A Mathematical Model of Corneal Metabolism in the Presence of an Iris-Fixated Phakic Intraocular Lens

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In recent years, phakic iris-fixated intraocular lenses (PIOLs) have attracted widespread acceptance for refractive error correction and, in particular, for treating myopia. PIOLs are surgically implanted in the anterior chamber of the eye and fixated to the iris by haptics. Recent developments in lens manufacturing technologies, design, and surgical procedures have significantly decreased the risk of complications associated with PIOL implantation, and PIOLs are generally considered very safe. In some cases, a decrease in corneal endothelial cell density has been observed after PIOL implantation,1,2 although this finding is still under debate and some authors have not observed evidence of it.3

Various mechanisms have been proposed and investigated to explain the possible occurrence of corneal endothelium cell loss in the presence of PIOLs. The surgical procedure itself can cause a decrease in endothelial cell density. Mechanical friction between the endothelium and the PIOL has also been postulated to possibly cause cell detachment in patients with the habit of rubbing their eyes or sleeping face down. Various authors1–6 have investigated through mathematical models the possible role of changes in the wall shear stress on the cornea due to aqueous humor motion on endothelial cell detachment. The authors have found that implantation of a PIOL does not induce a significant increase of the stress on the cornea and thus this is unlikely to cause cell loss.

Repetto et al.4 and Davvalo Khongar et al.7 have postulated that cell loss could be associated with a decrease in nutrient availability at the corneal endothelium in the presence of a PIOL. Since the cornea is an avascular tissue it relies on oxygen and nutrient supply from the surrounding tissues or from the external environment. In the healthy cornea, oxygen is primarily supplied by the surrounding air when the eyelids are open and from blood circulation in the palpebral conjunctiva when the eyelids are closed.8 On the other hand, glucose primarily diffuses into the cornea from the aqueous humor.9 The hypothesis put forward in the studies by Repetto et al.4 and Davvalo Khongar et al.7 is that the presence of a PIOL may interfere with the delivery of nutrients to the cornea. In particular, when the eyelids are open, owing to the existence of a temperature gradient across the anterior chamber, a buoyancy-driven aqueous flow is generated that quite efficiently allows mixing of the aqueous in the anterior chamber.10 This flow also exists with a similar intensity in the presence of a PIOL.4,11 Moreover, daytime eye rotations also generate significant velocities and mixing in the aqueous.11,12 Thus, in this case the presence of the PIOL is not likely to interfere much with nutrient transport to the cornea. On the other hand, during sleep the eyelids are closed and, when rapid eye movements (REMs) do not occur, the eye globe is approximately fixed. In this case both of the above flows are suppressed and the only mechanism generating fluid flow in the anterior chamber is aqueous production at the ciliary processes. The presence of a PIOL diverts the flow passing through the pupil toward the periphery of the anterior chamber and effectively shields the central cornea. In fact, the flow anterior to the PIOL is very slow in this case1 and nutrients have to rely mostly on molecular diffusion to reach the central region of the corneal epithelium, which is a very inefficient transport mechanism, on the spatial scale of millimeters. Thus during eyelid closure the cornea might experience nutrient depletion in the presence of a PIOL.
The aim of the present work was to explore this hypothesis. To this end we developed a mathematical model that accounts for aqueous flow in the anterior chamber and reaction-diffusion metabolic processes in the cornea.

Several mathematical models and experiments have been proposed, aimed at describing corneal metabolism. Taking advantage of the fact that the thickness of the cornea is much smaller than its lateral dimension, in most cases one-dimensional models have been adopted in which the transport of all species across the cornea is assumed to be much larger than in the other directions. Chhabra et al. have proposed a coupled reaction-diffusion model for nutrient and oxygen delivery to the cornea, which together with the model proposed by Pinsky, is the basis of the model used in this work. None of the above works have considered the direct effect of aqueous flow in delivering nutrients to the cornea.

**Materials and Methods**

**Corneal Metabolism Model**

Glucose consumption from corneal cells occurs through two main pathways: aerobic (or tricarboxylic acid or Krebs cycle) and anaerobic (Embden-Meyerhof) glycolysis. For the normal rabbit cornea, ≈15% of glucose breakdown is through aerobic glycolysis. Moreover, only ≈10% of corneal glucose is supplied from glycogen and endogenous glucose. The latter contribution was neglected in this work.

