The deepest radio study of the pulsar wind nebula G21.5−0.9: still no evidence for the supernova shell

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ABSTRACT
We report on sensitive new 1.4-GHz Very Large Array radio observations of the pulsar wind nebula G21.5−0.9, powered by PSR J1833−1034, and its environs. Our observations were targeted at searching for the radio counterpart of the shell-like structure seen surrounding the pulsar wind nebula in X-rays. Some such radio emission might be expected as the ejecta from the ∼1000 yr old supernova expand and interact with the surrounding medium. We find, however, no radio emission from the shell, and can place a conservative 3σ upper limit on its 1-GHz surface brightness of 7 × 10−22 W m−2 Hz−1 sr−1, comparable to the lowest limits obtained for radio emission from shells around other pulsar wind nebulae. In addition, our wide-field radio image also shows the presence of two extended objects of low surface brightness. We re-examine previous 327-MHz images, on which both the new objects are visible. We identify the first, G21.64−0.84, as a new shell-type supernova remnant, with a diameter of ∼1 arcmin and an unusual double-shell structure. The second, G21.45−0.59, ∼1 arcmin in diameter, is likely an H I region.

Key words: ISM: supernova remnants.

1 INTRODUCTION
The Crab-like supernova remnant (SNR) G21.5−0.9 (SNR 021.5−00.9) harbours a pulsar wind nebula (PWN), powered by the 61.86 ms pulsar, PSR J1833−1034. Despite having a high spin-down luminosity of 3.3 × 1037 erg s−1, PSR J1833−1034 produces only faint pulsed emission, and was only recently discovered (Gupta et al. 2005; Camilo et al. 2006). Radio imaging of the PWN spanning a ∼15-yr period has shown that it is expanding quite rapidly, having an expansion age of 870 ± 150 yr (Bietenholz & Bartel 2008), making PSR J1833−1034 one of the youngest pulsars known. Using a determination of the hydrogen column density, CO and H I measurements, Camilo et al. (2006) determined that the distance to G21.5−0.9 was 4.7 ± 0.4 kpc, which is consistent with, but more accurate than earlier determinations (e.g. Davelaar, Smith & Becker 1986; Safi-Harb et al. 2001). We will adopt the value of 4.7 kpc.

The PWN is bright in both the radio and X-ray, having luminosities of ∼10 and ∼1 per cent, respectively, of those of the Crab nebula.

Recent radio images of G21.5−0.9 show a flat-spectrum PWN, with an angular diameter of ∼1 arcmin (Bietenholz & Bartel 2008), which has filamentary structure similar to that seen in the Crab nebula. The pulsar is expected to have been born in a supernova explosion, and since it is quite young, one might expect to see some emission associated with the expanding shell of supernova ejecta. However, despite a number of studies in the radio (Becker & Kundu 1976; Wilson & Weiler 1976; Becker & Szynkowski 1981; Morsi & Reich 1987; Fürst et al. 1988; Kassim 1992; Bock, Wright & Dickel 2001; Bietenholz & Bartel 2008), no radio emission from the supernova shock front has been seen. In particular, the 1-GHz surface brightness, Σ1 GHz, of any such emission has been limited (1σ) to being < 4 × 10−21 W m−2 Hz−1 sr−1 (Slane et al. 2000). Although this limit represents much brighter emission than the faintest known supernova shell in our Galaxy, G156.2+5.7, which has Σ1 GHz = 5.8 × 10−21 W m−2 Hz−1 sr−1 (Reich, Fürst & Arnal 1992), G21.5−0.9 is much younger1 and therefore might be expected to have brighter radio emission assuming a similar interstellar medium (ISM) density and supernova explosion energy.

G21.5−0.9’s centrally condensed PWN is also seen clearly in X-rays (Slane et al. 2000; Safi-Harb et al. 2001; Warwick et al. 2001; Matheson & Safi-Harb 2005; Bocchino et al. 2005; Matheson

1 For G156.2+5.7, Yamauchi et al. (1999) give an age of 15 000 yr and a distance of 1.3 kpc, but we note that both these values are uncertain by a factor of ∼2.

