplified using the Ovation Pico WTA system V2 (Nugen). Fragmentation and biotin labeling was done using the Encore-Ovation cDNA Biotin Module (Nugen). The labeled samples were hybridized to the Mouse Exon 1.0 ST array (Affymetrix). The arrays were washed and stained with phycoerytrin conjugated streptavidin (SAPE) using the Affymetrix Fluidics Station® 450, and the arrays were scanned in the Affymetrix GeneArray® 3000 scanner to generate fluorescent images, as described in the Affymetrix GeneChip® protocol. Cell-intensity (CEL) files were generated in the GeneChip® Command Console® Software (AGCC) (Affymetrix).

Primary cell-culture model of hypothermia

Around 1 million primary mouse embryonic fibroblasts (Millipore) were seeded onto 100-mm culture dishes and were grown in DMEM (high glucose 4.5 g/l, supplemented with 10% FBS and L-glutamine, PAA) in normal conditions (atmospheric oxygen, 5% CO2 at 37°C) until 60–70% confluent. Hypoxia was initiated by lowering the oxygen concentration to 1% in a multi-gas incubator (Sanyo). The experiment was carried out in five biological replicates per experimental condition. After 24 h, RNA was extracted from the hypoxic and normoxic cells by Trizol® (Life) followed by large scale gene expression profiling with Mouse Exon 1.0 ST array (Affymetrix) according to manufacturer’s protocols. Briefly, 50 ng of total RNA from each sample was amplified using the Ovation Pico WTA system V2 (Nugen). Fragmentation and biotin labeling was done using the Encore-Ovation cDNA Biotin Module (Nugen). The labeled samples were hybridized to the Mouse Exon 1.0 ST array (Affymetrix). The arrays were washed and stained with phycoerytrin conjugated streptavidin (SAPE) using the Affymetrix Fluidics Station® 450, and the arrays were scanned in the Affymetrix GeneArray® 3000 scanner to generate fluorescent images, as described in the Affymetrix GeneChip® protocol. Cell-intensity (CEL) files were generated in the GeneChip® Command Console® Software (AGCC) (Affymetrix).

Quantitative real-time PCR

Total RNA was extracted from cells using Trizol® Reagent (Invitrogen, USA) according to the manufacturer’s protocol. First-strand cDNA was synthesized with random hexamers (Invitrogen, USA) and SuperScript™ III Reverse Transcriptase (Invitrogen, USA). The following Taqman® (Applied Biosystems) assays with FAM-labeled probes were used in the study: Mm00483336_g1 (Cirbp), Mm01253561_m1 (Nqo1), Mm00515065_m1 (Gss), Mm00443675_m1 (TxnrD1),
Enrichment analysis of HIF-1- and HIF-2-binding sites in hypoxia-induced genes

Lists of high-stringency HIF-1- and HIF-2-binding sites were obtained from the Supplementary Material of Schödel et al. (32). Annotation table linking human gene identifiers (RefSeq) to corresponding mouse orthologs (Ensembl) was downloaded from Ensembl using R (package biomaRt). As some of the human gene identifiers did not map to a mouse orthologue we were able to identify 295 mouse orthologs of HIF-1 targets and 245 orthologs of HIF-2 targets. Enrichment of putative HIF-1 and HIF-2 target genes was estimated among significantly up-regulated genes using the hypergeometric probability distribution.

