Detection of the irradiated donor in the LMXBs 4U 1636-536 (=V801 Ara) and 4U 1735-444 (=V926 Sco)

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ABSTRACT

Phase-resolved VLT spectroscopy of the bursting low-mass X-ray binaries 4U 1636-536/V801 Ara and 4U 1735-444/V926 Sco is presented. Doppler images of the N III λ4640 Bowen transition reveal compact spots which we attribute to fluorescent emission from the donor star and enable us to define a new set of spectroscopic ephemerides. We measure K_{em} = 277 ± 22 and 226 ± 22 km s^{-1} from the N III spots in V801 Ara and V926 Sco, respectively, which represent strict lower limits to the radial velocity semi-amplitude of the donor stars. Our new ephemerides provide confirmation that light-curve maxima in V801 Ara and likely V926 Sco occur at superior conjunction of the donor star and hence photometric modulation is caused by the visibility of the X-ray heated donor. The velocities of He II λ4686 and the broad Bowen blend are strongly modulated with the orbital period, with phasing suggesting emission dominated by the disc bulge. In addition, a reanalysis of burst oscillations in V801 Ara, using our spectroscopic T_{0}, leads to K_1 = 90–113 km s^{-1}. We also estimate the K-corrections for all possible disc flaring angles and present the first dynamical constraints on the masses of these X-ray bursters. These are K_2 = 360 ± 74 km s^{-1}, f(M) = 0.76 ± 0.47 M_{\odot} and q = 0.21–0.34 for V801 Ara and K_2 = 298 ± 83 km s^{-1}, f(M) = 0.53 ± 0.44 M_{\odot} and q = 0.05–0.41 for V926 Sco. Disc flaring angles α ≫ 12° and q ≲ 0.26–0.34 are favoured for V801 Ara whereas the lack of K_1 constraint for V926 Sco prevents tight constraints on this system. Although both binaries seem to have intermediate inclinations, the larger equivalent width of the narrow N III line in V801 Ara at phase 0.5 relative to phase 0 suggests that it has the higher inclination of the two.

Key words: accretion, accretion discs – binaries: close – stars: individual: V801 Ara – stars: individual: V926 Sco – X-rays: binaries.

1 INTRODUCTION

Low-mass X-ray binaries (LMXBs) are interacting binaries where a low-mass donor transfers matter on to a neutron star or black hole. 4U 1636-536 (=V801 Ara) and 4U 1735-444 (=V926 Sco) are among the optically brighter members in the class of persistent LMXBs, characterized by L_\lambda \sim 10^{37–38} erg s^{-1} and blue spectra with weak high-excitation emission lines (mainly He II λ4686 and the C II/NI/NI Bowen blend at λ4640). They also share similar properties: they are both atoll sources (as based on the pattern traced in X-ray colour–colour diagrams, see e.g. Hasinger & van der Klis 1989) with frequent burst activity and short orbital periods (3.80 and 4.65 h, respectively) revealed through optical photometry (Pedersen, van Paradijs & Lewin 1981; Corbet et al. 1986). Their light curves display shallow sinusoidal modulations which have been interpreted as due to the geometrically varying visibility of the irradiated donor star (e.g. van Paradijs, van der Klis & Pedersen 1988). Therefore, the photometric maxima supposedly define orbital phase 0.5 i.e. inferior conjunction of the compact object. Note, however, that this...
assumption requires confirmation because photometric maxima can sometimes be associated with asymmetries in the disc structure such as the visibility of the irradiated inner disc bulge at phase ~0.3 (e.g. 4U 1822-371 Hellier & Mason 1989) or superhump activity (see Haswell et al. 2001).

Only a few spectroscopic studies have been presented on these two binaries up to now. For example, Smale & Corbet (1991) report Hz spectroscopy of V926 Sco showing that the line core is dominated by emission from the disc bulge or splash region where the gas stream interacts with the outer disc rim. On the other hand, Augusteijn et al. (1998) (A98 hereafter) presented radial velocity curves of He II λ4686 and the Bowen blend at λ4640 for both V926 Sco and V801 Ara. They concluded that these high-excitation lines are also tracing the motion of the disc bulge.

V801 Ara is particularly remarkable since it is one of only 14 bursters where ‘burst oscillations’ (i.e. nearly coherent high-frequency pulsations) have been detected during several thermonuclear X-ray bursts (Giles et al. 2002, G02 hereafter). Furthermore, a train of burst oscillations was also discovered in a 13 min interval during a ‘superburst’, showing a frequency drift which has been interpreted as the orbital motion of the neutron star (Strohmayer & Markwardt 2002, SM02 hereafter). By fitting the frequency evolution with a circular orbit SM02 constrained the radial velocity amplitude of the neutron star to the range 90 < K1 < 175 km s⁻¹. These constraints on K1 will be readdressed and improved in this paper. Further constraints on the system parameters and the component masses, however, require dynamical information on the donor star which, unfortunately, is normally overwhelmed by the optical emission from the X-ray irradiated disc.