In glycolysis, one mole of 6-carbon glucose is first converted into 3-carbon pyruvate. Then, in the presence of oxygen, pyruvate is converted to acetyl-CoA and enters the Krebs cycle, resulting in the formation of carbon dioxide and, through oxidative phosphorylation, water. This pathway is simplified as follows:

\[
C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O + \text{energy}. \quad (1)
\]

In aerobic respiration, 6 moles of water and 6 moles of carbon dioxide are produced by the consumption of 1 mole of glucose with 6 moles of oxygen and the reaction produces 36 net moles of adenosine triphosphate (ATP). In the absence of oxygen, the pyruvate produced by glycolysis is converted to lactate and hydrogen ions. This pathway is called Embden-Meyerhof and is simplified as follows:

\[
C_6H_{12}O_6 \rightarrow 2C_3H_4O_5^- + 2H^+ + \text{energy}. \quad (2)
\]

In this path, for each mole of consumed glucose, 2 moles of ATP are produced. Acidification of the cornea due to this reaction is buffered by bicarbonate ion to produce dissolved carbon dioxide.

**Transport Equations**

As described in the previous section, corneal metabolism relies on the availability of oxygen and nutrients. Proper functioning of the metabolic processes described above is essential for corneal health. For example, accumulation of lactate ions due to lack of oxygen tension leads to edema. In this article, following Pinsky, we only considered the following three metabolic species: oxygen, glucose, and lactate.

As discussed in the introduction, when the eyelids are open the thermally driven buoyancy flow and eye rotations quite effectively mix the aqueous in the anterior chamber, smoothing out concentration gradients. This allowed us to avoid solving the problem of aqueous motion and transport in the anterior chamber. Rather, we assumed that concentration of all species is uniformly distributed in the anterior chamber and just imposed the corresponding concentration values as boundary conditions on the endothelium when solving the problem in the cornea.

On the contrary, when the eyelids are closed, aqueous velocities are much smaller and concentration gradients can develop in the anterior chamber. This implies that in order to study metabolic species transport to the cornea in this case, it is necessary to account for aqueous motion in the anterior chamber. This ingredient is essential for understanding the possible role of the presence of a PIOL.

We modeled the aqueous humor as an incompressible, Newtonian fluid. Fluid motion is governed by the Navier-Stokes and continuity equations that read as follows:

\[
\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} + \frac{1}{\rho} \nabla p - \nabla^2 \mathbf{u} = \mathbf{0}, \quad (3a)
\]

\[
\nabla \cdot \mathbf{u} = 0, \quad (3b)
\]

where \( t \) is time, \( \mathbf{u} \) denotes the velocity vector, \( \rho \) is the departure of the pressure from the hydrostatic profile (thus we omit the gravitational acceleration), \( \rho \) is the density, and \( v \) is the kinematic viscosity. The values of the density and viscosity adopted in the simulations are reported below.

Transport of metabolic species in the anterior chamber is governed by the advection/diffusion equation

\[
\frac{\partial c_i}{\partial t} + (\mathbf{u} \cdot \nabla) c_i - D_{i}^{a} \nabla^2 c_i + m Q_{j}^{i} = 0 \quad (i = O, G, L). \quad (4)
\]

In the above equation subscripts \( i = O, G, L \) refer to oxygen, glucose, and lactate ion, respectively. \( c_i \) and \( D_i^{a} \) are the concentration and diffusion coefficients of the corresponding metabolic species in aqueous, respectively. In our model the oxygen concentration \( c_O \) will be represented as \( k_{O} p_{O} \) where \( k_{O} \) is Henry’s constant for oxygen (\( k_{O} = 1.283 \times 10^{-5} \text{mM/Pa} \)) and \( p_{O} \) is the oxygen tension.

Chhabra et al. have proposed a one-dimensional metabolic model for the corneal layers, which is generalized to three dimensions by Pinsky. Transport of oxygen, glucose, and lactate ion in the corneal layers is governed by the following diffusion/reaction equations:

\[
\frac{\partial c_{i}^{L}}{\partial t} - D_{i}^{L} \nabla^2 c_{i}^{L} + m Q_{j}^{L} = 0 \quad (i = O, G, L). \quad (5)
\]

In the above equations, the index \( j \) refers to the three corneal layers of endothelium, stroma, and epithelium. \( Q_{i}^{L} (i = O, G, L) \) refers to oxygen, glucose consumption, and lactate production rate in each corneal layer \( j \), respectively. Moreover, \( m \) is 1 for oxygen and glucose (consumption) and −1 for lactate ion (production). \( D_{i}^{L} \) refers to the diffusion coefficients of metabolic species \( i \), for each corneal layer, see Table 1.