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& Safi-Harb 2010). In contrast to the radio, however, a fainter ‘halo’ of X-ray emission, with a radius of ~15 arcsec, is indeed seen surrounding the PWN. Both Matheson & Safi-Harb (2005) and Bocchino et al. (2005) argue that most of this halo X-ray emission is not from the outer shock, but is rather due to dust scattering. However, a relatively weak, limb-brightened X-ray component is also seen on the eastern side, which has been interpreted as non-thermal emission associated with the supernova shock (Bocchino et al. 2005; Matheson & Safi-Harb 2010).

With the goal of identifying any radio emission associated with this non-thermal X-ray emission from the forward shock, we obtained sensitive new observations of G21.5−0.9 and its surroundings.

2 OBSERVATIONS AND DATA REDUCTION

We observed G21.5−0.9 in the 1.4-GHz band on 2008 March 17, using the C array configuration of the National Radio Astronomy Observatory2 (NRAO) Very Large Array (VLA), with a total time of 6h. In this array configuration, the VLA is sensitive to structures up to 15 arcmin in size, so the structure of the putative radio-shell around G21.5−0.9 should be well sampled. In order to maximize the field of view, u−v coverage and dynamic range, we observed in spectral line mode using spaced centre frequencies of 1.4649 and 1.3851 GHz in the two intermediate frequency (IF) channels. Our total bandwidth per IF was 12.5 MHz, which was split into 16 channels. We phase-referenced our observations to the compact source PMN J1832−1035, whose position is accurate to better than 1 arcsec, therefore our astrometric uncertainty is dominated by contributions from noise and errors in phase-referencing. We estimate our astrometric uncertainty at <4 arcsec. Our flux density scale was set from observations of 3C 48 and 3C 286. The data reduction was carried out using standard procedures from NRAO’s AIPS software package.

Our final images were made from self-calibrated visibility data, using CLEAN deconvolution with multiple non-coplanar facets. We used a convolving beam with full width at half-maximum (FWHM) of 18.8 arcsec × 13.8 arcsec at position angle (p.a.) −12°.

Since our two IF frequencies differ by ~6 per cent, sources with different spectral indices could show noticeable differences in relative brightness between the two IFs. In particular, in Bietenholz & Bartel (2008) we found that the spectral index, α (where the flux density S at frequency ν is S ∝ να), of the G21.5−0.9 PWN is quite uniform over the nebula, with a value of +0.08±0.04. In contrast to a PWN, a supernova shell would be expected to have a notably steeper spectrum, with a typical value of −0.8 < α < −0.4 (Green 2009).

In order that such spectral index differences not limit the dynamic range in the deconvolved image, we chose to image and deconvolve our two IFs separately. We then averaged the resulting two images to obtain our final, combined image. The final image should correct for imperfectly removed side lobes from bright, nearby sources. The bottom part of Fig. 1 shows the Chandra X-ray image for the same field.

In fact, there are a number of other sources visible in the image in addition to G21.5−0.9. The brightest is QSO J1832−105, with a 1.43-GHz flux density of 1.07 Jy. Two other resolved sources are visible at approximately RA = 18h33m2s, Dec. = −10°27′0″ and RA = 18h32m4s, Dec. = −10°28′3″. We call these sources G21.64−0.84 and G21.45−0.59, as they are likely both Galactic, and we will discuss them below. There are also a number of weaker unresolved sources visible, which are likely extragalactic and which we do not discuss further.

Also present in the full image and included in the deconvolution and self-calibration was the SNR Kes 69, which is to the north-west of G21.5−0.9. We choose to exclude Kes 69 from the portion of the image displayed in Fig. 1, as it is beyond the 25 per cent point of the primary beam, and the image details are not reliable (see Kassim 1992, for a radio image of Kes 69). Some artefacts are visible in the western and north-western parts of the image, due to J1832−105 and Kes 69.

