Investigating coronal saturation and supersaturation in fast-rotating M-dwarf stars

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ABSTRACT
At fast rotation rates, the coronal activity of G- and K-type stars has been observed to ‘saturate’ and then decline again at even faster rotation rates – a phenomenon dubbed ‘supersaturation’. In this paper, we investigate coronal activity in fast-rotating M-dwarfs using deep XMM–Newton observations of 97 low-mass stars of known rotation period in the young open cluster NGC 2547 and combine these with published X-ray surveys of low-mass field and cluster stars of known rotation period. Like G- and K-dwarfs, we find that M-dwarfs exhibit increasing coronal activity with decreasing Rossby number $N_R$, the ratio of period to convective turnover time, and that activity saturates at $L_X/L_{bol} \simeq 10^{-3}$ for $\log N_R < -0.8$. However, supersaturation is not convincingly displayed by M-dwarfs, despite the presence of many objects in our sample with $\log N_R < -1.8$, where supersaturation is observed to occur in higher mass stars. Instead, it appears that a short rotation period is the primary predictor of supersaturation; $P < 0.3$ d for K-dwarfs and perhaps $P < 0.2$ d for M-dwarfs. These observations favour the ‘centrifugal stripping’ model for supersaturation, where coronal structures are forced open or become radiatively unstable as the Keplerian corotation radius moves inside the X-ray-emitting coronal volume.

Key words: stars: activity – stars: coronae – stars: rotation – open clusters and associations: individual: NGC 2547 – X-rays: stars.

1 INTRODUCTION
X-ray emission from the hot coronae of photospherically cool stars arises from magnetically confined and heated plasma with temperatures in excess of 10⁷ K (see the review by Güdel 2004). X-ray observations of cool stars with convective envelopes have long since shown that X-ray activity increases with the rotation rate and has led to the paradigm that a magnetic dynamo process produces and maintains the required magnetic fields, in analogy to processes observed to occur in the Sun (e.g. Pallavicini et al. 1981; Mangeney & Praderie 1984). The influence of a regenerative dynamo is supported by observations of coronal activity in stars at a range of masses. These demonstrate, in accordance with expectations from dynamo models, that rotation is not the only important parameter. The best correlations are found between increasing magnetic activity and the inverse of the Rossby number (e.g. Noyes et al. 1984; Dobson & Radick 1989; Pizzolato et al. 2003), where the Rossby number is $P/\tau_c$, the ratio of the stellar rotation period, $P$, to the convective turnover time, $\tau_c$. According to stellar models, $\tau_c$ increases towards lower masses (e.g. Gilliland 1986; Kim & Demarque 1996) and hence, for a given rotation period, a K-dwarf has a smaller Rossby number and is more magnetically active than a G-dwarf, where magnetic activity is expressed in a form normalized by the bolometric luminosity (e.g. the ratio of coronal X-ray to bolometric luminosity, $L_X/L_{bol}$).

Many young, cool stars have not lost significant angular momentum and rotate much more rapidly than the Sun, leading to higher coronal X-ray luminosities by several orders of magnitude. At fast rotation rates, magnetic activity (as measured in the corona and chromosphere) appears to ‘saturate’ (e.g. Vilhu & Walter 1987; Stauffer et al. 1994). Saturated coronal activity is manifested as a plateau of $L_X/L_{bol} \simeq 10^{-3}$ in G-dwarfs with rotation periods less than about 3 d. In lower mass stars, the plateau in coronal activity is at a similar level but the rotation period at which it first occurs is longer. A unified picture emerges by plotting X-ray activity against the Rossby number (Stepień 1994; Patten & Simon 1996; Randich et al. 1996; Pizzolato et al. 2003), such that coronal saturation occurs at Rossby numbers of about 0.1 in stars of spectral types G, K and M. This unification in terms of a parameter associated with dynamo efficiency suggests that coronal saturation reflects a saturation of the dynamo itself (Vilhu & Walter 1987), although other

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explanations, such as a redistribution of radiative losses to other wavelengths (Doyley 1996) or changes in magnetic topology with fast rotation (Solanki, Motamen & Keppens 1997; Jardine & Unruh 1999; Ryan, Neukirch & Jardine 2005), must also be considered.

At rotation rates approximately five times faster than required for saturation, it appears that coronal activity turns down again – a phenomenon dubbed ‘supersaturation’ (Prosser et al. 1996). Examples of supersaturated G- and K-stars, with \( L_X / L_{bol} \approx 10^{-3.5} \), have been found in a number of young open clusters (Stauffer et al. 1994, 1997; Patten & Simon 1996; Randich 1998; Jeffries et al. 2006), among the fast-rotating components of contact W UMa binaries (Cudlince & Dupree 1984; Stepien, Schmitt & Voges 2001), and have been suggested as the reason for lower X-ray activity in the fastest-rotating, very young pre-main-sequence (PMS) stars (Stassun et al. 2004; Preibisch et al. 2005; Dahm et al. 2007). Possible explanations for coronal supersaturation include negative feedback in the dynamo (Kitchatinov, Rüdiger & Küker 1994), decreasing coverage by active regions (Stepien et al. 2001), reorganization of the coronal magnetic field (Solanki et al. 1997) or centrifugal stripping of the corona (Jardine 2004).

An important test of these ideas is to look at the coronal properties of fast rotators across a wide range of masses. In particular, it is vital to gauge whether saturation and supersaturation occur at fixed values of the rotation period or Rossby number. This would illuminate which physical mechanisms are responsible. One of the principal gaps in our knowledge is the behaviour of coronal emission for ultra-fast rotating M-dwarfs. These have larger convection zones (as a fraction of the star), longer convective turnover times and hence smaller Rossby numbers at a given rotation period than G- and K-dwarfs. Of course M-dwarfs also have much lower bolometric luminosities than G- or K-dwarfs and so, at a given magnetic activity level, they are harder to observe in the young open clusters where the majority of ultra-fast rotators are found.

The most comprehensive work so far was by James et al. (2000) using X-ray observations for a small, inhomogeneous sample of fast-rotating low-mass stars from the field and open clusters. They found that, like G- and K-type stars, M-dwarfs with periods below \( \sim 6 \) d and Rossby numbers below 0.1 showed saturated levels of X-ray emission with \( L_X / L_{bol} \approx 10^{-3} \). They also claimed tentative evidence for supersaturation in the fastest-rotating M-dwarfs with periods of 0.2–0.3 d.

In this paper, we re-visit the question of saturation and supersaturation of coronal emission in fast-rotating M-dwarfs. We analyse new, deep XMM–Newton observations of a large, homogeneous sample of rapidly-rotating M-dwarfs identified in the open cluster NGC 2547 by Irwin et al. (2008). NGC 2547 has an age of 35–38 Myr (Jeffries & Oliveira 2005; Naylor & Jeffries 2006) and a rich population of low-mass stars (Jeffries et al. 2004). However, the cluster is at \( \sim 400 \) pc and while previous X-ray observations with ROSAT (Jeffries & Tolley 1998) and XMM–Newton (Jeffries et al. 2006) demonstrated an X-ray-active low-mass population, they were insufficiently sensitive to probe the coronal activity of its M-dwarfs in any detail.

In Section 2, we describe the new XMM–Newton observations of NGC 2547 and the identification of X-ray sources with rapidly-rotating M-dwarfs from the Irwin et al. (2008) catalogue. In Section 3, we combine X-ray and optical data, estimate coronal activity levels and examine the evidence for coronal saturation and supersaturation, using a homogeneous sample of fast-rotating M-dwarfs, several times larger than considered by James et al. (2000). In Section 4, we compare our results to those compiled in the literature for G- and K-stars and for other samples of M-dwarfs. In Section 5, we discuss our results in the context of competing models for saturation/supersaturation and our conclusions are summarized in Section 6.

### 2 XMM–NEWTON OBSERVATIONS OF NGC 2547

NGC 2547 was observed with XMM–Newton between UT 22:30:03 on 2007 November 12 and UT 09:30:03 on 2007 November 14 using the European Photon Imaging Counter (EPIC) instrument, for a nominal exposure time of 125.8 ks (Observation ID 0501790101). The two EPIC-MOS cameras and the EPIC-PN camera were operated in full-frame mode (Strüder et al. 2001; Turner et al. 2001), using the medium filter to reject optical light. The nominal pointing position of the observation was RA = 08° 10′ 06″, Dec. = 49° 15′ 42″ (J2000.0).