**Reaction Models**

In Chhabra et al. and Pinsky, for each layer of the cornea the dependency of \( Q_{i}^{L} \) on both \( p_{O} \) and \( c_{i} \) is modeled by using an enzymatic Monod kinetics model. We modified the authors’ approach and used a sigmoidal function to model the dependency of \( Q_{i}^{L} \) on \( p_{O} \), as proposed by Alvord et al. The reason for this choice is that a sigmoidal function better fits the in vivo experimental data of Bonanno et al. This results in the use of the following expression for the oxygen consumption rate:

\[
Q_{O}^{L} = \frac{Q_{O}^{L \max}}{1 + e^{-\frac{p_{O} - p_{O}^{o}}{p_{O}^{h} - p_{O}^{i}}}} \left[ c_{G} + K_{G}^{O} \left( 1 + 0.8 \frac{7.6 - pH}{K_{P} + 7.6 - pH} \right) \right] \quad (6)
\]

The parameters appearing in the sigmoidal function are based on the experimental data of Bonanno et al. and...
reported in Table 2. The glucose Monod dissociation equilibrium is considered equal to 0.4 mm Hg, corresponding to an oxygen consumption rate of 93.75% of the saturation value at a glucose concentration of 6 mM. The third term inside the brackets of Equation (6) refers to the reduction of \( \text{pH} \) from the normal value of 7.6 due to acidosis, which is described in Chhabra et al. In the case of open eyelids, corneal pH is approximately 7.6, while when the eyelids are closed, it decreases to approximately 7.39. Glucose consumption and lactate ion production have the same expressions as proposed by Chhabra et al.

**Geometry**

Figure 1 represents the idealized axisymmetric shape of the anterior chamber and the cornea. Following Repetto et al., we neglected the flow in the posterior chamber. Thus the iris-lens channel represents the inlet section of the production/drainage flow used in the simulations related to closed eyelids. The cornea consists of three layers, namely, endothelium, stroma, and epithelium, moving inside out (Fig. 1, inset). The Descemet’s and Bowman’s membranes are considered part of the stroma, since they have similar transport properties. Geometric characteristics of the cornea are given in Table 3.

We performed simulations, with and without a PIOL. For the PIOL we considered the Artiflex lens, whose geometry was provided by the manufacturer (Ophtec BV, Groningen, The Netherlands). In all simulations we neglected the presence of the PIOL haptics, which were shown in Repetto et al. to have a negligible influence on aqueous flow. We also studied the effect of a perforation with a diameter of 0.36 mm in the center of the body of the PIOL.

Since both the geometry of the anterior chamber and that of the Artiflex (without haptics) are axisymmetric, the resulting geometry is also axisymmetric, which allowed us to solve an axisymmetric problem on a plane.

We note that in the present work we neglected the presence of an iridotomy, that is, a perforation in the iris, which is typically performed when irisi-fixed lenses are implanted and whose role on the fluid dynamics in the anterior chamber in the presence of a PIOL has been investigated by Fernández-Vigo et al.

**Open Eyelids**

At the interfaces between each corneal layer, the three metabolic species should satisfy continuity of concentrations. Moreover, conservation of mass requires continuity of normal fluxes. Oxygen tension, glucose concentration, and lactate ion concentration at the anterior chamber–endothelium interface are set at 24 mm Hg, 6.9 mM, and 7.7 mM, respectively. At the epithelium–tear film interface, the oxygen tension is set at 155 mm Hg, which corresponds to the atmospheric oxygen tension. Glucose and lactate fluxes at the interface between the tear film and the anterior chamber is set to zero. At the corneal limbus, we consider a zero flux boundary condition for all metabolic species.