RESULTS

Computer simulations

To test the reasoning above, we performed 100 simulations of microarray experiments with two groups \( (N = 4) \) involving 45,000 genes and around 1.3 million probes. Up- and down-regulation of randomly picked 1000 genes was simulated by adding a fold-change of 2 or −2 to the log₂-transformed intensities of 80% of target-specific probes (i.e. \( r_i = 0.8 \)). Noise was added by applying the same fold-change to a randomly chosen 10% of the remaining probes (i.e. \( r_{\text{reference}} \approx 0.1 \)). False discovery rates and Matthews correlation coefficient (MCC) were studied under adjusting two limiting values, \( u \) (the maximum number of probes matching to a target) and \( t \) (the maximum number of distinct targets matching to a single probe). In the baseline setting, both \( u \) and \( t \) were not in effect. Setting \( t \) to 1 caused a considerable reduction in the number of false positives, which was expected as differentially expressed probes mapping to multiple targets affect multiple \( r_j - s \) (Figure 1C). Setting \( u \) to 30 had a less pronounced albeit still beneficial effect on the false positive rate (FPR). On average, only two false positives were found when both of the parameters were in effect. Taken together, the simulations suggest that on artificial data DEMI produces highly accurate results when \( t = 1 \) and \( u = 30 \).

MAQC data

To benchmark DEMI in relation to established methods of high-throughput gene-expression analysis, the most comprehensively characterized dataset, the MAQC reference samples (18), was studied. The dataset included three microarray platforms (Table 1) and high-throughput RNA-sequencing data (RNA-seq) from independent sources (Table 2). Microarray data was analyzed by DEMI and eight conventional DE analysis workflows. Performance was evaluated at different sample sizes \( (N = \{4 \ldots 2\}) \) using numerous well-established metrics including area under receiver-operator curve (AUC), MCC, true positive rate (TPR), FPR, true negative rate (TNR) and false negative rate (FNR). Cutoff-dependent metrics (MCC, TPR, FPR, TNR, FNR) were summarized as the average of two FDR cutoffs (0.05, 0.01). For comparison, two RNA-seq datasets representing the MAQC samples were analyzed by three state-of-the-art methods (Cuffdiff 2.0, DESeq, edgeR).

To offer a better overview of the benchmarking endpoints, appropriate performance indicators were juxtaposed on radial plots, which we refer to as ‘balanced performance plots’ (Figure 2). Perfect performance is represented on these plots by a colored plane occupying most of the upper semicircle while the lower semicircle remains blank. The benchmarking results are also available in numerical form (Supplementary Material, file 2). Overall, DEMI exhibited most stable performance across the tested microarrays and sample sizes (Figure 2A). RankProd appeared to lack power at the given FDR cutoffs as indicated by a relatively lower TPR, higher FNR and a larger difference between AUC and MCC. Limma was the most sensitive method at \( N = \{4, 3\} \) in terms of the TPR, but it exhibited a relatively higher FPR and, consequently, similar MCC to DEMI. Performance plots of PLIER appeared less consistent between the arrays than was the case for the other normalization methods. Significance analysis of MCC values obtained for various workflows indicated small, but mostly significant differences under otherwise identical conditions (Supplementary Material, file 3). We conclude that the performance of DEMI is comparable to the best-performing workflows, but it is more stable across arrays and sample sizes. Benchmarking of the RNA-seq data analysis pipelines revealed somewhat lower MCC in relation to the best-performing microarray analysis methods (Figure 2B). While DESeq and edgeR displayed higher TPR than array analysis methods, it came at the expense of a notably higher FPR resulting in MCC values ~0.3. Cuffdiff 2.0 was the most conservative of the three with substantially lower TPR, a very low FPR and an MCC slightly inferior to the other RNA-seq analysis methods.

Cell culture model of hypoxia

In order to benchmark DEMI in experimental settings, we sought to set up and validate a novel in vitro model of hypoxia using a primary cell culture of mouse embryonic fibroblasts. The fact that the transcriptional mechanisms of hypoxia response have been extensively studied enabled us to validate the cell model and the analysis methodologies in relation to established knowledge in the field (33,34). The cells were subjected either to 24 h of 1% O₂ or atmospheric oxygen followed by large-scale gene-expression profiling using the Mouse Exon 1.0 ST array (Affymetrix). Differential gene-expression estimates

Mm01609819_g1 (Rbm3), Mm00802655_m1 (Gclc), Mm00769566_m1 (Srxn1), Mm01281449_m1 (Vegfa). Assay Mm01158416_g1 (Ywhaz) with VIC-labeled probe was used as reference. qPCR reactions were run on the ABI PRISM 7900HT Fast Real-Time PCR System equipment (PE Applied Biosystems, USA) and quantified with the ABI PRISM 7900 SDS 2.2.2 software. For each assay, an average of four technical replicates was used as the endpoint.