A new indirect method to extract dynamical information from donor stars in persistent LMXBs was proposed by Steeghs & Casares (2002) (SC02 hereafter). They detected narrow high-excitation emission lines from the irradiated surface of the donor star in Sco X-1 which led to the first determination of its radial velocity curve and mass function. These lines are strongest in the Bowen blend, a combination of C iii and N iii lines which are powered by photoionization and fluorescence (respectively) due to UV photons arising from the hot inner disc (McCintock, Canizares & Tarter 1975). This technique has been amply confirmed by subsequent studies of the eclipsing accretion disc corona (ADC) and X-ray pulsar 4U 1822-371 (Casares et al. 2003), the black hole soft X-ray transient GX 339-4 during its 2002 outburst (Hynes et al. 2003) and Aql X-1 during its 2004 outburst (Cornelisse et al. 2006).

In this paper, we apply this method to the X-ray bursters 4U 1636-536 (=V801 Ara) and 4U 1735-444 (=V926 Sco) and present the first detection of the donor stars in these two LMXBs. This paper is organized as follows. Section 2 summarizes the observation details and data reduction. The average spectra and main emission-line parameters are presented in Section 3, with multi-Gaussian deconvolution of the Bowen blend. In Section 4, we analyse the radial velocities and orbital variability of the strong Bowen blend and He π λ4686 emission lines. Estimates of the systemic velocities are obtained through the double-Gaussian technique applied to the wings of the He π line. Using these systemic velocities, we compute Doppler tomograms of He π λ4686 and the Bowen fluorescence N iii λ4640 which are presented in Section 5. The N iii maps display evidence of irradiated emission from the donor star, which is used to refine the absolute phasing and systemic velocities. Finally, in Section 6 we provide an improved determination of K1 for V801 Ara and present our constraints on the masses in the two binaries.

2 OBSERVATIONS AND DATA REDUCTION

V801 Ara and V926 Sco were observed on the nights of 2003 June 23 and 25 using the FORS2 Spectrograph attached to the 8.2-m Yepun Telescope (UT4) at the Observatorio Monte Paranal (ESO). A total of 42 spectra of 603s of V801 Ara and 102 exposures of 200s of V926 Sco were obtained with the R1400V holographic grating, covering a complete orbital cycle per night for each target. We used a 0.7-arcsec slit width which rendered a wavelength coverage of λλ4514-5815 at 70 km s⁻¹ [full width at half-maximum (FWHM)] resolution, as measured from Gaussian fits to the arc lines. The seeing was variable between 0.6 and 1.2 arcsec during our run. The flux standard Feige 110 was also observed with the same instrumental configuration to correct for the instrumental response of the detector.

The images were de-biased and flat-fielded, and the spectra subsequently extracted using conventional optimal extraction techniques in order to optimize the signal-to-noise ratio of the output spectra (Horne 1986). A He–Ne–Hg–Cd comparison lamp image was obtained in daytime to provide the wavelength calibration scale. This was obtained by a fourth-order polynomial fit to 19 lines, resulting in a dispersion of 0.64 Å pix⁻¹ and rms scatter <0.05 Å. Instrumental flexure was monitored through cross-correlation between the sky spectra and was found to be very small, always within 14 km s⁻¹ (0.4 pix.) on each night. These velocity shifts were removed from each individual spectrum, and the zero-point of the final wavelength scale was established from the position of the strong OI λ5577.338 skyline. All the spectra were calibrated in flux using observations of the flux standard Feige 110. However, due to light loss caused by our narrow slit and variable seeing conditions, our flux calibration is only accurate to ~50 per cent.

3 AVERAGE SPECTRA AND EMISSION-LINE PARAMETERS

Fig. 1 presents the average spectra of V801 Ara and V926 Sco in fν flux units. They show a blue continuum with broad high-excitation emission lines of He π λ4686, λ5411, the Bowen blend at λλ4630-50 and Hβ, which are typical of X-ray active LMXBs. Possible HeI lines at λ4922 and λ5015 are also identified but these are significantly weaker. Table 1 summarizes the FWHM, EW and centroid λc of the main emission lines obtained through simple Gaussian fits. We note that the average spectra (including the line strengths) look very similar to those presented by A98, which seems to imply that there has been no large, long-term variations between the two

![Figure 1. Summed spectra of V801 Ara and V926 Sco with the principal emission lines indicated.](https://academic.oup.com/mnras/article-abstract/373/3/1235/1063835)
Irradiated donor in V801 Ara and V926 Sco

Table 1. Emission-line parameters.

<table>
<thead>
<tr>
<th>Line</th>
<th>FWHM (km s(^{-1}))</th>
<th>EW (Å)</th>
<th>Centroid (Å)</th>
<th>(\Delta V) (km s(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>V801 Ara</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bowen</td>
<td>1848 ± 65</td>
<td>4.25 ± 0.03</td>
<td>4643.2 ± 0.4</td>
<td>–</td>
</tr>
<tr>
<td>He(\text{II}) λ4686</td>
<td>1216 ± 45</td>
<td>3.31 ± 0.03</td>
<td>4685.6 ± 0.3</td>
<td>– 9 ± 11</td>
</tr>
<tr>
<td>H(\beta)</td>
<td>963 ± 56</td>
<td>1.67 ± 0.02</td>
<td>4860.9 ± 0.3</td>
<td>– 25 ± 21</td>
</tr>
<tr>
<td>V926 Sco</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Bowen</td>
<td>1662 ± 65</td>
<td>3.99 ± 0.02</td>
<td>4641.5 ± 0.4</td>
<td>–</td>
</tr>
<tr>
<td>He(\text{II}) λ4686</td>
<td>657 ± 26</td>
<td>2.18 ± 0.02</td>
<td>4683.9 ± 0.2</td>
<td>–118 ± 12</td>
</tr>
<tr>
<td>H(\beta)</td>
<td>507 ± 39</td>
<td>0.43 ± 0.02</td>
<td>4859.2 ± 0.4</td>
<td>–134 ± 25</td>
</tr>
</tbody>
</table>