3 RESULTS: 1.4-GHZ WIDE-FIELD IMAGE

We show the wide-field radio-image of the G21.5−0.9 region in the top part of Fig. 1. This image represents only part of the imaged area, chosen to show the sources of interest. We further chose the range of grey-scale in order to show the weaker sources, with the result that the stronger ones such as G21.5−0.9 itself are saturated. Clearly visible in this image is the feature called the ‘northern knot’, ~2 arcmin to the north of the centre of G21.5−0.9. This image is corrected for the response of the primary beam (which has an FWHM of 31 arcmin at 1.43 GHz). As a consequence, the rms background level increases with distance from the pointing centre. Near G21.5−0.9, the rms background brightness was ~220 μJy beam−1.

This is the deepest radio image so far obtained of G21.5−0.9 and its surroundings. Our image has a peak/rms dynamic range of ~4700, and we note that this image is not limited by thermal noise, but rather by dynamic range with the chief sources of the background likely being continuum emission from the galactic plane as well as imperfectly removed side lobes from bright, nearby sources. The bottom part of Fig. 1 shows the Chandra X-ray image for the same field.

3.1 G21.5−0.9

In Fig. 2 we show a detail of the radio image showing the G21.5−0.9 PWN. The image corresponds well, albeit at lower resolution, to the one of Bietenholz & Bartel (2008). G21.5−0.9 had a total 1.43-GHz flux density of 7.0 ± 0.4 Jy, with a peak surface brightness at our resolution of 0.62 ± 0.03 Jy beam−1, corresponding to a brightness temperature of 1500 ± 75 K (where the uncertainties are dominated by the assumed 5 per cent uncertainty in the flux-density calibration).

On our 327-MHz image (image not reproduced here; see Brogan et al. 2005), G21.5−0.9 is also clearly visible, although only marginally resolved. Comparison of the flux density of 7.3 ± 0.7 Jy determined from the 327-MHz image with that at 1.4 GHz yields
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Figure 1. Top: a wide-field 1.4-GHz radio image of the region around G21.5−0.9. The grey-scale range of −2–10 mJy beam$^{-1}$ was chosen to emphasize any weaker background emission, therefore saturating the G21.5−0.9 PWN itself, which had a peak brightness of 621 mJy beam$^{-1}$. The sources we discuss in the text are labelled. The image has been corrected for the VLA primary beam response, with the result that the rms is ∼220 µJy beam$^{-1}$ near G21.5−0.9, which was the pointing centre, and increases with increasing distance away from it. The FWHM of the convolving beam was 18.1 arcsec × 13.8 arcsec at p.a. −12°. Low-level artefacts are visible in the vicinity of the bright source, QSO J1832−105. The diagonal line segment shows the location and orientation of the slice through G21.64−0.84 shown in Fig. 4. Bottom: an X-ray image of G21.5−0.9, showing the same field of view, and convolved to the same resolution, as the radio image above, made by combining a total of ∼520 ks of Chandra observations in the energy range 0.2–10 keV (for details, see Matheson & Safi-Harb 2010). The grey-scale is chosen so that the G21.5−0.9 PWN in the centre is saturated in order to show the fainter X-ray emission surrounding it. Different regions of the image have been observed with different effective exposure times, resulting in a varying background level. The bright point source in the south-western part of the X-ray halo is an unrelated emission-line star, SS 397. 

an integrated spectral index between these frequencies, $\alpha_{1.4\text{GHz}}^{0.3\text{GHz}}$ of 0.0 ± 0.1, consistent with other determinations of G21.5−0.9’s radio spectral index (e.g. Bietenholz & Bartel 2008).

There is a relatively compact radio source, approximately 1 arcmin to the north of the main body of G21.5−0.9, which corresponds to the X-ray feature called the ‘northern knot’$^3$ (e.g. Matheson & Safi-Harb 2010). B. Gaensler (private communication) reported seeing the northern knot in earlier 1.4-GHz radio observations. The northern knot has a total 1.43-GHz flux density of 20.2 ± 1.8 mJy, and is marginally resolved in our image, with an intrinsic FWHM size, as estimated by an elliptical Gaussian fit, of 18 arcsec × 8 arcsec at p.a. 105°. The peak brightness position in the radio is consistent with that seen in the X-ray when the latter is convolved to the same resolution, as can be seen in the top and bottom panels of Fig. 1.