#### 2.1 Source detection

Version 7.1 of the XMM–Newton SAS (Science Analysis System) was used for the initial data reduction and source detection. Data from the three cameras were individually screened for high background periods and these time-intervals were excluded from all subsequent analyses. Observation intervals were excluded where the total count rate for events with energies \( > 10 \) keV exceeded 0.35 and 1.0 s\(^{-1}\) for the MOS and PN detectors, respectively. The remaining useful exposure times were 107.3, 104.8 and 87.4 ks for the MOS1, MOS2 and PN cameras, respectively, which can be compared with the equivalent exposure times of 29.0, 29.4 and 13.6 ks in the less-sensitive observation analysed by Jeffries et al. (2006).

Images were created using the EVSELECT task and a spatial sampling of 2 arcsec pixel\(^{-1}\). The event lists were filtered to exclude anomalous pixel patterns and edge effects by including only those events with ‘pattern’ \( \leq 12 \) for the MOS detectors and \( \leq 4 \) for the PN detectors. The contrast between background and source events was also increased by retaining only those events in channels corresponding to energies of 0.3–3 keV.

The EDETECT_CHAIN task was used to find sources with a combined maximum log-likelihood value greater than 10 (approximately equivalent to \(-\ln p\), where \( p \) is the probability that the ‘source’ is due to a background fluctuation), in all three instruments combined, over the 0.3–3 keV energy range. We expect one to two spurious X-ray detections at this level of significance, though they would be highly unlikely to correlate with NGC 2547 members, so will not hamper any analysis in this paper. The individual images from each instrument were source-searched first to confirm there were no systematic differences in the astrometry of the brightest sources. Count rates in each detector were determined using vignetting-corrected exposure maps created within the same task. Sources were identified with a signal-to-noise ratio greater than 3, which resulted in the removal of three sources from our list.

To check the EPIC astrometric solution, we cross-correlated all the brightest X-ray sources (those detected with a maximum log likelihood greater than 100) against a list of photometrically selected NGC 2547 members compiled by Naylor et al. (2002, their table 6), which is based on D’Antona & Mazzitelli (1997) isochrones.
and $BVI$ photometry and which incorporates bright cluster members from Clariá (1982). There were 98 correlations found within 6 arcsec of the nominal X-ray position and as discussed in Jeffries et al. (2006), where a similar procedure was followed, these correlations are very likely to be the genuine optical counterparts of the X-ray sources. The mean offset between the X-ray and optical positions was 0.11 arcsec in RA and 0.59 arcsec in Dec. As the optical catalogues have an absolute accuracy better than 0.2 arcsec and an internal precision of about 0.05 arcsec, the X-ray positions were corrected for these offsets. The remaining dispersion in the offsets indicates an additional 1 arcsec uncertainty (in addition to the quoted astrometric uncertainty from the source-searching routines) in the X-ray positions, concurring with the current astrometric calibration assessment of the XMM–Newton science operations centre (Guainazzi 2010).

### 2.2 Cross-correlation with the Irwin catalogue

The purpose of this paper is to study the properties of fast-rotating M-dwarfs, so an investigation of the full X-ray source population is deferred to a later paper. Here, we discuss cross-correlations between the astrometrically corrected X-ray source list and the catalogue of cool stars with known rotation periods in NGC 2547, given by Irwin et al. (2008). The Irwin et al. (2008) catalogue contains precise positions tied to the 2MASS reference frame, rotation periods and photometry in the V and $B$ bands. We found significant systematic differences (of up to 0.2 mag) between the photometry of Irwin et al. (2008) and that found in Naylor et al. (2002) for stars common to both. As the accuracy of the Naylor et al. photometry has support from an independent study by Lyra et al. (2006), we transformed the Irwin photometry using the following best-fitting relationships between the Naylor et al. and Irwin et al. photometry:

$$V = 1.029 V_{\text{Irwin}} - 0.428 \quad \text{rms} = 0.08 \text{mag}.$$  

$$V - I = 1.177 (V - I)_{\text{Irwin}} - 0.305 \quad \text{rms} = 0.10 \text{mag}.$$  

where the calibrations transform the photometry on to the Johnson–Cousins calibration used by Naylor et al. and are valid for $14 < V < 21$ and $1.2 < (V - I) < 3.4$. We take the rms deviation from these relationships as the photometric uncertainty in subsequent analysis.

A maximum correlation radius between X-ray and optical sources of 5 arcsec resulted in 68 correlations from the 97 Irwin et al. (2008) objects that are within the EPIC field of view (there were no correlations between 5-arcsec and our nominal 6-arcsec acceptance threshold). The missing objects were predominantly the optically faintest (see Section 3.2). Experiments involving offsetting the X-ray source positions by 30 arcsec in random directions suggest that fewer than one of these correlations would be expected by chance. The details of the correlations along with count rates, HRs and correlation separations appear in Table 1 (available fully in electronic form only).

### 2.3 Fluxes and coronal activity

To assess magnetic activity levels, X-ray count rates were converted into fluxes using a single conversion factor for each instrument. The use of a single conversion factor is necessitated because few of the X-ray sources that correlate with the Irwin et al. (2008) sample have sufficient counts (>500) to justify fitting a complex spectral model. The median source is detected in the EPIC-PN camera with about 150 counts and a signal-to-noise ratio of only 10. Instead, Table 1.: X-ray detections of sources in the Irwin et al. (2008) catalogue of NGC 2547 members with rotation periods. The table is available electronically (see Supporting Information) and contains 69 rows. Only two rows are shown here as a guide to the form and content. Columns are as follows: (1) – Identification from Irwin et al. (2008); (2) and (3) – RA and Dec. (J2000.0, from Irwin et al. 2008); (4) and (5) – V and $V - I$ magnitudes (modified from the Irwin et al. 2008 values – see Section 2.2); (6) – rotation period (from Irwin et al. 2008); (7) – log bolometric luminosity (assuming a distance of 400 pc); (9) – log convective turnover time (see equation 3); (10) – log Rossby number; (11) and (12) – stellar mass and radius (estimated from the Siess, Dufour & Forestini 2000 models); (13) – Keplerian corotation radius as a multiple of the stellar radius; (14) and (15) – RA and Dec. of the X-ray source; (16) – the maximum log likelihood of the detection; (17) – separation from the optical counterpart; (18) and (19) – total PN count rate (0.3–3 keV); (20) and (21) – PN count rate (0.3–1 keV, the ’$I$‘ band); (22) and (23) – PN count rate (1–3 keV, the ’$H$‘ band); (24) and (25) – PN HR [defined as ($H - S)/(H + S)$]; (26) and (27) – total MOS1 count rate (0.3–3 keV); (28) and (29) – total MOS2 count rate (0.3–3 keV); (30) and (31) – X-ray flux (0.3–3 keV); (32) and (33) – log X-ray to bolometric flux ratio; and (34) and (35) – cross-identification with Naylor et al. (2002) where available.

| Name | RA (J2000) | Dec. | V | V - I | P | BC | log $L_{\text{bol}}/L_{\odot}$ | log $r_{\text{c}}$ | log $N_R$ | M/M$_{\odot}$ | R/R$_{\odot}$ | $R_{K_{\text{Kepler}}}/R$ |
|------|------------|------|---|------|---|----|-----------------------------|-----------------|-----------|-------------|-------------|-----------------|-----------------|
| N2547-1-5-417 | 8.09 25.91 | -49.09 58.4 | 18.69 | 2.80 | 0.865 | -2.28 | -1.40 | 1.80 | -1.86 | 0.37 | 0.47 | 5.76 |
| N2547-1-5-1123 | 8.09 77.1 | -49.08 34.5 | 19.57 | 3.16 | 0.413 | -2.76 | -1.56 | 1.88 | -2.26 | 0.28 | 0.42 | 3.62 |

<table>
<thead>
<tr>
<th>X-ray RA (°, J2000.0)</th>
<th>X-ray Dec.</th>
<th>ML</th>
<th>Sep (arcsec)</th>
<th>PN0 (s$^{-1}$, 0.3–3 keV)</th>
<th>PN0$_{\text{err}}$</th>
<th>PN1 (s$^{-1}$, 0.3–1 keV)</th>
<th>PN1$_{\text{err}}$</th>
<th>PN2 (s$^{-1}$, 1–3 keV)</th>
<th>PN2$_{\text{err}}$</th>
<th>HR</th>
<th>HR$_{\text{err}}$</th>
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<td>122.35782</td>
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<td>421.1</td>
<td>60</td>
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<td>5.23e–04</td>
<td>5.00e–03</td>
<td>4.21e–04</td>
<td>2.23e–03</td>
<td>3.11e–04</td>
<td>-0.38</td>
<td>0.07</td>
</tr>
<tr>
<td>122.32372</td>
<td>-49.1431</td>
<td>36.4</td>
<td>0.57</td>
<td>1.84e–03</td>
<td>3.76e–04</td>
<td>1.33e–03</td>
<td>2.99e–04</td>
<td>5.04e–04</td>
<td>2.28e–04</td>
<td>-0.45</td>
<td>0.20</td>
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</tbody>
</table>