Our best fit yields N\(\text{III}\) ratio \(I(\lambda 4634)/I(\lambda 4641-2) = 0.31 ± 0.10\) and 0.59 ± 0.02 for V801 Ara and V926 Sco, respectively. This is a factor of \(\leq 2\) lower than the theoretical N\(\text{III}\) ratio of 0.71, computed by Nussbaumer (1971) for Bowen fluorescence, but consistent with the results of Schachter et al. (1989) for Sco X-1. Similarly, Hynes (private communication) finds a N\(\text{III}\) ratio in the range 0.36–0.56 (depending on time) for GX 339-4 during its 2002 outburst. We can also calculate the C\(\text{III}/\text{N}\(\text{III}\) ratio \((I(\lambda 4647-52))/(I(\lambda 4634 + \lambda 4641-2))\) and find 0.38 ± 0.06 and 0.35 ± 0.01 for V801 Ara and V926 Sco, respectively. For comparison, we have performed the same analysis on average spectra of Sco X-1 and 4U 1822-371, using data presented in SC02 and Casares et al. (2003), and find 0.44 ± 0.03 and 0.49 ± 0.01, respectively. The lower C\(\text{III}/\text{N}\(\text{III}\) ratio in V801 Ara and V926 Sco may indicate possible evidence of CNO processed material but we have to be cautious here because of the oversimplification in our fitting model. In particular, we cannot rule out other possible transitions (most likely O\(\text{II}\) lines at λ4641.8 and λ4649.1; see McClintock et al. 1975) contributing to our components at ~4641 and ~4651 Å, which so far we have assumed to be dominated by N\(\text{III}\) and C\(\text{III}\) transitions. Furthermore, since the C\(\text{III}\) and O\(\text{II}\) lines are not powered by Bowen fluorescence but photoionization, different line ratios may stem from differences in efficiency of these two excitation mechanisms rather than true CNO abundance variations.

4 RADIAL VELOCITY STUDY AND ORBITAL VARIABILITY

Fig. 3 displays the radial velocities of the Bowen blend and He\(\text{II}\) λ4686 line for V801 Ara and V926 Sco, obtained by cross-correlating the individual spectra with Gaussians of fixed FWHM as given in Table 1. We have assumed \(\lambda_c = 4643.0\) Å for the central wavelength of the Bowen blend. The velocities are folded in orbital phase, using the ephemerides of G02 and A98 for V801 Ara and V926 Sco but shifted in phase by +0.5 to make phase zero coincide with the inferior conjunction of the donor star. These will be called the photometric ephemerides and will be used throughout this section. The accumulated phase uncertainty at the time of our observations is ±0.06 for both systems. Note that this phase convention assumes that light-curve maxima are driven by the visibility of the irradiated donor star.

The radial velocity curves for V801 Ara show maxima at phase ~1. This phasing suggests that the velocity variations contain a significant component arising in the disc bulge (which has its maximum visibility at phase ~0.75), caused by the interaction of the gas stream with the outer edge of the disc, as is typically seen in persistent LMXBs (e.g. 4U 1822-371; Cowley, Crampton & Hutchings 1982). On the other hand, the radial velocity curves for V926 Sco show maxima at phase ~0.7. By comparing the He\(\text{II}\) curves in the two binaries we clearly see evidence for a large systemic velocity of ~150 km s\(^{-1}\) in V926 Sco, in good agreement with Smale & Corbet (1991). We also note that the C\(\text{III}/\text{N}\(\text{III}\) blend in V801 Ara is modulated with a much larger amplitude than in V926 Sco i.e. 280 km s\(^{-1}\) versus 70 km s\(^{-1}\), respectively.

Fig. 4 presents the trailed spectra of the Bowen blend and He\(\text{II}\) λ4686 for V801 Ara and V926 Sco, after co-adding our individual spectra in 15 phase bins to improve statistics. The cores of the emission lines in V801 Ara show clear S-wave components. The S-wave in the Bowen blend is quite narrow and it may arise from the heated face of the donor star, as observed in Sco X-1 (SC02). The S-wave in He\(\text{II}\) is rather extended and is likely produced in a region with a large velocity dispersion such as the disc bulge. On the
other hand, the Bowen blend in V926 Sco is rather noisy and does not exhibit any clear components that are visible by eye. The He II trailed spectra do show a clear orbital modulation with complex structure.