$^3$ This feature was also called the ‘northern spur’ by Bocchino et al. (2005)
we estimate a total 5-GHz flux density of 1.4 Jy beam$^{-1}$, which we discuss below. We derive a new upper limit to the radio emission from the SNR shell in Section 4.1.

### 3.2 G21.64$-$0.84

A so far uncatalogued source, G21.64$-$0.84, is distinctly visible in the 1.4-GHz image in Fig. 1. It is a large elongated structure, which extends from near G21.5$-$0.9 to the north of north-west. It is brightest in the middle, reaching a peak 1.43-GHz brightness of 6.8$\pm$0.5 mJy beam$^{-1}$ (corresponding to a brightness temperature of 17$\pm$1 K). It has a total length of $\sim$10 arcmin. It seems to consist of two relatively distinct and roughly parallel curved ridges of emission, with the western or outer one being better defined, and the eastern or inner one being more diffuse and $\sim$1.5 arcmin distant. The total 1.43-GHz flux density in the G21.64$-$0.84 is $660\pm50$ mJy, with each of the two ridges having approximately half the total.

G21.64$-$0.84 is also visible in the 327-MHz image, and we show a detail in Fig. 3. At this frequency, due to the larger primary beam, much more of the source is visible than at 1.4 GHz, and it can be seen to be a relatively circular shell structure. The centre of the shell is at RA = 18$^h$33$^m$6$^s$ and Dec. $-10^\circ$25$'$4, or at $l =$ 21.64, $b = -0.84$. Our name for this source, G21.64$-$0.84, is based on the central position of the shell as seen at 327 MHz. The outer angular diameter of the shell is $\sim$13 arcmin. The total flux density at 327 MHz is 2.8 Jy, with an estimated uncertainty of $\sim$0.5 Jy due to the somewhat uncertain zero-level in the images. The 327-MHz flux density of the part visible in the 1.4-GHz image is 1.4$\pm0.2$ mJy, and over this region the integrated value of $\alpha_{\nu=1.4$GHz} is $-0.5\pm0.1$. A somewhat steeper spectrum is suggested for the northern and eastern sides of the shell, which are not visible at 1.4 GHz, however due to the uncertain zero-levels and low signal-to-noise ratios, a constant value of $\alpha_{\nu=1.4$GHz} $\sim$ $-0.6$ for the whole shell is probably not excluded. The average over the whole of the 327-MHz surface brightness is $2.5 \times 10^{-21}$ W m$^{-2}$ Hz$^{-1}$ sr$^{-1}$, and if we take $\alpha = -0.5$, then $\Sigma_{\nu=327$GHz$} = 1.4 \times 10^{-21}$ W m$^{-2}$ Hz$^{-1}$ sr$^{-1}$.

We include the G21.64$-$0.84 region in the wide-field X-ray image shown in the lower panel of Fig. 1 above. Although this region was not the primary target, and the instrumental background differs in different parts of G21.64$-$0.84, no sign of X-ray emission which might be associated with G21.64$-$0.84 is seen down to limits of $10^{-3}$ times the peak brightness of G21.5$-$0.9. At the radio peak-brightness position of G21.64$-$0.84, we estimate that the X-ray exposure was $\sim$130 ks.

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Figure 2. A 1.4-GHz image of G21.5$-$0.9. The figure represents a detail of the top panel of Fig. 1. The contours are drawn at $-1, 1, 2, 4, 8, 16, 32, 100, 300, 500$ and 600 mJy beam$^{-1}$. The grey-scale is chosen to emphasize the fainter emission, and is labelled in mJy beam$^{-1}$. The convolving beam FWHM, indicated at lower left, was 18.8 arcsec$\times$13.8 arcsec at p.a. $-12^\circ$. The peak brightness in this subimage was 621 mJy beam$^{-1}$, and the rms background noise was 260 $\mu$Jy beam$^{-1}$. The ‘northern knot’ is labelled. Also visible at the top of the image is the lower portion of G21.64$-$0.84.