<table>
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<th>MOS1 (s$^{-1}$, 0.3–3 keV)</th>
<th>MOS1$_{\text{err}}$</th>
<th>MOS2 (s$^{-1}$, 0.3–3 keV)</th>
<th>MOS2$_{\text{err}}$</th>
<th>Flux (erg cm$^{-2}$ s$^{-1}$, 0.3–3 keV)</th>
<th>Flux$_{\text{err}}$</th>
<th>log $L_X/L_{\text{bol}}$</th>
<th>log $\Delta L_X/L_{\text{bol}}$</th>
<th>Naylor ID</th>
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<td>1.82e–03</td>
<td>2.41e–04</td>
<td>1.80e–03</td>
<td>2.32e–04</td>
<td>9.59e–15</td>
<td>9.87e–16</td>
<td>-2.92</td>
<td>0.08</td>
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<td>4.85e–04</td>
<td>1.62e–04</td>
<td>5.47e–04</td>
<td>1.82e–04</td>
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<td>6.05e–16</td>
<td>-3.30</td>
<td>0.12</td>
<td>14</td>
</tr>
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</table>
we designed a spectral model that agrees with the mean HR in
the EPIC-PN camera, defined as \((H - S)/(H + S)\), where \(S\) is the
0.3–1.0 keV count rate and \(H\) is the 1.0–3.0 keV count rate.

Our starting point was the analysis of an earlier, much shorter
\textit{XMM–Newton} observation of NGC 2547 (Jeffries et al. 2006).
This showed that single-temperature thermal plasma models
were insufficiently complex to fit the spectra of active stars in NGC
2547. A two-temperature ‘MEKAL’ model (Mewe, Kaastra &
Leidahl 1995) provided a satisfactory description, with \(T_1 \approx
0.6\) keV, \(T_2 \approx 1.5\) keV and an emission measure ratio (hot/cool)
of about 0.7, which was chosen to approximately match the mean
HR. This crude approximation to the differential emission measure
(DEM) of the coronal plasma reasonably matches detailed work on
the coronal DEM of several nearby, rapidly rotating low-mass stars,
which show a DEM maximum at around 10^7 K (García-Alvarez
et al. 2008). It was also established in Jeffries et al. (2006) that
the coronal plasma was best fitted with a subsolar metallicity (\(Z \approx
0.3\)), which seems to be a common feature for very active stars,
including fast-rotating K- and M-dwarfs (e.g. Briggs & Pye 2003;
García-Alvarez et al. 2008).

Adopting the same model, we have used the software package
\textsc{xspec} and instrument response files appropriate for the EPIC-PN
camera at the time of the observations to calculate a conversion
factor from 0.3–3.0 keV count rates to an unabsorbed 0.3–3.0 keV
flux. We assumed an interstellar absorbing column density of neutral
hydrogen \(N_H = 3 \times 10^{20} \text{ cm}^{-2}\) (see Section 2.5). The derived flux
conversion factor is \(1.68 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}\) per count and the derived
HR is –0.42, which closely matches the mean HR in our sample
(see Section 3). Analogous conversion factors for the EPIC-MOS
cameras were derived by dividing the EPIC-PN conversion factor
by the weighted mean ratio of the observed MOS and PN count
rates. This gave conversion factors of \(6.22 \times 10^{-12} \text{ erg cm}^{-2} \text{ s}^{-1}\)
per count for both of the EPIC-MOS cameras.

The unabsorbed 0.3–3 keV X-ray flux for each detected Irwin
et al. (2008) star is found from a weighted average of fluxes from
each detector. Uncertainties in these fluxes arise from the count rate
errors, but we added a further 10 per cent systematic error in quadra-
ture to each detector count rate to account for uncertainties in the
instrument response and in the point spread function modelling
in the \textsc{edetect\_chain} task (e.g. Saxton 2003; Guainazzi 2010). From
the average fluxes, the coronal activity indicator \(L_X/L_{bol}\) was cal-
culated by using the corrected \(V\) magnitudes, an extinction \(A_V =
0.19\), a reddening \(E(V - I) = 0.077\) (see Claria 1982; Naylor et al.
2002) and the relationship between intrinsic \(V - I\) and bolometric
correction described by Naylor et al. (2002). For the red stars in our
sample with \(V - I > 1.5\), these bolometric corrections are based on
the empirical measurements of Leggett et al. (1996). The bolometric
corrections and \(L_X/L_{bol}\) values are reported in Table 1.

2.4 Flux upper limits

There are 29 objects in the Irwin et al. (2008) catalogue within the
\textit{XMM–Newton} field of view (for only a subset of the detectors
in some cases), but not found as sources by the \textsc{edetect\_chain} task.
We inspected the X-ray images at the positions of these sources and
found one example (N2547-1.6-5108), which is a reasonably bright
X-ray source, that appears only in the MOS2 image, and which
was missed by the automated source searching. We evaluated the
X-ray count rates for this object using a 20-arcsec-radius aperture
(see below) and a local estimate of the background. This source has
been added to Table 1. There were no X-ray sources apparent at the
positions of the other 28 objects and X-ray flux upper limits were
derived as follows. In the \textsc{edetect\_chain} task, we generated images
for each detector consisting of smooth models of the X-ray back-
ground, to which were added models of the significantly detected
sources calculated from their count rates and the model point spread
function used to detect and parametrize them. These images were
‘noise-free’ estimates of the expected X-ray background for any
given position. The total expected background was summed within
circles of radius 20 arcsec surrounding each of the undetected Irwin
et al. (2008) objects. The number of observed X-ray counts in those
areas in the original X-ray images was also summed, consisting of
both source and background counts. A 3\(\sigma\) upper limit to the num-
ber of source counts was calculated using the Bayesian approach
20 arcsec radius follows the work of Carrera et al. (2007), who
showed that ‘aperture photometry’ using this radius gave count rates
that closely matched those found in \textsc{edetect\_chain}. The upper lim-
its to the X-ray count rates were determined by dividing by the
average exposure time within the same circular area.

Using this technique, we found that where objects were covered
by both PN and MOS data, the PN data were at least a factor of
2 more sensitive. Rather than attempting to combine the results
from the three instruments, we have either (i) taken the upper limit
from the PN, where PN data are present (23 objects); (ii) taken
the upper limit from one MOS detector where an object was only
covered by that detector (three objects); or (iii) taken the average
upper limit from both MOS detectors (two objects) and divided by
\(\sqrt{2}\), as in these cases, the two upper limits were very similar.
The count-rate upper limits were converted to upper limits in X-ray
flux and upper limits to \(L_X/L_{bol}\) using the procedures described in
the previous subsection. The details of the upper limit measurements
are presented separately in Table 2 (available in electronic form
only).

2.5 Uncertainties in X-ray fluxes

The uncertainties in the log \(L_X/L_{bol}\) values quoted in Table 1 incor-
porate the statistical count-rate uncertainties and the systematic
instrument response uncertainties mentioned in Section 2.3. In addi-
tion, we have included (in quadrature) uncertainties in the bolome-
tric flux due to the photometric uncertainties (or variability) implied
by equations (1) and (2), which amount to about \(\pm 0.07\) dex. The
final quoted uncertainties range from 0.08 to 0.21 dex, with a mean
of 0.10 dex.