Following our work on Sco X-1 (SC02) and 4U 1822-371 (Casares et al. 2003), we have applied the double-Gaussian technique (Schneider & Young 1980) to the wings of the He II λ4686 line in an attempt to estimate the radial velocity curve of the compact object. The trailed spectra presented in Fig. 4 demonstrate that the line cores are dominated by high-amplitude ($K$ ~ 200 km s$^{-1}$) S-waves which fade as we move to the line wings, where lower $K$-amplitudes of a few tens of km s$^{-1}$ are found. On the other hand, the $\gamma$ velocities are very steady throughout the profiles, with average values of $\sim$30 (V801 Ara) and $\sim$130 km s$^{-1}$ (V926 Sco). The blue-to-red crossing phase for V926 Sco displays a smooth decreasing trend from the line core to the wings, whereas it is rather constant for V801 Ara, with an average value of $\phi_0 \sim 0.7$. We estimate that the velocity points start to be corrupted by continuum noise for Gaussian separations larger than $a \sim 1000$ as indicated by the diagnostic parameter $\sigma(K)/K$ (see Shafter, Szkody & Thorstensen 1986). Therefore, we decided to adopt the average values for the parameters obtained from the last two separations before $\sigma(K)/K$ starts to rise i.e. $a = 900$–1000 km s$^{-1}$ for V801 Ara and 1000–1100 km s$^{-1}$ for V926 Sco. This yields $K_1 = 93 \pm 25$ km s$^{-1}$, $\gamma = -42 \pm 4$ km s$^{-1}$, $\phi_0 = 0.68 \pm 0.03$ for V801 Ara and $K_1 = 96 \pm 9$ km s$^{-1}$, $\gamma = -121 \pm 7$ km s$^{-1}$ and $\phi_0 = 0.20 \pm 0.01$ for V926 Sco. The error bars have been adjusted to incorporate the scatter between different values within our preferred range. Note that $\phi_0$ of V801 Ara is delayed by $\sim 0.18$ with respect to the inferior conjunction of the compact object (dotted line in Fig. 5), as predicted by the photometric ephemerides. This is classically observed in interacting binaries and interpreted as contamination of the line wings by residual emission from the disc bulge/hotspot (Marsh 1998). On the other hand, $\phi_0$ of V926 Sco
leads the inferior conjunction of the compact star by \( \sim 0.30 \), according to the photometric ephemerides. Such a large shift is unexpected and a full discussion is diverted to Section 6. Furthermore, we also note the very asymmetric distributions obtained in the He II Doppler maps (see next section) which may invalidate the double-Gaussian technique. Therefore, the constraints on zero-phase, \( \gamma \)-velocity and \( K_1 \) (for V801 Ara) will be superseeded in the following sections.

5 BOWEN FLUORESCENCE FROM THE IRRADIATED COMPANION

Doppler tomography enables us to map the brightness distribution of a binary system in velocity space through combining orbital phase spectra (see details in Marsh 2001). This is particularly effective when dealing with weak emission features which are barely detected or embedded by noise in individual spectra, such as our narrow Bowen emission lines. In order to compute Doppler images of the N III \( \lambda 4640 \) fluorescence line in V801 Ara and V926 Sco we have rectified the individual spectra by subtracting a low-order spline fit to the continuum regions and rebinned them into a uniform velocity scale of 37 km s\(^{-1}\) per pixel. Doppler images were subsequently computed using the photometric ephemerides and \( \gamma = -42 \) and \( -121 \) km s\(^{-1}\) for V801 Ara and V926 Sco, respectively. The maps show compact spots shifted in phase by \( +0.03 \) and \( -0.18 \) with respect to the expected location of the donor star in the velocity maps (i.e. along the vertical \( V_y \) axis).\(^1\) Assuming that these spots are produced on the irradiated hemisphere of the donor star, as has been shown to be the case in Sco X-1 (SC02) and 4U 1822-371 (Casares et al. 2003), we correct the previous photometric ephemerides and derive the following spectroscopic ephemerides, which will be used in the remainder of this paper:

\[
T_0(\text{HJD}) = 2452813.531(2) + 0.15804693(16)E
\]

and

\[
T_0(\text{HJD}) = 2452813.495(3) + 0.19383351(32)E,
\]

where the zero-phase error comes from the uncertainty in the centroid position of the spots. Equation (1) corresponds to the ephemerides of V801 Ara and equation (2) to V926 Sco. With these ephemerides, the He II \( \lambda 4686 \) maps of the two binaries show a crescent shape brightness distribution pointing towards emission from an extended disc bulge.

Following SC02, we have used the He II Doppler maps to refine the systemic velocities derived in the previous section. The \( \chi^2 \) value of the map was calculated for a range of values of \( \gamma \), and the best fit in terms of minimal \( \chi^2 \) was achieved for \( \gamma \sim -39 \) km s\(^{-1}\) (V801 Ara) and \( \gamma \sim -132 \) km s\(^{-1}\) (V926 Sco). The use of an incorrect systemic velocity has the effect of blurring bright spots into, as opposed to V801 Ara, elongated ‘defocused’ features in Doppler images. Therefore, as a further test, we have also computed N III \( \lambda 4640 \) maps for a set of \( \gamma \)-velocities in the range \(-200 \) to \(+200 \) km s\(^{-1}\) and we looked for the best focused N III spots by computing the skewness using box sizes of 5, 10 and 20 pixels.