Enrichment analysis of HIF-1- and HIF-2-binding sites in hypoxia-induced genes

Lists of high-stringency HIF-1- and HIF-2-binding sites were obtained from the Supplementary Material of Schödel et al. (32). Annotation table linking human gene identifiers (RefSeq) to corresponding mouse orthologs (Ensembl) was downloaded from Ensembl using R (package biomaRt). As some of the human gene identifiers did not map to a mouse orthologue we were able to identify 295 mouse orthologs of HIF-1 targets and 245 orthologs of HIF-2 targets. Enrichment of putative HIF-1 and HIF-2 target genes was estimated among significantly up-regulated genes using the hypergeometric probability distribution.
Figure 2. Performance analysis of DE analysis pipelines on the MAQC data. Performance of each pipeline is presented as a radial plot, which includes results from three microarrays (A) or two distinct RNA-seq datasets (B) based on six complementary performance indicators. Abbreviations: AUC, MCC, TPR, FPR, TNR and FNR.
from eight workflows were submitted to functional
category analysis in g:Profiler (35) while the built-in
analysis was used in DEMI (Supplementary Material,
files 4–5). We looked for the up-regulation of the GO
categories ‘cellular response to hypoxia’ (GO:0071456) and ‘glycolysis’ (GO:0006096) as indicators of the
hypoxia response (36). Nearly all workflows displayed
perfect pathway detection rate when $N \geq 3$ whereas only
DEMI had perfect detection rate at $N = 2$ indicating that
both pathways were detected as significantly upregulated
in all 2-element subsets of the original samples with $N = 4$
(Figure 3). To provide an additional measure of accuracy
the enrichment of mouse orthologs of HIF-1 targets
among hypoxia-induced genes was studied (Table 3).
Most methods produced a highly significant enrichment
of putative Hif-1 target genes among up-regulated genes
when $N \geq 3$. DEMI was least affected by the reduction in
sample size as indicated by a robust enrichment of
putative Hif1-target genes when $N = 2$. Essentially
similar results were obtained for putative Hif-2 targets
(Supplementary Table S2).

LRES
To demonstrate that DEMI can evaluate the expression of
unconventional target categories, such as genomic regions,
it was applied to gene-expression data related to LRES.
LRES refers to the suppression of gene expression from
large chromosomal regions and it might be related to
cancer progression (37). The original study used several
independent lines of evidence to identify putative
epigenetically silenced genomic regions in prostate
cancer (31). Here, we used DEMI to identify down-
regulated genomic regions in prostate cancer cell line
LNCaP in relation to normal prostate epithelial cells
from two replicate gene-expression array measurements
per cell line as provided by the original study. DEMI
identified 2242 of the 22 630 genomic regions (each
region spanning 0.5 Mbp) as down regulated
(Supplementary Material, file 6). In array permutations
corresponding to the null hypothesis the fraction was an
order of magnitude smaller (222 and 201). In total, 38 out
of the 47 putative LRES loci identified in the original
study were found to be significantly down-regulated
(81%). Furthermore, the enrichment of putative LRES
loci among down-regulated regions was highly significant
($p = 3.04e-13$, Fisher’s Exact Test). The enrichment was
not apparent in array permutations corresponding to the
null hypothesis ($p_{P1} = 0.961; p_{P2} = 1$, Fisher’s Exact Test).
To confirm that differentially expressed genomic regions
are associated with altered chromatin modification
between LNCaP and PrEC cells we compared the levels of
H3K27me3 and DE was found. Taken together, present
results indicate that DEMI accurately identifies genomic
regions that are candidates for long-range epigenetic
modification of gene expression.