Other contributing uncertainties have also been considered. The
X-ray flux conversion factors are rather insensitive to the details of
the spectral model. For instance, doubling the temperature of the hot
component increases the conversion factor by just 3 per cent and the
HR increases to –0.39; varying the metal abundance in the range
0.1 < \(Z\) < 1.0 changes the conversion factor by only \(\pm 5\) per cent;
and doubling the ratio of hot to cool plasma emission measures increases
the conversion factor by 3 per cent and increases the HR to –0.32.
The value assumed for \(N_H\) has a little more effect. The value of \(N_H =
3 \times 10^{20} \text{ cm}^{-2}\) is derived from the cluster reddening of \(E(B-V) =
0.06 \pm 0.02\) (Claria 1982), and the relationship between reddening
and \(N_H\) found by Bohlin, Savage & Drake (1978), and could be
uncertain by factors of 2. Altering \(N_H\) from our assumed value to
either 1.5 \times 10^{20} or 6 \times 10^{20} \text{ cm}^{-2}\) would lead to conversion factors
about 5 per cent smaller or 10 per cent larger and HR would change
to either –0.44 or –0.35, respectively. All these uncertainties are
small compared with those we have already considered and they are
neglected.
The final source of uncertainty is difficult to quantify, but is probably dominant when considering a single epoch of X-ray data, namely the coronal variability of active stars. Active, low-mass stars show frequent X-ray-flaring behaviour on time-scales of minutes and hours, resulting in an upward bias in an X-ray flux estimated, as here, over the course of more than a day. The more active the low-mass star is, the more frequently it exhibits large X-ray flares (Audard et al. 2000). Rather than trying to correct for this, and as the comparison samples in Section 4 have not had any flare exclusion applied, we continue to use the time-averaged X-ray flux to represent coronal activity. An idea of the uncertainties can be gained by looking at similar estimates from more than one epoch. For example, Gagné, Caillault & Stauffer (1995) find that young Pleiades low-mass stars show differences of more than a factor of 2 in their X-ray fluxes only 25 per cent of the time on time-scales of 1–10 yr. Marino et al. (2003) find that the median level of X-ray flux variability of K3-M dwarfs in the Pleiades is about 0.2 dex on time-scales of months. Jeffries et al. (2006) looked at the variability of G- to M-dwarfs in NGC 2547 itself on time-scales of 7 yr, finding a median absolute deviation from equal X-ray luminosity of about 0.1 dex in G- and K-dwarfs, with a hint that the M-dwarfs are slightly more variable. Only about 20 per cent of sources varied by more than a factor of 2. Our conclusion is that we should assume an additional uncertainty of about 0.1–0.2 dex in our single-epoch measurements, but we caution that the distribution is probably non-Gaussian in the sense that a sample will probably contain a small number of objects that are upwardly biased by more than a factor of 2 by large flares.

3 CORONAL ACTIVITY IN THE M-DWARFS OF NGC 2547

3.1 Hardness ratios

In Fig. 1, we show the dependence of the HR, measured by the PN camera, on the intrinsic colour of the star and on the magnetic activity level, expressed as $L_X/L_{bol}$. There is no significant dependence of HR on colour and hence the approximation of a uniform flux conversion factor with spectral type is shown to be reasonable. The weighted mean HR is $-0.42 \pm 0.02$, with a standard deviation of 0.16. The standard deviation is about twice that expected from the statistical errors, hinting at some genuine HR variation. Note that this assumes that the HR uncertainties are symmetric and Gaussian, even though the X-ray data are Poissonian in nature and the HR is strictly limited to $-1 \leq HR \leq 1$ (e.g. see Park et al. 2006). The majority of sources are detected with sufficiently large numbers of counts in both energy ranges and with sufficiently precise count rates to make such an assumption reasonable. The second plot shows there is some evidence that the HR increases slightly with the activity level. A best-fitting linear model is $HR = -0.09(\pm 0.12) + 0.11(\pm 0.04)\log L_X/L_{bol}$, but the residuals suggest there may still be star-to-star variation at a given activity level. Note though that time-variability of the X-ray activity or HR values has not been considered (see Section 2.5) and this might plausibly account for some of this star-to-star variation.

A significant increase in average coronal temperatures (and hence HR) with activity level is well established in field stars (e.g. Telleschi et al. 2005). The relationship between the HR and $L_X/L_{bol}$ found here and the size of the intrinsic scatter are indistinguishable from those found for somewhat higher mass G- and K-stars in NGC 2547 by Jeffries et al. (2006), as is the likelihood of an intrinsic scatter. The mean HR agrees well (by design) with the HR predicted by the spectral model used to calculate the X-ray fluxes. The probable intrinsic variation in the HR at a given $L_X/L_{bol}$ corresponds to variations of about a factor of 2 in the emission measure ratio of the hot and cool plasmas in the two-temperature coronal model. Such variations lead to very small uncertainties in $L_X/L_{bol}$ of the order a few per cent (see Section 2.5) and so we have not attempted to correct for them.

3.2 X-ray activity

Fig. 2(a) shows a $V$ versus $V - I$ colour–magnitude diagram for the stars of the Irwin et al. (2008) sample (with rotation periods), which lie within the XMM–Newton field of view. As a comparison, we show photometric members of NGC 2547 (from Naylor et al. 2002) that also lie within the X-ray field of view and indicate those which have an X-ray counterpart among the 323 significant X-ray sources reported in Section 2.1. Fig. 2(a) shows that the Irwin et al. (2008) sample is only about 50 per cent complete. A significant fraction of photometric cluster candidates at all colours have no detected rotation periods. Most of these non-periodic candidates are X-ray
Figure 1. HRs for the NGC 2547 sample [defined as \((H - S)/(H + S)\), where \(H\) is the 1.0–3.0 keV count rate and \(S\) is the 0.3–1.0 keV count rate in the EPIC-PN camera] as a function of (a) \(V - I\) colour and (b) the X-ray-to-bolometric flux ratio.

Figure 2. (a) A colour–magnitude diagram in NGC 2547 showing low-mass stars with rotation periods (from Irwin et al. 2008) that have significant X-ray detections (solid circles); stars with rotation periods, that are in the XMM–Newton field of view, but have only upper limits to their X-ray activity (open triangles); additional photometric candidate members of NGC 2547 (from Naylor et al. 2002) that are in the XMM–Newton field of view (open diamonds); and those additional photometric candidates that are detected in X-rays (filled diamonds). (b) X-ray activity, expressed as \(\log L_X/L_{bol}\), as a function of colour. We compare the X-ray activity (and 3\(\sigma\) upper limits to X-ray activity) for stars in NGC 2547 with known rotation periods (from Irwin et al. 2008) to the X-ray activity of detected photometric members of NGC 2547 (from Naylor et al. 2002) that have no known rotation period. Almost all photometric candidate members of NGC 2547 are X-ray detected for \(V - I < 2.8\) (see text), so we argue that the members with known rotation periods represent a reasonably unbiased sample with regard to X-ray activity and that the spread of activity at a given colour is less than an order of magnitude for \(V - I > 1.2\).

detected and very likely to be genuine NGC 2547 members (see Jeffries et al. 2006 for a detailed discussion). Only for stars with \(V - I < 1.5\) and \(V - I > 2.8\) are there a significant number of candidates without X-ray detections. For the former, these are likely to be contaminating giants among the photometrically selected members, but the latter are more likely to be genuine cluster members that become too faint for detection at very low luminosities (see below), as indeed are many of the Irwin et al. (2008) objects at similar colours.

Fig. 2(b) plots X-ray activity, expressed as \(\log L_X/L_{bol}\), versus colour. There is a gradually rising mean activity level as we move from K- through to M-dwarfs. The upper envelope is ill defined due to three very high points that seem well separated from the rest of the distribution. A time-series analysis of these three stars reveals that each was affected by a large flare during the course of the XMM–Newton observation. The lower envelope is well defined for \(1 < V - I < 3\) and probably represents a true floor to the level of X-ray activity in cool stars at the age of NGC 2547. Although
our NGC 2547 sample is biased by having detected rotation periods, Irwin et al. (2008) argue that there is not a population of more slowly rotating low-mass stars and Fig. 2(b) also shows that photometrically selected members of NGC 2547 without rotation periods, and which also have a XMM–Newton counterpart, share a similar minimum (and median) level of X-ray activity as a function of colour. This minimum level is not a product of the sensitivity of the X-ray observations, because almost all photometric candidates with \( V - I < 2.8 \) and which lie in the XMM–Newton field of view have been detected (see Fig. 2a).

The important point that emerges from these arguments is that the range of X-ray activity levels in NGC 2547 at a given colour is quite small (less than an order of magnitude) for young K- and M-dwarfs with \( V - I < 2.8 \). For cooler stars with \( V - I > 2.8 \), the X-ray observations become progressively incomplete and we can say very little about the range of X-ray activity here.

### 3.3 Activity versus rotation period and Rossby number

#### 3.3.1 The dependence of activity on the rotation period

Fig. 3 shows the dependence of activity (\( L_X/L_{bol} \)) on the rotation period, considering here only those stars in NGC 2547 with rotation periods given by Irwin et al. (2008). For the purposes of later discussion, we have categorized the stars according to their estimated masses: \( 0.55 < M/M_\odot < 0.95 \) M\(_\odot\) (roughly corresponding to K-stars, blue circles); \( 0.35 < M/M_\odot < 0.55 \) (corresponding to M0-M3 stars, red crosses); and \( M < 0.35 \) M\(_\odot\) (corresponding to stars cooler than M3, black open circles). The masses were estimated from the luminosities of the stars and a 35-Myr isochrone from the evolutionary models of Siess et al. (2000). The bolometric luminosities of our sample were calculated using the corrected, intrinsic \( V \) magnitudes, the bolometric corrections described in Section 2.3 and an assumed distance to NGC 2547 of 400 pc (e.g. Mayne & Naylor 2008).