The northern knot is not discernible on our lower resolution 327-MHz image, being blended with G21.5$-$0.9 itself. The knot is marginally visible in an image made from the 5-GHz data of Bietenholz & Bartel (2008). We estimate a total 5-GHz flux density for the northern knot of 19$\pm7$ mJy, resulting a nominal value for the knot spectral index, $\alpha_{\nu=5$GHz}, of $-0.04$, similar to that body of G21.5$-$0.9. However, the uncertainties on the spectral index are large, and the $p = 2.3$ per cent (2$\sigma$) limits on $\alpha_{\nu=5$GHz} are $-1.3$ and $+0.5$.

What is notably absent from our deep 1.4-GHz image is radio emission corresponding to the limb-brightened X-ray emission visible in the bottom panel of Fig. 1. Although some diffuse radio emission appears north of the northern knot, we believe that it is not the counterpart of the X-ray shell of G21.5$-$0.9, but more likely associated with G21.64$-$0.84, which we discuss below. We derive a new upper limit to the radio emission from the SNR shell in Section 4.1.

Figure 3. A 327-MHz image of G21.64$-$0.84. The FWHM resolution was 85 arcsec, and is indicated at lower left. The grey-scale is labelled in mJy beam$^{-1}$, and the rms background was $\sim$14 mJy beam$^{-1}$. The contours are drawn at $-0.6, 0.6, 1, 1.5, 3.0, 5, 10, 15, 20$ and 30 per cent of the peak brightness which was 5.73 Jy beam$^{-1}$. G21.5$-$0.9 is partly visible at the bottom of the image.
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3.3 G21.45–0.59

A further weak resolved source is visible in both our 1.4-GHz (Fig. 1) and 327-MHz images near RA 18°33′20″, Dec. = −10°28′ (l = 21.459, b = −0.59), which we call G21.45–0.59. It is approximately 1.5 arcmin in diameter. Its 327-MHz peak brightness was 209 ± 24 mJy beam⁻¹ (at 85-arcsec resolution), corresponding to a brightness temperature of 330 ± 38 K.

We estimate total flux densities for G21.45–0.59 of ~0.3 Jy at 1.4 GHz and ~0.5 Jy at 327 MHz, corresponding to α_{1.4\text{GHz}} ~ −0.3, although this spectral index estimate should be treated with caution as the total flux densities are rather uncertain because of the uncertain extent of the source and zero-levels, as well as the large primary-beam correction factor of ~2.6 at 1.4 GHz.

G21.45–0.59 has likely been identified already in the 2.7-GHz continuum survey of the Galactic plane by Reich et al. (1984), who list the source RFS 323 at a position about 90 arcsec away from our peak brightness position for G21.45–0.59, and having a total 2.7-GHz flux density of 0.50 ± 0.15 Jy. The position offset between G21.45–0.59 and RFS 232 is larger than either our own astrometric uncertainty of <4 arcsec or that of 20 arcsec listed by Reich et al. (1984). However, the FWHM resolution of the Reich et al. survey was 4.3 arcmin, so the positional offset is only approximately one-third the Reich et al. beamwidth, and thus probably not significant.

We consider that RFS 232 can thus be identified with G21.45–0.59, with the 2.7-GHz flux density of Reich et al. implying α_{2.7\text{GHz}} ~ 0.

We note that G21.45–0.59 is also visible in the 1.4-GHz VLA Galactic Plane Survey (VGPS; Stil et al. 2006), and has a peak-brightness position consistent to within 2 arcsec with the one we measured at that frequency. We consider our peak-brightness position for G21.45–0.59 more reliable than that listed for RFS 232 by Reich et al. (1984).

Our X-ray observations do not extend to G21.45–0.59, so its X-ray brightness is unknown. We will discuss the nature of G21.45–0.59 in Section 4.3 below.