Cell culture model of hypothermia
Finally, we devised a strategy to demonstrate that DEMI
can handle novel experimental designs unrelated to group-
wise comparisons. Therapeutic hypothermia is a clinically
effective treatment for various hypoxic and ischemic con-
ditions (38–40), but the associated molecular mechanisms
remain unclear. To gain insight into hypothermia-induced
transcriptional response, mouse embryonic fibroblasts
were exposed to mild hypothermia (32°C) or
normothermia (37°C) for increasing time periods. We
aimed to identify genes with temporally near-monotonic
response as the most obvious candidates for mediating the
therapeutic effects of hypothermia. Monotonicity is char-
acteristic of many physiological responses (including the
activation of transcription) as demonstrated by the wide
applicability of the Michaelis–Menten kinetics and the
Hill equation, which describe nonlinear and saturable
mechanisms (41). We reasoned that a near-monotonic
temporal relation between gene expression and hypother-
mia is a more selective indicator of a causal relation than
the comparison of treatment to control at any single point
in time. Importantly, the experimental design required
only 13 arrays to study hypothermic and normothermic
response at seven time points. The departure of probe-
level responses from monotonicity was evaluated using
Kendall’s tau statistic, a measure of rank correlation.

Figure 3. Performance analysis of DE-analysis pipelines on data from
mouse embryonic fibroblasts exposed to 1% $O_2$ for 24 h. The plot
depicts the combined detection rate of GO categories ‘cellular
response to hypoxia’ (GO:0071456) and ‘glycolysis’ (GO:0006096) as
indicators of hypoxia response. The data is plotted as mean ± standard
error of all possible comparisons between subsets of size $N$ of the
hypoxic and normoxic groups (original $N = 4$).
Differential gene expression was estimated by nine pipelines including various normalization and DE-analysis methods. The data is presented as mean and standard error of hypergeometric $P$-values from all possible comparisons between subsets of size $N$ of the hypoxic and normoxic groups (original $N = 4$). $N$, sample size; SEM, standard error of mean; NA, not available.

### Table 3. Enrichment of mouse orthologs of HIF-1 targets among significantly up-regulated genes in mouse embryonic fibroblasts exposed to 1% O$_2$ for 24 h

<table>
<thead>
<tr>
<th>Normalization</th>
<th>DE</th>
<th>$N = 4$</th>
<th></th>
<th>$N = 3$</th>
<th></th>
<th>$N = 2$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean</td>
<td>SEM</td>
<td>Mean</td>
<td>SEM</td>
<td>Mean</td>
<td>SEM</td>
</tr>
<tr>
<td>Relative ranking</td>
<td>DEMI</td>
<td>3.0E-25</td>
<td>NA</td>
<td>4.3E-22</td>
<td>2.4E-22</td>
<td>6.0E-19</td>
</tr>
<tr>
<td>DFW</td>
<td>Limma</td>
<td>1.4E-28</td>
<td>NA</td>
<td>2.5E-21</td>
<td>1.5E-21</td>
<td>2.4E-08</td>
</tr>
<tr>
<td>FARMS</td>
<td>Limma</td>
<td>9.5E-22</td>
<td>NA</td>
<td>3.1E-10</td>
<td>2.1E-10</td>
<td>0.457</td>
</tr>
<tr>
<td>PLIER</td>
<td>Limma</td>
<td>9.4E-10</td>
<td>NA</td>
<td>0.9</td>
<td>0.1</td>
<td>0.037</td>
</tr>
<tr>
<td>RMA</td>
<td>Limma</td>
<td>6.0E-19</td>
<td>NA</td>
<td>1.7E-14</td>
<td>1.5E-14</td>
<td>0.481</td>
</tr>
<tr>
<td>RMA</td>
<td>RankProd</td>
<td>1.4E-18</td>
<td>NA</td>
<td>4.3E-13</td>
<td>2.1E-13</td>
<td>0.001</td>
</tr>
</tbody>
</table>