The choice of the mass division at \( 0.55 \) M\(_\odot\) is to isolate K-dwarfs from the cooler M-dwarfs and at \( 0.35 \) M\(_\odot\) to mark the approximate transition to a fully convective star (Siess et al. 2000). More importantly, the latter division marks the lowest mass at which our sample can be considered complete, in the sense that X-ray upper limits begin to occur in stars of lower mass. The lowest luminosity stars in the sample have masses of \( \gtrsim 0.1 \) M\(_\odot\).

Fig. 3 shows that X-rays have been detected from K- and M-dwarfs with periods ranging from 0.2 to 10 d. Most of the upper limits occur for stars with short periods. Given the possibility of a correlation between X-ray activity and rotation, this at first seems surprising. The reason is that most of the lowest luminosity (and hence lowest mass) objects in the Irwin et al. (2008) catalogue have short rotation periods. As the ratio \( L_X/L_{bol} \) is close to constant in this sample, this means that many short-period objects have low bolometric and X-ray luminosities and are thus harder to detect.

There is a very shallow decline in X-ray activity towards longer periods. As we will show when considering the Rossby numbers for these stars, the reason that the longer period stars do not show much lower X-ray activity is that most of them still have small Rossby numbers and are in the regime where saturated activity levels are expected.

There is some evidence that the very shortest period stars might have lower activity corresponding to ‘supersaturation’. This is primarily based on a group of three very low mass stars with \( P < 0.4 \) d and only upper limits to their X-ray activity and a similar group of three K-stars (\( M > 0.55 \) M\(_\odot\)) where \( L_X/L_{bol} \approx 10^{-3.5} \).

Any correlations, trends or threshold periods may be confused or blurred by the inclusion of a range of spectral types/convection zone depths within the sample plotted in Fig. 3. It was exactly this issue, which led previous authors to consider the use of the Rossby number as a proxy for magnetic dynamo efficiency (e.g. Noyes et al. 1984; Dobson & Radick 1989; Pizzolato et al. 2003).

#### 3.3.2 Rossby numbers

The use of Rossby number raises a problem when dealing with M-dwarfs. The widely used semi-empirical formula of Noyes et al. (1984) predicts convective turnover time, \( \tau_c \), as a function of the \( B - V \) colour. This relationship is poorly defined for \( B - V > 1 \) and has no constraining data in the M-dwarf regime. Theoretically, little work has been done on turnover times at very low masses. Gilliland (1986) calculated that the turnover time at the base of the convection zone increases with decreasing \( T_{eff} \) and mass along the main sequence. These models are limited to stars \( \geq 0.5 \) M\(_\odot\), corresponding to \( T_{eff} \geq 3500 \) K on the main sequence. \( \tau_c \) is roughly linearly dependent on \( \log T_{eff} \) and increases from about 1.2 (when \( \tau_c \) is expressed in days) at \( T_{eff} = 5800 \) K to about 1.85 at 3500 K. Similar calculations, with similar results (except for arbitrary scaling factors), have been presented more recently by Kim & Demarque (1996), Ventura et al. (1998) and Landin, Mendes & Vaz (2010). Ventura et al. (1998) attempted to extend the calculation into the fully convective region, predicting that the convective turnover time would continue to increase. A complication here is that the M-dwarfs of NGC 2547 are not on the main sequence. Gilliland (1986), Kim & Demarque (1996) and Landin et al. (2010) predict that \( \tau_c \) is about 50 per cent larger for stars of 0.5 M\(_\odot\) at an age of \( \sim 30 \) Myr on the PMS.

An alternative approach has been to empirically determine \( \tau_c \) by demanding that activity indicators (chromospheric or coronal) satisfy a single scaling law with Rossby number, irrespective of stellar mass (e.g. Noyes et al. 1984; Stepić 1994). The most recent work has focused on \( L_X/L_{bol} \) as an activity indicator. Using...
An interesting insight was provided by Pizzolato et al. (2003) and Kiraga & Stepien (2007), and a scaled theoretical 200-Myr isochrone from Kim & Demarque (1996). The masses for the NGC 2547 stars were estimated from their luminosities (see text).

Figure 4. Convective turnover time as a function of stellar mass. The open circles show the turnover times adopted for the NGC 2547 sample, calculated according to \( \tau_c \propto L_{bol}/M \) (see text), compared with empirical calibrations from Noyes et al. (1984), Pizzolato et al. (2003) and Kiraga & Stepien (2007), and a theoretical isochrone from Kim & Demarque (1996). The masses for the NGC 2547 stars were estimated from their luminosities (see text).

In the M-dwarf data for NGC 2547 (\( M < 0.55 M_\odot \)), red crosses and open circles), there is no decline in activity at large Rossby numbers. This is probably due to a lack of targets with long enough periods to populate the unsaturated regime (Log \( N_R < -1.8 \)), which may be examples of supersaturated stars, and whilst there are also some with similar activity levels at higher Rossby numbers, it is clear that the K-dwarfs with the lowest Rossby numbers are less active than their equivalents in the M-dwarf subsample. The five K-dwarfs with Log \( N_R < -1.7 \) have a mean log \( L_X/L_{bol} = -3.46 \pm 0.11 \) (standard deviation), while the seven M-dwarfs (with \( M > 0.35 M_\odot \)) at similar Rossby numbers have a mean log \( L_X/L_{bol} = -3.02 \pm 0.21 \).

In the M-dwarf data for NGC 2547 (\( M < 0.55 M_\odot \)), the turnover time has been anchored, such that log \( \tau_c = 1.1 \) for a solar luminosity star, following the convention adopted by Noyes et al. (1984) and Pizzolato et al. (2003).

In Fig. 4, we compare the \( \tau_c \) values calculated for our sample as a function of mass, with the theoretical and empirical relationships discussed above. Overall, our \( \tau_c \) values lie a little below (but not significantly) the Pizzolato et al. (2003) calibration and marginally above the values determined by Kiraga & Stepien (2007) and a theoretical isochrone from Kim & Demarque (1996).1 From the discussion by these latter authors and their fig. 3, it is clear that any discrepancy between theory and data could be explained by the younger age of NGC 2547. Stars with \( M < 1.0 M_\odot \) are still approaching the main sequence at 30–40 Myr, their \( \tau_c \) values are still falling and one would expect them to have larger \( \tau_c \) than for a 200-Myr isochrone or indeed M-dwarf field stars. Unfortunately, Kim & Demarque (1996) did not provide \( \tau_c \) isochrones at these younger ages. The semi-empirical relationship between \( \tau_c \) and mass proposed by Noyes et al. (1984) is also shown. As discussed above, this has little or no constraining data below about \( 0.7 M_\odot \) and our adopted turnover times in this regime are much larger.

We conclude that our adopted \( \tau_c \) values and hence Rossby numbers are quite consistent with previous work, although systematic uncertainties at the level of \( \sim 0.2 \) dex must be present when comparing stars at \( M < 0.5 M_\odot \) with solar mass stars. Tables 1 and 2 include our calculated convective turnover times and Rossby numbers.

3.3.3 The dependence of activity on Rossby number

Fig. 5 shows the dependence of \( L_X/L_{bol} \) on Rossby number. Dashed loci indicate the approximate divisions between the unsaturated, saturated and supersaturated regimes found from data for G- and K-stars (see Randich 1998; Pizzolato et al. 2003 and Section 4). There is some evidence that the K-stars in our sample (\( M > 0.55 M_\odot \), blue circles) are following the pattern seen in other young clusters. Most of the K-dwarfs appear to have a saturated level of magnetic activity, although we do not clearly see any fall in activity levels at the largest Rossby numbers in our sample. There are three K-dwarfs with \( L_X/L_{bol} \simeq 10^{-1.5} \) at Log \( N_R < -1.8 \), which may be examples of supersaturated stars, and whilst there are also some with similar activity levels at higher Rossby numbers, it is clear that the K-dwarfs with the lowest Rossby numbers are less active than their equivalents in the M-dwarf subsample. The five K-dwarfs with Log \( N_R < -1.7 \) have a mean log \( L_X/L_{bol} = -3.46 \pm 0.11 \) (standard deviation), while the seven M-dwarfs (with \( M > 0.35 M_\odot \)) at similar Rossby numbers have a mean log \( L_X/L_{bol} = -3.02 \pm 0.21 \).