**Closed Eyelids**

The measurement of oxygen tension in the anterior chamber is crucial when specifying the boundary conditions for the validation of our models. We mainly focused our attention on the article by McLaren et al. in which the authors use a scanning ocular fluorometer and measure the oxygen tension through the depth of the anterior chamber. This experiment was repeated for different cases and we focused our attention on the measurement of oxygen tension obtained on the cornea in the case with a PMMA contact lens and when eyelids are closed. Most of the oxygen is provided to the cornea from the air, with open lids, and from the palpebral conjunctiva, with closed lids. Since the oxygen permeability of a PMMA contact lens is low, a very small amount of oxygen can pass through it and thus the cornea is deprived of these oxygen sources. In this case, we speculate that oxygen is mostly provided by the aqueous humor. Under these conditions, McLaren et al. have found that the oxygen tension close to the crystalline lens is approximately equal to 6 mm Hg and it decreases to 3 mm Hg in the central region of the anterior chamber. Following these observations, we set the oxygen tension on the crystalline lens and the inlet channel to 6 mm Hg. At these surfaces, we imposed a lactate ion concentration equal to 9 mM. Concerning glucose concentration, the choice is not obvious. In the open eyelids case, assuming that concentration gradients in the anterior chamber are smoothed out by aqueous motion, we assumed a value of 6.9 mM directly at the corneal endothelium. In the case of closed eyelids we need glucose...
concentration in the aqueous at the iris-lens channel, which is the inlet of the domain. The value of 6.9 mM can be seen as a lower limit value: any values smaller than this would necessarily produce a smaller value at the corneal endothelium, which would be inconsistent with the condition used for the open eyelids case. On the other hand an upper limit for glucose concentration in the aqueous humor is the glucose concentration in blood at the ciliary processes (8.3 mM), where the aqueous is secreted. Following the above reasoning, we tried different values in the range 6.9 mM to 8.3 mM. The actual value adopted is relevant if one wishes to compare the open and closed eyelid cases. However, we note that it is less crucial when comparing the cases with and without the PIOL, which is the main focus of the present work. This is because for the latter comparison all simulations will be run for the closed eyelids case. As baseline in the following, we used the value of 7.5 mM for glucose concentration at the crystalline lens and the iris-lens channel.

For the iris and corneal limbus, we imposed zero flux for all metabolic species. At the epithelium–tear film interface, since information regarding fluxes are absent in the literature, the oxygen tension was set to 61.5 mm Hg, which is the oxygen tension in the palpebral conjunctiva. In analogy with the open eyelids case, glucose and lactate fluxes were set to zero at the epithelium–tear film interface. At the trabecular meshwork, an outflow boundary condition (zero diffusive flux) for all of the metabolic species was imposed.

For aqueous flow, at the iris-lens channel we imposed a parabolic velocity profile, which corresponds to a volumetric flux \( Q \) across the patch equal to \( 2.5 \times 10^{-11} \) m\(^3\)/s (Table 4). Aqueous production is known to vary from diurnal to nocturnal conditions; the value we assumed is close to what Nau et al. have found for the latter case (\( \approx 2.2 \times 10^{-11} \) m\(^3\)/s). At the trabecular meshwork zero pressure is imposed, thus the pressure has to be interpreted as the departure from the value at the trabecular meshwork. We assumed that all other surfaces are solid walls and imposed a so-called no-slip boundary condition.

We solved the governing equations with the associated boundary conditions, using Comsol Multiphysics version 4.3a (Stockholm, Sweden).

### RESULTS

We first studied the steady state solution of the problem described in the previous section and we then investigated the time required for this steady solution to be reached, starting from a given initial condition. For all cases, we ran a simulation both with and without the PIOL. We also investigated the effect of a perforation in the PIOL on the transport of metabolic species in the anterior chamber and cornea. The first REM phase occurs approximately 90 minutes after falling asleep, but this was not explicitly modeled here. However, our unsteady simulations reproduced the evolution of glucose and lactate concentrations and oxygen tension, before the first REM phase starts. Further, the steady solutions provided the aforementioned values in the limit of long sleep phases without REM.

### Steady Simulations

**Solution in the Absence of PIOL.** Figure 2 shows the steady state profiles of oxygen tension (Fig. 2a) and of lactate (Fig. 2b) and glucose (Fig. 2c) concentration across the thickness of the axis of symmetry of the cornea. In the plots the x-axis represents a coordinate in the direction toward the anterior pole, with the origin at the interface between the corneal layers and the implant. We solved the governing equations with the associated boundary conditions, using Comsol Multiphysics version 4.3a (Stockholm, Sweden).