### Table 4. Enrichment of regions exhibiting differential epigenetic modification among differentially expressed genomic regions between LNCaP and PrEC cell lines

<table>
<thead>
<tr>
<th>Modification</th>
<th>Higher modification level in LNCaP</th>
<th>Lower modification level in LNCaP</th>
<th>H3K27me3/3.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Higher</td>
<td>0.998</td>
<td>0.266</td>
<td>H3K27me3</td>
</tr>
<tr>
<td>expression</td>
<td>7.99E-05</td>
<td>7.99E-05</td>
<td>H3K9ac</td>
</tr>
<tr>
<td>level in LNCaP</td>
<td>0.102</td>
<td>5.400E-22</td>
<td>H3K9ac</td>
</tr>
</tbody>
</table>

Significant $P$-values (hypergeometric probability distribution) indicate that down-regulation of H3K9ac is associated with silenced genomic regions while up-regulation of H3K9ac is prevalent among up-regulated regions in LNCaP cells when compared to PrEC. No significant association was found between DE and H3K27me3.

We identified 1750 and 274 genes with significantly monotonic-like temporal response to hypothermia and normothermia, respectively (Supplementary Material, files 7 and 8). The previously established hypothermia-responsive gene Cold inducible RNA-binding protein, Cirbp (42,43) was found among the top-five of up-regulated genes with 24 probes out of 25 exhibiting a statistically significant monotonic-like response (Figure 4A). In contrast, none of the Cirbp-specific probes displayed a significant response when incubated at 37°C (Figure 4B) validating both the experimental design and our analysis strategy. As a novel insight, we identified time-dependent increase in the expression of multiple genes related to the two major antioxidant pathways, the glutathione and thioredoxin systems (Table 5). Results from the microarray study were confirmed by qPCR (Figure 5). To our knowledge, this is the first study to report coordinated up-regulation of antioxidant gene expression by hypothermia.

## DISCUSSION

DEMI makes a notable departure from the conventional methods of DE analysis (5,6,44) in a couple of respects. First, a variety of statistical tests can be used to evaluate DE on probe level. Such flexibility can be used to adapt the method to a variety of experimental designs. Here we have demonstrated the use of Wilcoxon–Mann–Whitney test and Kendall’s tau to calculate probe-level statistics for two-group comparisons and time-series, respectively. Similarly, it should be possible to adapt DEMI to factorial designs (using probe-level ANOVA) and to identifying relationships between covariates (ANCOVA), for example. Second, DEMI summarizes probe-level responses after testing for DE, whereas conventionally, probe signals are summarized before testing. Our results suggest that having more data points at disposal enables more robust evaluation of DE by compensating for the loss of statistical power when $N$ is very small. Finally, it seems likely that DEMI can be adapted to the analysis of RNA sequencing and proteomic data as well. Fundamentally, both RNA-seq and proteomic analysis of tryptic peptides estimate the abundance of the target by concurrent quantification of its numerous fragments. As there are a number of practical issues, which need to be addressed, a thorough discussion is currently out of scope.

In the present article, several unrelated datasets were used to evaluate the performance of DEMI. The datasets were chosen carefully to include different application domains (e.g. gene versus genomic region-expression analysis), experimental designs (comparison of two groups versus time-series experiment), and to enable comprehensive benchmarking (MAQC data, evaluation of hypoxia response). First, twelve DE estimation workflows were benchmarked on the MAQC reference samples including data from three microarray platforms and two RNAseq studies. While it can be argued that the average gene expression study might not be faithfully represented by the MAQC reference samples (differences between the Human Brain RNA and Universal Human RNA samples appear to be uncommonly large and there is a lack of biological variation between replicates) the fact that the samples have been thoroughly characterized by various gene-expression assays makes it an attractive dataset for benchmarking. In the present article, an indicator of major differences between the MAQC reference samples
was the considerably higher rate of differentially expressed probes in the MAQC data when compared to the tissue culture model of hypoxia (38% in MAQC samples versus 11% in hypoxia). Our argument is substantiated by the consensus that hypoxia exerts wide-spread effects on gene expression (36,45).