In the M-dwarf data for NGC 2547 (\( M < 0.55 M_\odot \)), red crosses and open circles), there is no decline in activity at large Rossby numbers. This is probably due to a lack of targets with long enough periods to populate the unsaturated regime (Log \( N_R > -0.8 \), Stauffer et al. 1997). However, there is no doubt that an unsaturated coronal activity regime exists for field M-dwarfs with long rotation periods (see Kiraga & Stepien 2007 and Section 4).

The lack of obvious supersaturation among the M-dwarfs is more significant. The phenomenon is claimed to begin in G- and K-dwarfs

1 The \( \tau_c \) values from Kim & Demarque (1996) were multiplied by 0.31 to anchor them at log \( \tau_c = 1.1 \) for a solar mass star.

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**Figure 4.** Convective turnover time as a function of stellar mass. The open circles show the turnover times adopted for the NGC 2547 sample, calculated according to \( \tau_c \propto L_{bol}/M \) (see text), compared with empirical calibrations from Noyes et al. (1984), Pizzolato et al. (2003) and Kiraga & Stepien (2007), and a theoretical isochrone from Kim & Demarque (1996). The masses for the NGC 2547 stars were estimated from their luminosities (see text).

**Figure 5.** X-ray activity as a function of Rossby number. The sample is divided by mass and shown with symbols as in Fig. 3. The dashed lines indicate divisions between unsaturated, saturated and supersaturated coronal activity defined in the literature for G- and K-stars (see Section 3.3.3).
with \( \log N_R \leq -1.8 \) (Patterson & Simon 1996; Stauffer et al. 1997; Randich 1998) and there are plenty of stars in our sample with much smaller Rossby numbers than this, mostly among the lowest-mass M-dwarfs. A complication here is that the cited papers used relationships in Noyes et al. (1984) to calculate \( \tau_R \). However, Fig. 4 shows that Rossby numbers estimated for G- and K-dwarfs \( (M > 0.55 \text{ M}_\odot) \) using the Noyes et al. (1984) formula would be \( \lesssim 0.2 \) dex larger than those calculated in this paper for a star of similar mass, so the conclusion is robust.

It is possible that supersaturation begins in the M-dwarfs of NGC 2547 at very low Rossby numbers, say, \( \log N_R < -2.3 \), but this is only indicated by three upper limits. James et al. (2000) also claimed tentative evidence of supersaturation in their collected sample of field and cluster M-dwarfs. Their claim was based on two stars, VX47 and VXR60b in IC 2391, which have \( (V-I) = 1.7 \) and 2.06, respectively, and according to their luminosities would both be classified as late K-dwarfs \( (M > 0.55 \text{ M}_\odot) \) with \( \log N_R \simeq -2 \) in our classification scheme.

Our conclusion from the NGC 2547 sample is that if supersaturation occurs in M-dwarfs, then it occurs at Rossby numbers that become (in the lowest-mass stars) at least a factor of 3 lower than in supersaturated G- and K-dwarfs.

### 4 Combination with Other Data Sets

The NGC 2547 data suggest that supersaturation does not occur at a single critical Rossby number, irrespective of spectral type (see Fig. 5). Instead, it seems more plausible that supersaturation may occur below some critical period \((\lesssim 0.4 \text{ d}, \text{ see Fig. 3})\). This interpretation is hampered by relatively few targets with very short rotation periods and also few targets of higher mass, where the very different convective turnover times would result in quite different Rossby numbers at the same rotation period. To increase our statistics and to make a better comparison with a larger sample of higher mass stars, we combined our data set with published data for stars with known rotation periods in young open clusters and the field. The main sources of the comparison data are catalogues of X-ray activity in field M-dwarfs by Kiraga & Stepien (2007) and in field and cluster dwarfs by Pizzolato et al. (2003). We have also used the recent catalogue of rotation periods in Hartman et al. (2010, see below) to add many new stars from the young Pleiades cluster to the rotation–activity relationship. This large sample covers a range of ages: NGC 2547 at 35 Myr (Jeffries & Oliveira 2005); IC 2391 and IC 2602 at \( \simeq 50 \text{ Myr} \) (Barrado y Navascues, Stauffer & Jayawardhana 2004); Alpha Per at \( \simeq 90 \text{ Myr} \) (Stauffer et al. 1999); Pleiades at \( \simeq 125 \text{ Myr} \) (Stauffer, Schultz & Kirkpatrick 1998); Hyades at \( \simeq 625 \text{ Myr} \) (Perryman et al. 1998); and field stars that have ages from tens of Myr to many Gyr.

There are important issues to address regarding the completeness of comparison samples. For NGC 2547, we started with stars of known rotation period and determined their X-ray activity level or upper limits to their X-ray activity, if they could not be detected. Almost all stars were detected down to about 0.35 \text{ M}_\odot \text{ (spectral type M3)} \) and there were a mixture of detections and upper limits at lower masses. The samples of stars with known X-ray activity and rotation period found in the literature have been generated in a different way. Generally, field star samples have been compiled by matching objects with known rotation periods to X-ray sources in the ROSAT All-Sky Survey (RASS, Voges et al. 1999). In clusters, the data are mostly from ROSAT pointed observations, from which detected X-ray sources were matched with known cluster members. The problem is, especially when searching for evidence of supersaturation, that we must be sure that the X-ray observations were sensitive enough to have detected examples of supersaturated stars \((\text{say with } L_X/L_{bol} \leq 10^{-3.5})\). This difficulty is exacerbated for active M-dwarfs, because they frequently flare, so there is a possibility that what has been reported in the literature is an X-ray bright tail, disguising a hidden population of undetected, supersaturated M-dwarfs.

For field stars at a given \( V \) magnitude, and for a given X-ray flux detection threshold, the corresponding \( L_X/L_{bol} \) detection threshold becomes smaller in cooler stars, because the magnitude of the V-band bolometric correction increases. The catalogue of M-dwarfs with rotation periods compiled by Kiraga & Stepien (2007) was taken from optical samples with \( V < 12.5 \) and correlated with ROSAT data, mainly from the RASS. The flux sensitivity of the RASS varies with ecliptic latitude, but the minimum detectable count rate over most of the sky is \( \simeq 0.015 \text{ counts s}^{-1} \). For a typical coronal spectrum, and neglecting interstellar absorption for nearby stars, this equates to a flux sensitivity of \( 10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1} \).

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Per and Pleiades clusters; and (iii) a 50 Myr age for stars in the IC 2391 and IC 2602 clusters. Rossby numbers were calculated using equation (3). $L_X/L_{bol}$ values were taken from Pizzolato et al. (2003) and Kiraga & Stepień (2007), or from Stauffer et al. (1994) and Micela et al. (1999) for the Pleiades. The X-ray fluxes in these papers are quoted in the 0.1–2.4 keV ROSAT passband. The spectral model adopted for NGC 2547 in Section 3.3 predicts that a flux in the 0.1–2.4 keV band would only be 6% per cent higher than the 0.3–3 keV fluxes reported in Table 1. This difference is small enough to be neglected in our comparisons.

The combined data are shown in Fig. 6, where correlations between activity and period, and activity and Rossby number are investigated. The stars have been split into three mass ranges (the same subsets as in Section 3.3) to see whether period or Rossby number is the best parameter with which to determine X-ray-activity levels across a broad range of masses and convection zone depths. The number of stars taken from each of the clusters and the field in each of the three mass ranges is: NGC 2547 (45 for $M/M_\odot < 0.35$, 25 for $0.35 < M/M_\odot < 0.55$, 26 for $0.55 < M/M_\odot < 0.95$); IC 2391/2602 (0, 3, 24); Alpha Per (0, 2, 29); Pleiades (10, 38, 71); Hyades (0, 1, 8); and Field (8, 27, 44).

The additional data, particularly more fast rotating K-dwarfs and slow-rotating M-dwarfs, clarifies a number of issues:

(i) The left-hand panels of Fig. 6 show that both slowly rotating K- and M-dwarfs have a decreasing level of coronal activity at long periods. However, the rotation period alone appears to be a poor indicator of X-ray activity for slowly rotating stars. K-dwarfs and M-dwarfs follow different rotation–activity relationships at long periods – compare the M-dwarfs with the (red) solid locus, which approximately indicates the relationship followed by the K-dwarfs. The rotation period at which saturation sets in may be longer for lower mass stars.