<table>
<thead>
<tr>
<th>Table 4. Aqueous Humor Parameters Used in Equations 3a and 4</th>
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<tr>
<td><strong>Aqueous Humor Properties</strong></td>
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<tr>
<td>Density ( \rho )</td>
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<tr>
<td>Aqueous inlet flux ( Q )</td>
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<tr>
<td>Kinematic viscosity ( \nu )</td>
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<tr>
<td>Oxygen diffusion coefficient ( D_{O2} )</td>
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<tr>
<td>Glucose diffusion coefficient ( D_{G} )</td>
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<tr>
<td>Lactate diffusion coefficient ( D_{L} )</td>
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**Figure 1.** Cross-section of the idealized anterior chamber with corneal layers and implanted PIOL. Left: PIOL with a central perforation. Right: PIOL without perforation.
aqueous humor and the corneal endothelium. The vertical lines mark the boundaries between the three corneal layers. Let us consider first the case in which no PIOL is present in the anterior chamber (black and red curves in the figure). Both in the case of open and closed eyelids, moving from epithelium toward the anterior chamber (negative $x$ direction), owing to oxygen consumption by corneal layers, there is a decline in the oxygen tension. Moreover, since the glucose in our model is solely provided by the aqueous humor and is consumed by the corneal layers, there is a decrease of glucose concentration toward the epithelium. As a consequence of glycolysis, lactate concentration increases toward the epithelium. The results relative to the open eyelids case (black curve) are very similar to what has been predicted by Pinsky\textsuperscript{15} (reported with purple dots in Fig. 2).

As discussed above, direct comparison between the two cases has to be considered with care. The reason is that we did not solve for aqueous motion in the case of open eyelids, assuming that the aqueous is well mixed, but we did so in the case of closed eyes (flow streamlines are shown in Fig. 3, right). However, the two cases are likely to be quite different since, in the case of closed eyes, a significant gradient of concentration for all species develops in the anterior chamber, as shown in Figure 4 (right side of each panel). In particular, glucose concentration within the anterior chamber decreases toward the cornea, whereas oxygen and lactate behave oppositely. With our choice for the boundary conditions, oxygen levels in the cornea are significantly lower than when the eyes are closed and the minimum value, which occurs at the endothelium, drops from 24 to $\approx 13$ mm Hg, which is consistent with the experiments of McLaren et al.\textsuperscript{21} Glucose concentration at the corneal endothelium is also significantly lower in the case of closed eyelids. We note, not shown here, that this is true even if we impose for glucose concentration at the inlet of the domain the value of 8.3 mM (glucose concentration in blood), which we regard as an upper limit value.

Comparison of the Cases With and Without a PIOL. To better understand the effect of a PIOL in the anterior chamber it is useful to first consider the changes in aqueous flow that are generated by presence of the PIOL. In Figure 3 we present a color map of the velocity magnitude together with streamlines of the flow in the anterior chamber with and without the presence of PIOL. It appears that the PIOL forces fluid toward the periphery of the anterior chamber, and a region of very slow motion forms anteriorly to the PIOL. In this region the flow is characterized by two extremely slow circulations with opposite signs. Since the flow anterior to the lens is slow, glucose in the aqueous has to rely primarily on molecular diffusion in order to reach the central region of the cornea. Since diffusion is a very slow transport mechanism, in this case we expect to find lower levels of glucose along the endothelium. This is confirmed by our results, as shown in Figure 2c (green curve). Indeed, in this case the glucose concentration drops to very low values throughout the thickness of the central cornea. At the posterior apex the glucose concentration drops from 3.5 to 0.5 mM, while at the anterior apex the concentration drops from 1.7 to 0.06 mM. As a consequence of glucose drop, oxygen partial tension in the cornea is higher when the PIOL is present than in the reference case, as shown in Figure 2a.