In order to evaluate DE workflows in a more natural context, we devised and conducted an experiment comparing the transcriptomes of hypoxic and normoxic mouse embryonic fibroblasts. Our choice was motivated by the facts that the molecular mechanisms of hypoxia response have been extensively characterized and relevant pathways are included in the GO database. Accordingly, we were able to evaluate the accuracy of pathway-level DE predictions based on the detection rate of pathways linked to the experimental response by definition. We believe that this approach has high validity and it should be preferred over

Table 5. Genes responding to increasing durations of hypothermia with significantly monotonic increase in expression and relating to the antioxidant system

<table>
<thead>
<tr>
<th>Gene ID</th>
<th>Symbol</th>
<th>P-value</th>
<th>FDR</th>
<th>System</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENSMUSG00000003849</td>
<td>Nqo1</td>
<td>9.04E-35</td>
<td>4.72E-30</td>
<td>Quinone detoxification</td>
</tr>
<tr>
<td>ENSMUSG00000032802</td>
<td>Srxn1</td>
<td>1.23E-19</td>
<td>2.14E-16</td>
<td>Glutathione</td>
</tr>
<tr>
<td>ENSMUSG00000027610</td>
<td>Gss</td>
<td>1.08E-13</td>
<td>4.74E-11</td>
<td>Glutathione</td>
</tr>
<tr>
<td>ENSMUSG00000020250</td>
<td>Txnrd1</td>
<td>4.29E-11</td>
<td>9.83E-09</td>
<td>Thioredoxin</td>
</tr>
<tr>
<td>ENSMUSG00000032350</td>
<td>Gclc</td>
<td>4.29E-11</td>
<td>9.83E-09</td>
<td>Glutathione</td>
</tr>
<tr>
<td>ENSMUSG00000000811</td>
<td>Txnrd3</td>
<td>9.85E-09</td>
<td>1.19E-06</td>
<td>Thioredoxin</td>
</tr>
</tbody>
</table>

**Figure 4.** Large-scale analysis of temporal dynamics of transcription in mouse embryonic fibroblasts exposed to mild hypothermia. (A and B) Temporal profiles of probe expression levels of selected genes during mild hypothermia (A) and normothermia (B). The solid blue line indicates a linear fit to the data points and the gray shadowing represents standard error of the fit.
computer simulations, which are unlikely to capture the probe- and target-level correlations arising from biological and technical causes in natural datasets (12,46,47).

Next, the dataset of Coolen et al. (31) was used to demonstrate the efficacy of DEMI in detecting DE on the genomic level, a level of analysis rarely approached by traditional DE workflows. As epigenetic modification of chromatin can have widespread effects on DNA expression, we expect this type of analysis to be of great relevance. Finally, we devised and validated a novel method for detecting temporally near-monotonic expression patterns to demonstrate that DEMI is extendable beyond two-group comparisons. In consequence, we identified hypothermia-dependent up-regulation of genes encoding for major constituents of the antioxidant response as a possibly novel route for the therapeutic effects of hypothermia.

As endorsed by the MAQC consortium (48), we used MCC (49) as the indicator for benchmarking performance on the MAQC reference samples, because it is informative when the distribution of the two classes in a dataset is skewed. Based on the Taqman® assays, the numbers of positive and negative findings was 569 and 298, respectively, substantiating the choice of MCC as a primary performance indicator. For an even more comprehensive view, a number of related performance indicators, such as AUC, TPR, FPR, TNR and FNR, were included in a single radial plot we termed as a balanced performance plot. Although related, MCC and AUC represent different approaches to performance as the former is cutoff-dependent while the latter is not. As statistical reasoning is usually based on a predetermined significance level (e.g. $P < 0.05$), there are potentially many cases where AUC might not yield meaningful results. For example, given vector $p_i (i = 1 \ldots n)$ of $n$ $P$-values the AUC is calculated by integrating the ROC curve over the range of $p_i$ whereas in the context of statistical testing cutoff $i$ is used for rejecting the null hypothesis. As AUC is cutoff-independent,