We find that the most symmetric and compact spots are found for \( \gamma \) values in the range \(-29 \) to \(-39 \) km s\(^{-1}\) (V801 Ara) and \( 137 \)–\( 143 \) km s\(^{-1}\) (V926 Sco). Therefore, we decided to adopt \( \gamma = -34 \pm 5 \) km s\(^{-1}\) (V801Ara) and \( \gamma = -140 \pm 3 \) km s\(^{-1}\) (V926 Sco) and these are the values that we have used in the final Doppler maps, which are presented in Fig. 6. The N III maps reveal compact bright spots which we interpret as irradiated emission from the inner hemisphere of the donor star. These spots are obviously located along the vertical axis because of our ephemerides definition. We have calculated the position of these spots by computing their centroids using the centring algorithm CENTROID in IRAF\(^2\) and find \( K_m \) = \( 277 \pm 22 \) km s\(^{-1}\) (V801 Ara) and \( 226 \pm 22 \) km s\(^{-1}\) (V926 Sco). We note that \( K_m \) is very weakly dependent on \( \gamma \), with only a 10 km s\(^{-1}\) drift when \( \gamma \) varies by \( \pm 20 \) km s\(^{-1}\) around our central value. Therefore, our \( K_m \) determinations seem very robust and they represent strict lower limits to the true radial velocity semi-amplitude \( K_2 \) of the donor stars because they must arise from the irradiated hemisphere facing the neutron star. Further confirmation of our system parameters is provided by the appearance of the sharp C III/N III transitions after co-adding all the spectra in the rest frame of the N III \( \lambda 4640 \) emission-line region (see Fig. 7). Note that we have not attempted to compute Doppler images of the He II lines because these are contaminated by phase-variable absorption components, as was also the case in 4U 1822-371 (e.g. Casares et al. 2003). Absorption violates the principles of Doppler tomography and makes it very difficult to interpret the corresponding Doppler images.

6 DISCUSSION

The detection of N III \( \lambda 4640 \) fluorescence emission from the irradiated donor in V801 Ara and V926 Sco provides new absolute

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\(^1\) Note that the grey-scale in the N III maps have been set to enhance the contrast of the sharp components. This is the reason why these maps do not show any trace of emission from the underlying broad component.

\(^2\) IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities of Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.
the other hand, light-curve maxima in V926 Sco are located at orbital phase 0.68 ± 0.06. This is in between the maximum visibility of the irradiated donor and the disc bulge and hence it would imply that light-curve maxima arise by a combination of these two emitting regions. However, we note that the uncertainty in the photometric ephemerides of V926 Sco is likely to be higher than stated in A98 due to the limited number of arrival times fitted and their large scatter (Augusteijn, private communication). Therefore, it is possible that light-curve maxima in V926 Sco are also consistent with superior conjunction of the irradiated donor star. This is the most likely scenario because it would be hard to understand an emission source peaking at phase ~0.8 in an irradiation-dominated environment without invoking some strange (and stable) disc configuration.

We have also determined the systemic velocities for the two binaries i.e. −34 ± 5 km s\(^{-1}\) (V801 Ara) and −140 ± 3 km s\(^{-1}\) (V926 Sco). These can be compared with \( V_r \), the radial velocity, relative to the local standard of rest, due to Galactic rotation at the location of the binaries. For the case of V801 Ara, we take \( l = 332.9^\circ, b = -4.8^\circ \) and \( d = 6-7 \) kpc, based on peak fluxes of radius-expansion X-ray bursts for \( M_1 \) = 1.4–2 M\(_\odot\) (Galloway et al. 2005). Assuming the Galactic rotation curve of Nakanishi & Sofue (2003) we find \( V_r \) in the range -103 to -111 km s\(^{-1}\). This is much larger than our systemic velocity which could be explained through the recoil velocity gained by the binary during the supernova explosion which formed the neutron star. Thus, we can set a lower limit to the kick velocity in V801 Ara of \( \geq 70 \) km s\(^{-1}\). Regarding V926 Sco, we take \( l = 346.1^\circ, b = -7.0^\circ \) and a distance of \( d = 9.1 \) kpc (for a canonical 1.4 M\(_\odot\) neutron star, see A98). The Galactic rotation curve at the position of V926 Sco yields \( V_r = -111 \) km s\(^{-1}\), close but significantly lower than our systemic velocity. The difference might also be ascribed to a kick velocity received by the neutron star at birth or, alternatively, a neutron star mass of \( \geq 1.7 \) M\(_\odot\). Note that the latter implies a larger distance of \( d = 10 \) kpc and hence \( V_r = -140 \) km s\(^{-1}\).

### 6.1 System parameters for V801 Ara

The N\( \text{iii} \) λ4640 spot in the Doppler map yields \( K_{\text{em}} = 277 \pm 22 \) km s\(^{-1}\). It must arise on the inner hemisphere of the donor and hence it sets a lower limit to the velocity semi-amplitude of the companion’s centre of mass \( K_2 \). In order to find the real \( K_2 \) we need to calculate the K-correction or \( K_{\text{em}}/K_2 \) for the case of emission lines in illuminated atmospheres, which depends mainly on the binary mass ratio \( q = M_2/M_1 \) (with \( M_2 \), \( M_1 \) the masses of the donor and compact star, respectively) and the disc flaring angle \( \alpha \). The K-correction has been calculated by Muñoz-Darias, Casares & Martínez-Pais (2005) using an irradiation binary code which includes shadowing by an axisymmetric flared disc. The results are tabulated as a function of \( q \) and the inclination angle \( i \) in table 1 of their paper, although the dependence on \( i \) is very weak. The K-correction is constrained between \( \alpha = 0 \) (i.e. we neglect disc shadowing) and the geometrical limit set by emission from the irradiated limb of the donor, i.e. \( K_{\text{em}}/K_2 < 1 - 0.213 q^{3/2} (1 + q)^{1/3} \) (see Muñoz-Darias et al. 2005).