(ii) The addition of further fast-rotating K-dwarfs, mainly from other young clusters, clearly demonstrates a supersaturation effect at $P < 0.3$ d. The evidence for supersaturation in M-dwarfs is not convincing: there are two upper limits (from NGC 2547 and also present in Fig. 3) that may suggest supersaturation at $P \simeq 0.2$ d in the lowest-mass stars. However, the few additional short-period M-dwarfs from the comparison samples show no indication of supersaturation down to periods of 0.25 d.

(iii) The Rossby number (or at least the Rossby number found from the convective turnover times that we have calculated) unifies the low-activity side of the rotation–activity correlation (in the right-hand panels of Fig. 6). The Rossby number is capable of predicting the level of X-ray activity with a modest scatter and applies to a wide range of masses and convection zone depths, including some stars, which are fully or nearly fully convective. Coronal saturation occurs, within the limitations of the small number statistics for the lowest-mass stars, at a similar range of Rossby numbers ($-1.8 < \log N_R < -0.8$) for all low-mass stars and at a similar value of $L_X/L_{bol}$.

(iv) For $\log N_R < -1.8$, the Rossby number does less well in predicting what happens to the coronal activity. Whilst there is evidence that some G- and K-dwarfs supersaturate at $\log N_R < -1.8$, there is a large scatter. There is no evidence for declining activity at low Rossby numbers among the M-dwarfs, unless the two upper limits at $\log N_R < -2.5$ in NGC 2547 mark the beginning of supersaturation at much lower Rossby numbers. Comparing the left-hand and right-hand panels of Fig. 6, it may be that, for fast-rotating stars, the rotation period is the better parameter to determine when and if supersaturation occurs.

(v) None of these conclusions is affected by the inclusion or otherwise of cluster M-dwarfs from Pizzolato et al. (2003) that may be subject to an upward selection bias.

(vi) There are three K-dwarfs (one detection – HII 1095 and two upper limits – HII 370 and HII 793) in the Pleiades sample, with $P$ in the range 0.87–0.94 d, which have anomalously low X-ray activity. We do not believe these are examples of coronal supersaturation, but more likely they are stars where the period found by Hartman et al. (2010) is a 1-d alias of a true longer period.

5 DISCUSSION

A summary of the findings of Sections 3 and 4 would be that X-ray activity rises with decreasing Rossby number, reaches a saturation plateau at a critical Rossby number ($\log N_R \simeq -0.8$) that is approximately independent of the stellar mass and then becomes saturated at a smaller Rossby number in a way that is dependent on the stellar mass – either in the sense that supersaturation does not occur at all in low-mass M-dwarfs or if it does, it occurs at much lower Rossby numbers than for K-dwarfs. The Rossby number is the parameter of choice to describe the occurrence of saturation and the decline of activity at slower rotation rates, but the rotation period may be a better parameter for predicting the occurrence of supersaturation at $P \sim 0.3$ d in K-dwarfs and perhaps $P \sim 0.2$ d in lower mass stars.

There are a number of ideas that could explain the progression from the unsaturated to saturated to supersaturated coronal regimes: (i) feedback effects in the dynamo itself may manifest themselves at high rotation rates. The increasing magnetic field could suppress differential rotation and the capacity to regenerate poloidal magnetic field (e.g. Robinson & Durney 1982; Kitchatinov & Rüdiger 1993; Rempel 2006); (ii) the photosphere may become entirely filled with equipartition fields (e.g. Reiners, Basri & Browning 2009). This leads to saturation of magnetic activity indicators in the corona and chromosphere. At faster rotation rates, it is possible that the magnetic field emerges in a more restricted way (e.g. constrained to higher latitudes – Solanki et al. 1997; Stepien et al. 2001), reducing the filling factor again and leading to supersaturation; and (iii) at high rotation rates, centrifugal forces could cause a rise in pressure in the summits of magnetic loops, which then break open or become radiatively unstable, reducing the emitting coronal volume and emission measure (Jardine & Unruh 1999).

The results from NGC 2547 and Fig. 6 favour an explanation for saturation in terms of saturation of the dynamo or magnetic filling factor, rather than a simple dependence on the rotation rate. The coronal activity of low-mass and very low mass M-dwarfs in the right-hand panels of Fig. 6 is well described by the same relationship between activity and Rossby number as the higher mass K-dwarfs, at least for $\log N_R > -1.8$. The Rossby number at which coronal activity saturates is also broadly similar across a wide range of masses. These facts suggest that X-ray activity levels depend primarily on Rossby number, which is a key parameter describing the efficiency of a magnetic dynamo (Durney & Robinson 1982; Robinson & Durney 1982). Supporting evidence for an explanation involving saturation of magnetic flux generation comes from direct measurements of magnetic flux in fast-rotating M-dwarfs (Saar 1991; Reiners et al. 2009) and from chromospheric magnetic activity indicators, which also show saturation at Rossby numbers of $\lesssim 0.1$ (Cardini & Cassatella 2007; Marsden, Carter & Donati 2009). A caveat to this conclusion is that the convective turnover times and hence Rossby numbers of the lowest-mass stars in our
Figure 6. X-ray activity as a function of the rotation period (left-hand column) or as a function of Rossby number (right-hand column) for low-mass stars in NGC 2547 and for literature compilations of cluster and field dwarfs as explained in the text. The plots are separated according to the estimated masses of the stars (top panels: K-stars with $0.55 < M/M_\odot < 0.95$; middle panels: M-stars with $0.35 < M/M_\odot < 0.55$; bottom panels: M-stars with $M < 0.35 M_\odot$), the symbols are those used in Fig. 3). The loci in each plot are by-eye trends identified in the K-stars and then repeated in the subsequent plots to highlight differences with stellar mass. Cluster M-dwarfs from Pizzolato et al. (2003) may be subject to an upward bias (see text) and are marked with asterisks.
sample are uncertain. In fact, the semi-empirical scaling of $\tau_c \propto L_{bol}^{1/2}$ was designed to minimize the scatter at large Rossby numbers (Pizzolato et al. 2003). Clearly, better theoretical calculations of $\tau_c$ are desirable for $M < 0.5 M_\odot$.

The phenomenon of supersaturation does not seem to be well described by Rossby numbers calculated using similar $\tau_c$ estimates. Some G- and K-dwarfs show supersaturation at log $N_R \approx -1.8$, but using the same $\tau_c$ values that tidy up the low-activity side of Fig. 6 implies that M-dwarfs do not supersaturate, unless at log $N_R \approx -2.5$. This suggests that supersaturation may not be intrinsic to the dynamo mechanism, a point of view supported by the lack of supersaturation in the chromospheric emission from very rapidly rotating G- and K-dwarfs (Marsden et al. 2009). It is worth noting that the lack of supersaturation in M-dwarfs is probably not related to any fundamental change in dynamo action, such as a switch from an interface dynamo to a distributed dynamo as the convection zone deepens. There are sufficient M-dwarfs in Fig. 6 with $M > 0.35 M_\odot$, which should still have radiative cores (Siess et al. 2000), to demonstrate that they also show no signs of supersaturation at the Rossby numbers of supersaturated G- and K-dwarfs.

Stepień et al. (2001) put forward a hypothesis that a latitudinal dependence of the heating flux at the base of the convection zone is caused by the polar dependence of the local gravity in rapid rotators. This could result in strong poleward updrifts in the convection zone that sweep magnetic flux tubes to higher latitudes, leaving an equatorial band that is free from magnetically active regions, hence reducing the filling factor of magnetically active regions in the photosphere, chromosphere and corona. In this model, supersaturation occurs when the ratio of the centrifugal acceleration at the surface of the radiative core to the local gravitational acceleration reaches some critical value $\gamma$, that is,

$$GM_\odot \frac{R_\odot}{L_{bol}} = \frac{\gamma}{4 \pi^2} R_c P^{-2},$$

where $M_\odot$ and $R_\odot$ are the mass and radius of the radiative core.