4 DISCUSSION

4.1 G21.5–0.9 and limits on radio emission from its forward shock

Our 1.4-GHz radio image of the G21.5–0.9 region (Fig. 1, top) is dominated by the pulsar wind nebula G21.5–0.9. Our observations are sensitive to structures much larger than the G21.5–0.9 PWN, so there is no reason to suspect any significant deficit in the recovered flux density due to missing short interferometer spacings. Indeed, our total recovered flux density of 7.0 ± 0.4 Jy is consistent within the uncertainties with the value measured by Altenhoff et al. (1970) and the radio spectrum compiled by Salter et al. (1989).

Except for the northern knot, no radio emission is visible which can be associated with the X-ray halo or the limb-brightened feature
seen in X-ray. Conservatively scaling the rms background brightness of our image (260 \mu Jy beam$^{-1}$ at 1.43 GHz) to the standard frequency of 1 GHz using a steep assumed spectral index,\(^5\) we obtain a 3\(\sigma\) upper limit on \(\Sigma_{1\,\text{GHz}}\) of 1.6 \times 10^{-21} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}.

Since the X-ray limb detected at a radius of \(\sim 150\) arcsec likely indicates the location of the forward shock (see Bocchino et al. 2005; Matheson & Safi-Harb 2010), we can place more stringent limits on the radio brightness of the shell by integrating over the shell region. Over an annular region with an outer angular radius of 150 arcsec and a thickness of 20 per cent of the outer radius, the observed total 1.43-GHz flux density is 12 \pm 6 mJy, with a \(\sigma\) upper limit of 30 mJy, corresponding to an average 1.43-GHz spectral luminosity of \(\sim 8 \times 10^{20}\) erg s$^{-1}$ Hz$^{-1}$/pc (or a surface brightness of \(\sim 1.2\) \mu Jy arcsec$^{-2}$). Again conservatively scaling to 1 GHz with \(\alpha = -0.8\) results in a 3\(\sigma\) limit on the average surface of \(\Sigma_{1\,\text{GHz}} < 7 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}$. Our assumption for the shell geometry is conservative: for shells thicker than 20 per cent, as might be expected for an age of 870 yr (see e.g. Jun & Norman 1996; Chevalier 1982), the surface-brightness limit would be lower. In addition, as noted above, for values of \(\sigma\) flatter than the assumed \(-0.8\), the limit would also be slightly lower, with \(\alpha = -0.5\) resulting in a value of \(6 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\) for the limit. Finally, the annular region above includes real emission due to G21.64–0.84, which is probably not associated with G21.5–0.9. If we exclude this contribution, the limit on the average surface brightness decreases by approximately 20 per cent.

The limit on the radio surface brightness of G21.5–0.9’s shell, which corresponds to \(< 6 \times 10^{-17}\) times the peak surface brightness of the PWN, is \(\sim 17\) times lower than those previously obtained for G21.5–0.9 (Slane et al. 2000).

It is expected that the shocks formed as the shell of supernova ejecta plough through the ISM would both accelerate particles and amplify the ambient magnetic field by compression and through instabilities. Radio emission from this region might therefore be expected, especially for a remnant as young as G21.5–0.9. Where then is this radio emission?

We note first that G21.5–0.9 is not unique in having no detectable radio emission from the supernova shell. In fact, most other young PWNe seem to show little radio emission from the putative shell, with the best studied example being the Crab nebula, which is one of the youngest known and also one of the very few identified with a supernova (SN 1054), and which does not have any radio emission from the ejecta shell down to a 3\(\sigma\) upper limit of \(\Sigma_{1\,\text{GHz}} = 7.5 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\) (Falait et al. 1995). 3C 58, also a young PWN, also has no detectable radio emission from the shell to a 3\(\sigma\) surface brightness limit of \(\lesssim 5 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\) (Reynolds & Aller 1985; Bietenholz, Kassim & Weiler 2001). In other words, the present limits on the radio surface brightness of G21.5–0.9 shell, although low, are not unusual when compared to those for other bright PWNe. What is unusual about G21.5–0.9, however, is that unlike either the Crab or 3C 58, X-ray emission from which can reasonably be attributed to the forward shock has been detected (Bocchino et al. 2005; Matheson & Safi-Harb 2010). Matheson & Safi-Harb (2010) fit the X-ray spectrum of the eastern limb after subtracting the halo emission, in other words the non-thermal part of the X-ray emission thought to be due to the forward shock, with broad-band models consisting of a power law with an exponential high-energy cut-off (model srcut, Reynolds 1998).