An upper limit on \( q \) is established by taking \( M_1 \geq 1.4 \) M\(_\odot\) and \( M_2 \leq 0.48 \) M\(_\odot\), the largest possible zero-age main-sequence (ZAMS) star fitting in a 3.79 h period Roche lobe (Tout et al. 1996), which leads to \( q \leq 0.34 \). As a first approach, one can assume the empirical mass–radius relation for low-mass stars in cataclysmic variables and LMXBs (see e.g. Warner 1995; Smith & Dhillon 1998) which yields \( M_2 \leq 0.32 \). This, combined with a canonical neutron star of \( M_1 \approx 1.4 \) M\(_\odot\), would lead to a plausible \( q \approx 0.23 \). The K-correction for \( K_{\text{em}} = 277 \pm 22 \) km s\(^{-1}\) and \( q \approx 0.23 \) would yield...
These imply a mass function \( m \) mated from the width of the sharp N III fluorescence emission in V of X-ray eclipses for \( \lambda \) to FWHM 113 km s\(^{-1}\), because fluorescence lines arise in optically thin conditions. Our simulations indicate that \( V_{\text{rot}} \sin i = 92 \pm 16 \text{ km s}^{-1} \) is equivalent to FWHM = 140 \pm 21 km s\(^{-1}\). On the other hand, by substituting \( V_{\text{rot}} \sin i \geq 76 \text{ km s}^{-1} \) and the K-correction for \( \alpha > 0^\circ \) into equation (3), one finds a secure lower limit \( q \geq 0.08 \).

An upper limit to the rotational broadening of the donor star is set by \( V_{\text{rot}} \sin i = 2 \pi R_2 \sin i / P \). By assuming that the donor must be more evolved than a ZAMS star within a 3.79-h Roche lobe, then \( R_2 \lesssim 0.44 R_\odot \) (Tout et al. 1996). This, together with \( i \lesssim 78^\circ \) (lack of X-ray eclipses for \( q \geq 0.08 \)), yields \( V_{\text{rot}} \sin i \leq 138 \text{ km s}^{-1} \).

Further constraints are provided by the study of burst oscillations which can set limits to the neutron star’s projected velocity \( K_1(= q K_2) \). SM02 derived \( 90 \leq K_2 \leq 175 \text{ km s}^{-1} \) by fitting the frequency drift of highly coherent X-ray pulsations observed in an 800 s interval during a superburst. They used a circular orbit model and fixed the zero phase to the ephemeris of G02. We have used our new spectroscopic ephemeris to reanalyse the superburst pulsation data in order to better constrain \( K_1 \). Based on our spectroscopic ephemeris, the pulsation interval during the superburst from V801 Ara comes slightly earlier in orbital phase by 0.032 cycles as compared to the G02 ephemeris. We fit the pulsation data (see SM02 for details on the phase timing analysis) to a circular orbit model with the reference epoch fixed to our new \( T_0 \), and we also fixed the orbital period (using the G02 value). This leaves two free parameters, the projected neutron star velocity, \( K_1 \), and the rest-frame spin frequency, \( v_0 \). We find acceptable fits with a reference epoch within the \( \pm 1 \sigma \) range for our spectroscopic \( T_0 \). The inferred \( K_1 \) velocity ranges from 90 to 113 km s\(^{-1}\) as \( T_0 \) ranges over \( \pm 1 \sigma \). The best-fitting \( K_1 \) values range from 14.6 to 10.6 (with seven degrees of freedom) over this same range, that is, higher velocities are modestly favoured, but given the shortness of the pulse train compared to the orbital period, we do not consider these differences as significant.

With the reference epoch fixed, the statistical error on the velocity is much smaller than the range given above, so \( 90 \sim 113 \text{ km s}^{-1} \) is a robust range for \( K_1 \) at the \( \pm 1 \sigma \) limits of \( T_0 \). The best-fitting \( v_0 \) ranges from 582.041 43 to 582.095 48 Hz, and which may help constrain future searches for a persistent millisecond pulsar in V801 Ara. Fig. 8 summarizes the results of the new timing analysis.

Fig. 9 summarizes all our restrictions in the \( K_2 - q \) parameter space i.e. \( 0 \leq \alpha \leq \max, V_{\text{rot}} \sin i = 76\sim 138 \text{ km s}^{-1} \) and \( K_1 = 90\sim 113 \text{ km s}^{-1} \). The shaded area indicates the region allowed by our constraints, which yields \( q = 0.21\sim 0.34 \) and \( K_2 = 286\sim 433 \text{ km s}^{-1} \). These imply a mass function \( f(M) = M_1 \sin^3 i / (1 + q)^2 = 0.76 \pm 0.47 \text{ M}_\odot \) and hence \( M_1 \sin i = 1.24 \pm 0.77 \text{ M}_\odot \). Clearly the large uncertainties are dominated by the error in \( K_{\text{min}} \) and the uncertainty in the disc flaring angle.