Leaving aside the issue of what happens in fully convective stars, we can make the approximation that $M_\odot R_\odot^{-3}$ is approximately proportional to the central density, so that the period $P_\odot$ at which supersaturation would be evident depends on the central density as $P_\odot \propto \rho_c^{-1/2}$ (assuming that the convection zone rotates as a solid body). The central density as a function of mass is very time-dependent on the PMS. At 35 Myr, a star of 0.3 $M_\odot$ has $\rho_c \approx 3000$ kg m$^{-3}$, while a 0.9-$M_\odot$ star has $\rho_c = 6900$ kg m$^{-3}$ (Siess et al. 2000). At 100 Myr, however, the core of the 0.3-$M_\odot$ star is nearly three times denser, while the 0.9-$M_\odot$ star remains almost unchanged. Thanks to the inverse square root dependence on density, however, one would expect supersaturation to occur at quite similar periods in objects with a range of masses and certainly with a variation that is much smaller than if supersaturation occurred at a fixed Rossby number. However, there is no evidence of supersaturation in the chromospheric activity of G- and K-dwarfs, which are coronally supersaturated (Marsden et al. 2009), and this suggests that a simple restriction of the filling factor due to a polar concentration of the magnetic field is not the solution.

Jardine & Unruh (1999) have shown that dynamo saturation or complete filling by active regions may not be necessary to explain the observed plateau in X-ray activity and its subsequent decline at very fast rotation rates. In their model, centrifugal forces act to strip the outer coronal volume, either because the plasma pressure exceeds what can be contained by closed magnetic loops (see also Ryan et al. 2005) or because the coronal plasma becomes radiatively unstable beyond the Keplerian corotation radius (Collier-Cameron 1988). The reduced coronal volume is initially balanced by a rising coronal density, causing a saturation plateau, but at extreme rotation rates, as more of the corona is forced open, the X-ray emission measure falls (see also Jardine 2004).

We might expect centrifugal effects to become significant in the most rapidly rotating stars and whilst there will clearly be a correlation with Rossby number, there will be an important difference in mass dependence. The key dimensionless parameter in the centrifugal stripping model is $\alpha_c$, the corotation radius expressed as a multiple of the stellar radius,

$$\alpha_c = \left( \frac{GM_\odot P^3}{4 \pi^2 R_c^3} \right)^{1/3} \propto M_\odot^{1/3} R_\odot P^{-2/3},$$

where $P$ is the rotation period. Thus, coronal activity should saturate at some small value of $\alpha_c$ and then supersaturate at an even smaller $\alpha_c$. In the samples considered here, there is a two order of magnitude range in $P$ but a much smaller range in $M_\odot^{1/3} R_\odot^{-1}$. Hence, we expect to see saturation and supersaturation occur at short periods corresponding to some critical values of $\alpha_c$. However, in stars with lower masses and smaller radii, these critical $\alpha_c$ values will be reached at shorter periods, such that $P_\odot \propto M^{1/2} R^{3/2}$, which in NGC 2547 varies from 0.9 (in solar units) for the most massive stars in our sample to 0.5 in the lowest-mass stars. Hence, supersaturation in the M-dwarfs would occur at shorter periods than for K-dwarfs by a factor approaching 2.

To test these ideas, Fig. 7 shows $L_X/L_{bol}$ as a function of both $log N_R$ and $\alpha_c$, with the stars grouped into mass subsets in a similar way to Sections 3 and 4. The stellar radii and masses for the comparison samples were estimated from their luminosities and the Siess et al. (2000) models as described in Sections 3 and 4.

The $\alpha_c$ parameter, like the rotation period, is a poor predictor of what happens to X-ray activity in the slowly-rotating and low-activity regimes. Saturated levels of coronal activity are reached for $\alpha_c = 10$–30, dependent on the mass of the star. We interpret this to mean that centrifugal forces have a negligible effect on coronal structures in this regime. For large values of $\alpha_c$ and concomitantly large values of log $N_R$, we suppose that coronal activity is determined by the efficiency of the magnetic dynamo, hence explaining the reasonably small scatter within the shaded area of the left-hand panel of Fig. 7. On the other hand, supersaturation seems to be achieved when $\alpha_c \lesssim 2.5$, and the modest scatter within the shaded area of the right-hand panel of Fig. 7, compared to that for log $N_R < -1.8$ in the left-hand panel, suggests that centrifugal effects may start to control the level of X-ray emission somewhere between this value and $\alpha_c \sim 10$.

In this model, it now becomes clear that the reason we have no clear evidence for supersaturation in M-dwarfs is that they are not spinning fast enough for their coronae to be affected by centrifugal forces. There are only two very low mass M-dwarfs in our sample (from NGC 2547) with $\alpha_c < 2.5$ and they do have upper limits to their activity that could be indicative of supersaturation.

If the corona is limited at some small multiple of the corotation radius, it implies that X-ray-emitting coronal structures exist up to this extent above the stellar surface. The arguments for and against the presence of such extended coronal structures are summarized by Güdel (2004). Perhaps the best-supporting evidence comes from the ‘slingshot prominences’ observed to occur around many rapidly rotating stars, which often form at or outside the corotation radius (e.g., Collier-Cameron & Robinson 1989; Jeffries 1993; Barnes et al. 1998), which may signal the action of the centrifugal stripping process.
Coronal supersaturation in M-dwarfs

6 SUMMARY

We have determined the level of X-ray activity (in terms of $L_X/L_{bol}$) for a sample of low-mass K- and M-dwarfs with rotation periods of 0.2–10 d, in the young ($\sim$35 Myr) open cluster NGC 2547. A deep XMM–Newton observation is able to detect X-rays from almost all stars with $M \geq 0.35 M_\odot$ and provides detections or upper limits for many more with lower masses. Most targets exhibit saturated levels of X-ray activity ($L_X/L_{bol} \simeq 10^{-3}$), but a few of the most rapidly rotating showed evidence of lower, 'supersaturated' activity. The evidence for supersaturation in M-dwarfs with $M < 0.55 M_\odot$ is weak, limited to three objects with short periods and very small Rossby numbers, which have $3\sigma$ upper limits to their coronal activity of $L_X/L_{bol} \lesssim 10^{-3.3} - 10^{-3.4}$. These data were combined with X-ray measurements of fast-rotating low-mass stars in the field and from other young clusters, and the results were considered in terms of stellar rotation period and in terms of the Rossby number, which is thought to be diagnostic of magnetic dynamo efficiency. The main result is that while coronal saturation appears to occur below a threshold Rossby number, log $N_R \lesssim -0.8$, independent of stellar mass, there is evidence that supersaturation does not occur at a fixed Rossby number. Supersaturation in the lowest-mass M-dwarfs occurs, if at all, at Rossby numbers that are at least three times smaller than those for which supersaturation is observed to occur in G- and K-dwarfs; there is no evidence for supersaturation in M-dwarfs with log $N_R > -2.3$. Instead, it appears that a rotation period <0.3 d is a more accurate predictor of when supersaturation commences and there are only a few M-dwarfs rotating at these periods in our sample.

A caveat to this result is that our calculated Rossby numbers rely on rather uncertain semi-empirical values of the convective turnover time. However, these turnover times do unify the slowly-rotating side of the rotation–activity relation in the sense that the use of Rossby numbers significantly reduces the scatter in this relationship and predicts a common threshold Rossby number for coronal saturation.

These phenomena can be interpreted within a framework where coronal saturation occurs due to saturation of the dynamo itself at a critical Rossby number, or perhaps due to complete filling of the surface by magnetically active regions. Coronal saturation is probably not an intrinsic property of the dynamo, but instead associated with topological changes in the coronal magnetic field with fast rotation rates. The observations favour the centrifugal stripping scenario of Jardine & Unruh (1999) and Jardine (2004), in which the reduction of the available coronal volume due to instabilities induced by centrifugal forces leads to a drop in X-ray emission as the Keplerian corotation radius moves in towards the surface of the star.

If centrifugal stripping is the correct explanation for supersaturation, then M-dwarfs should supersaturate at shorter periods than K-dwarfs, by factors of up to ~2. The data analysed here are sparse but consistent with this idea. Determining the X-ray emission from a small sample of rapidly rotating ($P < 0.25$ d) M-dwarfs would resolve this issue. The centrifugal stripping idea may also explain the positive correlation between X-ray activity and rotation period seen in very young PMS stars by Stassun et al. (2004) and Preibisch et al. (2005). It could be that the fastest-rotating young PMS stars are centrifugally stripped, whilst those of slower rotation are merely saturated. Investigating this in detail faces formidable observational and theoretical difficulties, not least the estimation of the intrinsic, non-accretion-related X-ray emission, individual absorption column densities for stars and the determination of PMS stellar radii, masses and convective turnover times.

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REFERENCES

SUPPORTING INFORMATION
Additional Supporting Information may be found in the online version of this article:
Table 1. X-ray detections of sources in the Irwin et al. (2008) catalogue of NGC 2547 members with rotation periods.
Table 2. The properties of stars from the Irwin et al. (2008) catalogue that have known rotation periods but were not detected within the XMM–Newton field.

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