Using an assumed radio spectral index of \(\alpha = -0.5\), their best-fitting model would imply \(\Sigma_{1\,\text{GHz}} = 2.3 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\), which is well below our measured 3\(\sigma\) limit of \(7 \times 10^{-22}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\), along with a cut-off frequency between \(2.4 \times 10^{12}\) and \(1.4 \times 10^{13}\) Hz (90 per cent confidence limits). The absence of radio emission from G21.5–0.9’s forward shock is therefore consistent with the observed non-thermal X-ray emission.

Although we detect no radio emission from the shell, we do clearly detect G21.5–0.9’s northern knot in our deep 1.4-GHz image. A marginal detection at 4.8 GHz results in a nominal spectral index, \(\alpha_{4\,\text{GHz}}^{1\,\text{GHz}}\), of \(\sim 0\), albeit with large uncertainties. This nominal value of \(\alpha_{4\,\text{GHz}}^{1\,\text{GHz}}\) is similar to that for the body of G21.5–0.9, suggesting that the knot, like the body of G21.5–0.9, consists of electrons energized by the pulsar. However, the alternate hypothesis of the knot consisting of electrons accelerated in the forward shock and having \(\alpha_{4\,\text{GHz}}^{1\,\text{GHz}} \sim -0.5\) is not excluded by the data, so no firm conclusions as to its nature can be drawn.

4.2 G21.64–0.84: a new shell supernova remnant

We have identified a new shell-like radio source in our radio images, which we have called G21.64–0.84. In the high-resolution 1.4-GHz image (Fig. 1 top), only the western part of the shell is visible, but most of the shell can be seen in the 327-MHz image (Fig. 3). Its radio spectral index of \(\sim -0.6\) (Section 3.2) is consistent with those seen for shell-type SNRs (see e.g. Green 2009). We examined the 8-\mu m infrared images from the Spitzer Glimpse survey (Benjamin et al. 2003), and find no infrared emission for G21.64–0.84, which implies that G21.64–0.84 is unlikely to be either an H II region or a wind blown bubble, which latter often have a shell-like structure but are almost inevitably accompanied by infrared emission (e.g. Brogan et al. 2006). It seems most probable that G21.64–0.84 is an as yet uncatalogued SNR.

We noted in Section 3.2 above that no X-ray emission is seen from G21.64–0.84 to levels of \(\sim 0.1\) per cent of the peak brightness of G21.5–0.9. The lack of X-ray detection, however, does not argue against the SNR hypothesis: Green (2009) has a comprehensive list of Galactic SNRs and finds that only \(\sim 40\) per cent of them are detected in X-ray, with high absorption in the X-ray being seen for many.

Could G21.64–0.84 represent the radio emission associated with the forward shock in G21.5–0.9, the search for which motivated our observations? We think this possibility very unlikely, as the centre off the new shell is clearly displaced from the G21.5–0.9 PWN. If PSR J1833–1034 had been at the centre of the newly identified radio shell 870 yr ago, then its average speed since then must have \(\sim 15\,000\) km s$^{-1}$, which is far higher than the speeds seen for pulsars. Moreover, X-ray emission from G21.5–0.9’s forward shock has in fact been identified, and is not coincident with G21.64–0.84. We therefore identify G21.64–0.84 as a previously unidentified shell-type SNR, which is unrelated to G21.5–0.9.

\(^5\) To determine the limit, we use \(\alpha = -0.8\) as the steepest reasonable spectrum for a shell. As the difference between the observed frequency of 1.43 GHz and the nominal one is not large, our result is not sensitive to reasonable changes in \(\alpha\), for example, using a more usual value of \(\alpha = -0.5\) would lower our 3\(\sigma\) surface brightness limit by \(\sim 8\) per cent to \(1.4 \times 10^{-21}\) W m$^{-2}$ Hz$^{-1}$ sr$^{-1}\).