### 6.2 System parameters for V926 Sco

The same reasoning can be applied to V926 Sco. The spot in the N \( \lambda 4640 \) map yields \( K_{\text{min}} = 226 \pm 22 \text{ km s}^{-1} \) whereas the ZAMS mass–radius relation for a 4.65-h Roche lobe leads to \( M_2 \leq 0.58 \text{ M}_\odot \) (Tout et al. 1996) and hence \( q \leq 0.41 \). On the other hand, we measure FWHM (N \( \lambda 4640 \)) = 115 \pm 23 km s\(^{-1}\) which, after deconvolution of the instrumental resolution using Gray rotation profiles as above, yields \( V_{\text{rot}} \sin i \geq 71 \pm 21 \text{ km s}^{-1} \). This lower limit, combined with the K-correction for \( \alpha > 0^\circ \) and equation (3), yields \( q \geq 0.05 \) and,
0.0 and 0.5, when the visibility of the irradiated face of the donor is minimum and maximum, respectively. These spectra are presented in Fig. 11 and show a marked difference for the two binaries: the narrow C iii/N iii lines become significantly enhanced around phase 0.5 (top spectra) for V801 Ara, but not much difference is seen in V926 Sco between phases 0.5 and 0. This clearly supports a higher inclination angle in V801 Ara. Furthermore, the relative contribution of the N iii λ4640 line with respect to the broad base, as estimated through a multi-Gaussian fit, is a factor of ~2 larger for V801 Ara than for V926 Sco. This can be taken as the relative contributions of the heated donor and disc; and hence, strongly suggests that V801 Ara is seen at a higher inclination angle than V926 Sco. This seems at odds with the fact that the optical light curves in V801 Ara and V926 Sco display similar amplitudes, A ≃ 0.2 mag (van Amerongen, Pedersen & van Paradijs 1987; van Paradijs et al. 1990). However, de Jong, van Paradijs & Augusteijn (1996) have shown that light-curve amplitudes are more sensitive to α than i, which might simply imply a thicker disc in V926 Sco and hence light-curve amplitudes cannot be taken as a simple indication of the inclination angle.

6.4 Mass estimate and evolutionary scenarios

Meyer & Meyer-Hofmeister (1982) analysed the effects of X-ray heating in the vertical structure of discs and demonstrated that these are strongly correlated. Even in the absence of irradiation, they found a disc opening angle of ~6°. de Jong et al. (1996) modelled the effects of irradiation in optical light curves and, by comparing with observations of LMXBS, they inferred a mean disc opening angle of 12°. Most of their systems are short-period LMXBs, just like V801 Ara and V926 Sco, and hence it seems justified to speculate what our system parameters would be in this particular case.

Regarding V801 Ara, α = 12° leads to q ≃ 0.25–0.30, K1 ≃ 356–375 km s⁻¹ (see dashed line in Fig. 9) and hence f(M) ≃ 0.81 ± 0.07 M⊙ and M1 sin³ i ≃ 1.32 ± 0.13 M⊙. Assuming that the donor star is a 0.48 - M⊙ ZAMS, then M1 ≃ 1.6–1.9 M⊙ and i ≃ 60–71°. On the other hand, a canonical 1.4 M⊙ would imply an evolved donor with M2 ≃ 0.35–0.42 M⊙ and i ≳ 71°, which is difficult to reconcile with the absence of X-ray eclipses, dips and the low amplitude of the optical modulation (see Section 6.3). Therefore,

<table>
<thead>
<tr>
<th>Parameter</th>
<th>4U 1636-536 V801 Ara</th>
<th>4U 1735-444 V926 Sco</th>
</tr>
</thead>
<tbody>
<tr>
<td>( P_{\text{orb}} ) (d)</td>
<td>0.158 046 93(16)</td>
<td>0.193 833 51(32)</td>
</tr>
<tr>
<td>( T_0 ) (HJD−245 000)</td>
<td>813.531 ± 0.002</td>
<td>813.495 ± 0.003</td>
</tr>
<tr>
<td>( y ) (km s⁻¹)</td>
<td>-34 ± 5</td>
<td>-140 ± 3</td>
</tr>
<tr>
<td>( K_{\text{sm}} ) (km s⁻¹)</td>
<td>277 ± 22</td>
<td>226 ± 22</td>
</tr>
<tr>
<td>( q (M_2/M_1) )</td>
<td>0.21–0.34</td>
<td>0.05–0.41</td>
</tr>
<tr>
<td>( K_1 ) (km s⁻¹)</td>
<td>90–113</td>
<td>-</td>
</tr>
<tr>
<td>( K_2 ) (km s⁻¹)</td>
<td>360 ± 74</td>
<td>298 ± 83</td>
</tr>
<tr>
<td>( f(M) (M_\odot) )</td>
<td>0.76 ± 0.47</td>
<td>0.53 ± 0.44</td>
</tr>
<tr>
<td>( i^\circ )</td>
<td>36–60</td>
<td>27–60</td>
</tr>
</tbody>
</table>

hence \( i \leq 80° \). And, under the assumption that the donor star is more evolved than a ZAMS star, the Roche lobe geometry implies \( K_2 < 0.54 R_\odot \) which, for \( i \leq 80° \), leads to \( V_{\text{acm}} \ sin i \leq 137 \) km s⁻¹.