Figure 4a shows color maps of the steady state glucose concentration in the anterior chamber and cornea, with and without the PIOL. The figure shows that glucose distribution in the two cases is very different. This is essentially due to the advective transport induced by the aqueous motion seen in Figure 3. In the case of an implanted PIOL, fluid is forced toward the periphery of the anterior chamber, and a region of very slow motion forms anteriorly to the PIOL. In this region the flow is characterized by two extremely slow circulations with opposite signs. Since the flow anterior to the lens is slow, glucose in the aqueous has to rely primarily on molecular diffusion in order to reach the central region of the cornea. Since diffusion is a very slow transport mechanism, in this case we expect to find lower levels of glucose along the endothelium. This is confirmed by our results, as shown in Figure 2c (green curve). Indeed, in this case the glucose concentration drops to very low values throughout the thickness of the central cornea. At the posterior apex the glucose concentration drops from 3.5 to 0.5 mM, while at the anterior apex the concentration drops from 1.7 to 0.06 mM. As a consequence of glucose drop, oxygen partial tension in the cornea is higher when the PIOL is present than in the reference case, as shown in Figure 2a.
PIOL, the center of the cornea has a lower glucose concentration and a lower consumption of oxygen, leading to an increased oxygen level. Moreover, owing to the lack of glucose (and in spite of the small increase of oxygen tension in the cornea), the production rate of lactate increases in the case of an implanted PIOL, which in turn increases lactate concentration.

**Comparison of the Cases With and Without a Hole in the PIOL.** When a perforation is present in the center of the PIOL, part of the aqueous flow enters the anterior chamber through the iris-lens channel and flows directly toward the cornea (see Fig. 5). Figure 6a shows color maps of steady state glucose concentration in the anterior chamber and the cornea.

**Figure 3.** Velocity magnitude and flow streamlines in the anterior chamber with (left) and without (right) PIOL.

**Figure 4.** Glucose concentration (a), oxygen tension (b), and lactate concentration (c) in the anterior chamber and cornea with (left) and without (right) PIOL.
As can be seen, considering the advective transport of aqueous flow toward the hole, the availability of glucose at the endothelium is higher than without the perforation. Furthermore, as shown in Figure 2c (blue curve), throughout the corneal layers, the glucose concentration in the presence of the PIOL with a central hole is higher than with the PIOL without any modification, although still much lower than in the case without the PIOL.

Finally, Figures 6b and 6c show color maps of oxygen tension and lactate concentration, respectively. Since oxygen is...
mainly provided from the epithelium side, the central hole in
the lens body has a negligible effect in comparison to the case
where the PIOL is without a hole. On the other hand, owing to
the increase in glucose concentration, anterior to the
perforated lens, lactate concentration in this region decreases,
which also decreases the risk of corneal acidification.

Unsteady Simulations

In the previous section we discussed the steady state results of
our model. Obviously, for steady state concentrations to be
reached a certain time is required, and it is of interest to
estimate it. This allows us to verify whether the solutions
described in the previous section can be reached in reality. We
recall that when eyelids are open it is assumed that the
aqueous humor is efficiently mixed by eye rotations and
thermal flow. During sleep, these sources of fluid motion are
suppressed and fluid motion is generated mainly by produc-
drainage flow. However, we know that at relatively regular
intervals, REMs occur during sleep, which will induce fluid
mixing. On average, the first REM phase occurs approximately
90 minutes after falling asleep, during the first sleep cycle. The
following REM phases, which are increasingly longer, occur
within each sleep cycle, which lasts approximately 1½ hours.
Changes of posture during sleep also produce rotations of the
eye bulb, which are, however, characterized by low angular
velocities and short duration. Thus, they are unlikely to
contribute much to fluid mixing.

We assumed that a fully developed production/drainage
flow exists in the anterior chamber and we computed the
temporal evolution of species’ concentrations, imposing values
at an initial time corresponding to the open eyelids case.
Moreover, we assumed that at the initial time the concentra-
tions of all species in the anterior chamber are uniformly
distributed. With these initial conditions we ran unsteady
simulations, using the same boundary conditions adopted in
the previous section for the case of closed eyelids.

Figure 7 shows the time evolution of the concentration of
all species at the anterior chamber–endothelium interface, on
the axis of symmetry of the cornea. The red curve corresponds
to the case without the PIOL; the green curve, the case in
which a PIOL is present; and the blue curve, the case in which
the PIOL has a central hole. In this figure we also marked with
a vertical dashed black line the time at which the first REM
phase is expected to occur. The figure shows that the time scale
of evolution is of the order of some hours: the final steady state
is reached in approximately 4 hours. Since the first REM occurs
after approximately 90 minutes and successive REMs occur
within each sleep cycle, this final steady state is unlikely to be
reached in normal conditions.