\(^6\) We note that a shell of thermal X-ray emission was seen in 3C 58 by Gotthelf, Helfand & Newburgh (2007). The diameter of \(<5.6\) pc of this shell is smaller than the maximum extent of the PWN, which is \(\sim 8.5\) pc. The thermal X-ray emission is therefore likely associated with supernova ejecta swept up by the expanding PWN rather than the original forward shock from the supernova.
SNR shells typically have steeper brightness gradients at their outside edges than the inside ones, thus naturally explaining the asymmetry in the profile (Fig. 4). Although the partial double-shell morphology is not common for SNRs, other remnants with similar structure have been observed (e.g. Gaensler 1998; Giacani et al. 2009).

We found that G21.64–0.84 has an average surface brightness of \( \Sigma_{1\text{GHz}} \approx 1.4 \times 10^{-21} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1} \). This SNR is therefore near the peak of the observed distribution of \( \Sigma_{1\text{GHz}} \) values in the catalogue of Green (2009), but below his estimated completeness limit of \( \approx 1 \times 10^{-20} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1} \). We note that the catalogued number of SNRs in the Galaxy (\( n = 274 \)) in the catalogue of Green (2009) is lower than the \( \approx 1000 \) generally expected from supernova rates (e.g. Tammann, Loefler & Schroeder 1994, see also discussion in Brogan et al. 2006), suggesting that there likely are many more SNRs to be discovered at these sensitivity levels.

A relationship has been observed between the surface brightness and the diameter (\( D \)) for SNRs. Although this \( \Sigma-D \) relation has in the past often been used to determine SNR distances it has been shown to be of limited value for this purpose, (see, e.g. Green 2004, 2005; Bandiera & Petruk 2010). If we take \( \Sigma_{1\text{GHz}} = 1.4 \times 10^{-21} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1} \) for G21.64–0.84 and compare it to the sample of 47 SNRs of known distance shown in Green (2004), we can conclude only that the G21.64–0.84’s diameter is likely between 10 and 100 pc, and its distance therefore in the not very restrictive range of 3 \( \sim \) 30 kpc. The lack of apparent X-ray emission suggests high absorption and therefore perhaps argues against the shorter end of this range.

4.3 G21.45–0.59: a probable H ii region

Our wide-field 1.4-GHz image also shows a relatively faint extended radio source which we have called G21.45–0.59. Unlike G21.64–0.84, it does not have a clear shell-like morphology. Although the current data do not reliably determine its radio spectral index, a relatively flat spectrum, with \( \alpha \) in the range of \( \approx 0.3-0 \) is suggested (Section 3.3). The source is present on the Glimpse 8-\( \mu \)m infrared images, and listed as G021.4571–00.8594 in the GLIMPSE II source list.\(^7\) We therefore tentatively identify G21.45–0.59 as an H ii region.

5 SUMMARY AND CONCLUSIONS

(i) We present a new deep 1.4-GHz radio image of the PWN G21.5–0.9 and its environs. We also show a deep X-ray image, made from 520 ks of \( \textit{Chandra} \) data, of the same region.

(ii) Although the G21.5–0.9 PWN is clearly visible in our 1.4-GHz image, we see no sign of shell radio emission from the supernova forward shock. We place a 3\( \sigma \) upper limit of 7 \( \times 10^{-22} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1} \) on the 1-GHz surface brightness of any such emission, in particular also on any radio emission corresponding to the limb-brightened, non-thermal X-ray shell component. Although low, these limits on the radio emission are none the less compatible with a broad-band model of the X-ray emission.

(iii) The feature called the northern knot of G21.5–0.9 is clearly seen at 1.4 GHz. Its spectral index was \( \alpha_{1\text{GHz}} = -0.04 \pm 0.31 \), similar to that of the remainder of G21.5–0.9, (i.e. \( \alpha \approx 0 \)), although a steeper value as is typical of shells is not excluded by the large uncertainties.

\(^7\) Available at http://irsa.ipac.caltech.edu/data/SPITZER/GLIMPSE

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