All these restrictions translate into constraints on the \( K_2 - q \) plane which are presented in Fig. 10. The allowed region results in \( q = 0.05–0.41 \) and \( K_2 = 215–381 \) km s⁻¹, depending on the value of \( \alpha \). These numbers imply \( f(M) = 0.53 ± 0.44 M_\odot \) and, thus, \( M_1 \ sin^3 i = 0.80 ± 0.71 M_\odot \). Unfortunately, we do not have any constraints on \( K_1 \) from burst oscillations and hence our mass restrictions are not as well constrained as for V801 Ara. Our best estimates of the system parameters for both objects are presented in Table 2.

### 6.3 Constraints on the inclination

Further constraints on the stellar masses require the knowledge of the binary inclination. While strict upper limits are set by the absence of X-ray eclipses, lower limits can be established by combining \( M_1 \leq 3.1 M_\odot \) (the maximum mass allowed for a stable neutron star, Rhoades & Ruffini 1974) with our mass function and \( q \) restrictions. This leads to \( i = 36°–74° \) and \( 27°–80° \) for V801 Ara and V926 Sco, respectively. In addition, the physical model of Frank, King & Lasota (1987) indicates \( i \leq 60° \) due to the lack of X-ray dips.

On the other hand, we mentioned in Section 3 that the factor of ~2 narrowness of the He II λ4686 profile in V926 Sco with respect to V801 Ara indicates a lower inclination. To test this hypothesis, we have produced Doppler-corrected averages for V801 Ara and V926 Sco by co-adding all the spectra in two bins centred at orbital phases 0.0 and 0.5, when the visibility of the irradiated face of the donor is minimum and maximum, respectively. These spectra are presented in Fig. 11 and show a marked difference for the two binaries: the narrow C iii/N iii lines become significantly enhanced around phase 0.5 (top spectra) for V801 Ara, but not much difference is seen in V926 Sco between phases 0.5 and 0. This clearly supports a higher inclination angle in V801 Ara. Furthermore, the relative contribution of the N iii λ4640 line with respect to the broad base, as estimated through a multi-Gaussian fit, is a factor of ~2 larger for V801 Ara than for V926 Sco. This can be taken as the relative contributions of the heated donor and disc; and hence, strongly suggests that V801 Ara is seen at a higher inclination angle than V926 Sco. This seems at odds with the fact that the optical light curves in V801 Ara and V926 Sco display similar amplitudes, A ≃ 0.2 mag (van Amerongen, Pedersen & van Paradijs 1987; van Paradijs et al. 1990). However, de Jong, van Paradijs & Augusteijn (1996) have shown that light-curve amplitudes are more sensitive to \( \alpha \) than \( i \), which might simply imply a thicker disc in V926 Sco and hence light-curve amplitudes cannot be taken as a simple indication of the inclination angle.

### Table 2. System parameters. \( T_0 \) indicates zero phase or inferior conjunction of the donor star. Orbital periods \( P_{\text{orb}} \) are from G02 and A98.

![Figure 10](https://academic.oup.com/mnras/article-abstract/373/3/1235/1063835/figure10)

**Figure 10.** Same as Fig. 9 but for V926 Sco, with no pulsation constraints yet.

![Figure 11](https://academic.oup.com/mnras/article-abstract/373/3/1235/1063835/figure11)

**Figure 11.** Doppler-corrected averages of V801 Ara (left-hand panel) and V926 Sco (right-hand panel) in the rest frame of the donor star. Top spectra present averages between orbital phases 0.25 and 0.75 and bottom spectra between 0.75 and 0.25. The sharp C iii/N iii components in V801 Ara are clearly more intense around phase 0.5 than 0, suggesting a higher inclination binary. Spectra have been smoothed by a 2-pixel boxcar.

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a flaring angle of $\alpha \simeq 12^\circ$ seems to support scenarios with ZAMS donors and massive neutron stars. These masses can be reproduced by recent evolutionary scenarios where some LMXBs are supposed to descend from binaries with high-mass donors (Schenker & King 2002). These are significantly evoked at the beginning of the mass-transfer phase and mass is transferred in a thermal time-scale until mass ratio reverses, which can result in the accretion of several tenths of solar masses by the neutron star. This would make V801 Ara similar to other LMXBs such as 4U 1822-371 (Muñoz-Darias et al. 2005).

However, it is also possible to accommodate a canonical neutron star with a MS donor and a plausible inclination angle by pushing the disc flaring angle to higher values. For instance, a star with a MS donor and a plausible inclination angle by pushing tenths of solar masses by the neutron star. This would make V801 Ara transfer phase and mass is transferred in a thermal time-scale until it descends from binaries with high-mass donors (Schenker & King 2002). Alternatively, higher opening angles $\alpha \simeq 16^\circ$ are consistent with canonical neutron stars and main-sequence (or slightly evolved) donors which have evolved from standard LMXBs through a dynamically stable mass-transfer phase.

(v) The lack of an X-ray mass function in V926 Sco prevents to set tighter constraints to the K-correction, mass estimates and evolutionary history in this LMXB.

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REFERENCES


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