![Temporal expression profiles](image-url)

**Figure 5.** Temporal expression profiles of selected genes during mild hypothermia (32°C) and normothermia (37°C) as reported by quantitative real-time PCR. Expression level of Ywhaz was used as reference. The mean of three replicates and standard error has been plotted.
an estimator with $p_i > t$ can still yield excellent AUC values even though TPR and FPR at $t$ are 0 in which case MCC is 0. Using MCC and AUC simultaneously has the benefit of identifying cases where the predictions are accurate (based on AUC), but the method lacks statistical power at the given cutoff (indicated by MCC) as was the case with RankProd in the current study.

In parallel with the increasing popularity of high-throughput sequencing platforms, there have been numerous claims that studying gene expression by RNA-seq technology is superior to microarray analysis (23,50–53). Of the aforementioned publications, two studies (23,50) compared the performance of RNA-seq and microarrays in terms of DE-detection accuracy. For a number of reasons, the studies do not provide substantial evidence for the increased accuracy of RNA-seq-based estimates. For example, the dataset used by Marioni et al. (50) lacked extensive quantitative PCR (qPCR) data (expression levels of only 11 genes were available) making it clearly inferior to the MAQC dataset used here. Second, an outdated array platform (HG-U133 Plus 2.0, Affymetrix) was used with approximately five-times lower coverage of targets in terms of total probe hits than the Human Exon 1.0 ST array. Most importantly, neither AUC nor MCC was used as a performance indicator in the study. The more recent study by Trapnell et al. (23) used the MAQC data, but the performance of RNA-seq based estimates was not evaluated in relation to the available microarray data. In addition, the performance was evaluated against fold-change estimates from the qPCR whereby genes with a log2-fold change of $>2.0$ were declared DE. Such practice has been deemed unsatisfactory by the microarray community due to fold-change not being an inferential statistic as it does not produce known and controllable long-range error rates (44).

On the other hand, we are aware of at least two studies suggesting that high-sequencing depth is critical for differential analysis of transcripts present at low abundance (2,23). Accordingly, a comparison of RNA-seq with a high-density microarray platform indicated higher sensitivity of the latter in detecting DE for low abundance genes (2). Similarly, several studies have reported a high variation (i.e. unreliable detection) in the expression level of targets with low read counts (1,50,54). Furthermore, DE-detection sensitivity is lower for shorter exons when compared to the microarray (55). These biases are consistent with a uniform sampling hypothesis whereby less abundant and shorter nucleic acid molecules yield fewer fragments and, consequently, less reads to base the estimates on. To illustrate, Labaj et al. (54) have estimated that 75% of the RNA-seq’s measurement power is spent on only 7% of the known transcriptome. In addition, it was estimated that $\sim$30% of the transcriptome might exhibit read counts too low for accurate prediction of DE. Our extensive analysis including three microarray platforms, >10 analysis pipelines and various sample sizes indicate that the accuracy of DE estimates obtained from the RNA-seq data available on the MAQC reference samples is slightly lower than for the tested microarray platforms.

In conclusion, we have presented a statistical framework and implementing software for DE analysis of microarray data suggesting that it surpasses conventional workflows in terms of robustness and application range. In addition, many studies are expected to benefit from the cost-saving measure of accurate DE analysis from a small number of replicates (e.g. pilot studies), especially if the pooling of samples is feasible. The accompanying software, available at http://biit.cs.ut.ee/demi/, contains largely automated workflows that will facilitate the analysis of large-scale gene-expression data.

**ACCESSION NUMBERS**

Microarray gene expression data generated in this study is available from Gene Expression Omnibus under accession numbers GSE54228 and GSE54229.

**SUPPLEMENTARY DATA**

Supplementary Data are available at NAR Online.

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