However, we found that when the first REM phase occurs,
the glucose concentration is reduced from 6.9 mM to 4.1 mM
(without PIOL), to 2.5 mM (PIOL with hole), and to 1.8 mM
(with PIOL).

Discussion and Conclusions

We proposed a mathematical model of transport of metabolic
species to the cornea, considering the role of aqueous flow in
the anterior chamber, which has been neglected in previous
works. We considered both the case of open eyelids, when
aqueous motion is enhanced by eye rotations and the onset of a
thermally induced flow, and closed eyelids, in which case
aqueous flow is much less intense. We considered both the
physiological case and the case in which a PIOL is implanted in
the eye, with the aim of understanding if and to what extent
the PIOL affects corneal metabolism.

We accounted for the presence of three species (oxygen,
glucose, and lactate) and modeled corneal metabolism,
adopting the model proposed by Chhabra et al.,14 Pinsky,15
and Alvord et al.,13 which we suitably modified to better
reproduce available experimental data. In particular, we
focused on glucose availability at the cornea. This is because
oxygen is mostly delivered to the cornea from outside of the

Figure 7. Time evolution of metabolic species’ concentration: oxygen
(a), lactate (b), glucose (c), at the center of cornea with and without
the PIOL. The vertical dashed lines mark the time at which, typically,
the first REM occurs. The three curves correspond to the physiological
case (red), the case of an implanted PIOL (green), and the case on an
implanted perforated PIOL (blue).
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eye, from the air in the open eyelids condition and from the palpebral circulation in the closed eyelids case. On the other hand, glucose is transported to the cornea by the aqueous humor and its availability at the corneal endothelium is likely to be affected by the presence of an intraocular lens.

Steady state simulations show that the presence of a PIOL has a significant influence on glucose availability on the cornea, in sleep conditions. When a PIOL is implanted, aqueous flow is diverted toward the periphery of the anterior chamber and glucose concentration decreases in the region anterior to the PIOL. However, we showed that several hours are needed for this steady solution to be reached. Since during sleep REMs are expected to occur within every sleep cycle, which occurs every 90 minutes, the steady state solution predicted by our model is unlikely to ever be reached. Rather, the system is constantly in an unsteady state. Glucose concentration anterior to the PIOL progressively decreases until REMs occur; then eye rotations cause mixing of the aqueous humor, and the glucose concentration in front of the PIOL increases again. We found that the minimum value of glucose that is expected to be reached in the presence of a PIOL is approximately half of that corresponding to the nonsurgically altered case, which might be relevant for cell damage (4.1 mM without PIOL and 1.8 mM with PIOL). In the case of a perforated PIOL, glucose and oxygen availability on the cornea increases, compared to the case of a PIOL without a hole, and the lactate concentration correspondingly decreases. It is useful to keep in mind that the duration of the REM depends on age and sleep patterns and may therefore have an influence on glucose availability at the cornea after PIOL implantation. On this basis one could speculate that some people may be at higher risk of corneal endothelial cell damage than others.

Some possible relevant effects were neglected in the present work, which are worth mentioning. Firstly, we neglected the possible presence of an iridotomy, which is often created when a PIOL is implanted. Iridotomy creates an additional passage from the posterior to the anterior chamber, thus modifying fluid flow characteristics in the anterior chamber. We note, however, that iridotomies are typically produced in the periphery of the iris. Thus, the jet of aqueous through the iridotomy enters the anterior chamber close to the trabecular meshwork, where it drains, and is unlikely to significantly contribute to advective transport of nutrients to the central cornea. For this reason we do not think that our conclusions would be qualitatively different, even if the presence of an iridotomy was considered.

We also did not consider the effect of endogenous glycogen in our model. Thus, variations of glucose concentration in the cornea in vivo may not be as strong as predicted by our model.

In summary, we studied the effect of aqueous motion on nutrient transport to the cornea. We compared the physiological case to the case in which an iris-fixated PIOL is implanted in the anterior chamber. Our model suggests that implantation of a PIOL may produce a decrease in nutrient availability in the central region of the cornea during sleep that might be related to the possible loss of endothelial cells. We are unaware of data regarding the physiological threshold of glucose concentration for cell damage, and it must be verified whether our theoretical predictions have clinical relevance.

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References


