Enabling Scalability by Partitioning Virtual Environments Using Frontier Sets

Abstract

We present a class of partitioning scheme that we have called frontier sets. Frontier sets build on the notion of a potentially visible set (PVS). In a PVS, a world is subdivided into cells and for each cell all the other cells that can be seen are computed. In contrast, a frontier set considers pairs of cells, A and B. For each pair, it lists two sets of cells (two frontiers), \( F_{AB} \) and \( F_{BA} \). By definition, from no cell in \( F_{AB} \) is any cell in \( F_{BA} \) visible and vice versa.

Our initial use of frontier sets has been to enable scalability in distributed networking. This is possible because, for example, if at time \( t_0 \) Player1 is in cell A and Player2 is in cell B, as long as they stay in their respective frontiers, they do not need to send update information to each other.

In this paper we describe two strategies for building frontier sets. Both strategies are dynamic and compute frontiers only as necessary at runtime. The first is distance-based frontiers. This strategy requires precomputation of an enhanced potentially visible set. The second is greedy frontiers. This strategy is more expensive to compute at runtime, however it leads to larger and thus more efficient frontiers.

Network simulations using code based on the Quake II engine show that frontiers have significant promise and may allow a new class of scalable peer-to-peer game infrastructures to emerge.

1 Introduction

Multi-user online simulations and games pose a number of challenges to system designers (Singhal & Zyda, 1999). One challenge is that of scaling the system to large numbers of users. Two problems are key: the simulation or game mechanics may require computation of \( O(N^2) \) in the number of participants; and maintaining the game state potentially involves the exchange of \( O(N^2) \) messages across a network. Simulations of more than a few tens of participants have usually required dedicated networks and assumptions about resource availability and interaction capabilities of the simulation client. Alternatively they have had to limit the interactivity of the simulation or use a nonreal time simulation.

Networked virtual environments (NVEs) often implement an area of interest management scheme that tries to identify participants that do not need to...
communicate (Morse, Bic, & Dillencourt, 2000). A common strategy is to allocate each participant to one of a set of predetermined regions of space and then only enable communication between participants who share the same region.

In Steed and Angus (2004, 2005) we introduced the concept of a frontier set. Frontier sets exploit a potentially visible set (PVS) to produce a new data structure that allows pairs of entities to negotiate a criterion, a frontier, that can test independently to ensure that no interaction is necessary between the pairs of entities. This criterion will typically be valid for several seconds.

Figure 1 gives an example using two players, A and B, in an online game. Two frontiers have been created and both A’s and B’s clients know about the existence of these frontiers. Because no cell in A’s frontier is visible to any cell in B’s frontier, as long as A stays in his frontier and B stays in her frontier, they never have to send any information. As soon as A or B leave their frontiers, they either have to renegotiate frontiers, or they can potentially see each other and thus have to send information to each other continuously.

The frontier concept is very general, and in Steed and Angus (2004) we showed how to build a particular type of frontier using a region growing approach. We pre-computed a complete set of frontiers which required $O(N^3)$ storage space in the number of cells in the world. To be usable with a reasonable sized world this required compression of the original PVS.

However, many different types of frontiers exist, and in this paper we present two alternatives, distance-based frontiers and greedy frontiers, that delay computation of frontiers until required at runtime. Distance-based frontiers require precomputation of an intermediary data structure called an enhanced potentially visible set (EPVS) which only requires $O(N^2)$ space.

In Section 2 we describe related work. In Section 3 we give a brief introduction to the frontier sets data structure and give examples of how frontiers could be used. In Section 4 we describe distance-based frontiers. In Section 5 we describe greedy frontiers. In Section 6 we then describe how we can apply frontiers to NVEs and we detail how we used the game Quake II (IdSoftware, 1997) as an example. We analyze how frontier sets perform in Quake II in Section 7. We then discuss further applications of frontiers and potential avenues for further research in Section 8.

2 Related Work

Today’s networked games have built upon techniques and technologies developed for military simulators (Singhal & Zyda, 1999; Smed, Kaukoranta, & Hakonen, 2001). SIMNET was an early military simulator that was designed for training small teams (Miller & Thorpe, 1995). Each SIMNET client simply broadcasts information about its state on the network. SIMNET’s underlying network technology was developed and standardized with the Distributed Interactive Simulation standard (IEEE, 1993). The core of DIS is the Protocol Data Unit (PDU), which describes the state of a simulator entity (e.g., plane, tank, or dismounted infantry).

DIS-based systems are a good example of a peer-to-peer system where every client communicates with all other clients. Such systems require a lot of bandwidth to cope with the volume of messages. There is also a general problem in ensuring consistency. Because every client independently evolves the simulation state based on information received, it is not guaranteed that any pair of clients will have the same state. This is especially true...
if attempting to deploy such a system over the internet where packets may be lost or suffer jitter in delivery time. Finally, safeguards have to be put in place so clients can’t cheat. A modern game that uses a peer-to-peer approach is Age of Empires (Bettner & Terrano, 2001).

The main alternative to peer-to-peer systems is the client-server system. In this type of system all clients connect to a server, and that server is responsible for computing the state of the game and distributing it to all the clients. This is the most common networking model for games. Consistency is no longer an issue since there is one canonical copy of the game state on the server. However a server introduces extra latency as any update to the game state needs to be relayed via the servers. The issue of latency is very important for real-time games, especially the first-person shooter games that have become very popular in recent years (Henderson, 2001).

### 2.1 Partitioning

In order to have environments that scale to large numbers of users, one common approach is to partition the world and only relay a subset of all events and states to each client (Morse et al., 2000).

One of the first systems to employ a partitioning scheme was the NPSNET system (Macedonia, Zyda, Pratt, Barham, & Zeswitz, 1994). NPSNET divides the virtual world into fixed sized hexagonal cells. Participants send information (e.g. location updates) to their current local cell but can choose to receive information from potentially many cells that fall within their area of interest. The use of fixed-size cells is appropriate for applications such as outdoor battle simulations where entities move with predictable speeds and trajectories and where entities are spread reasonably evenly across the entire space.

In contrast to the regular partitioning scheme of NPSNET, the Spline system (Sterns & Yerazunis, 1997) divides the virtual world into arbitrary-shaped locales that are stitched together using portals. Each locale defines its own coordinate system and participants receive information from their current locale and its immediate neighbors. The ability to use variable-sized locales provides additional flexibility in coping with less predictable entities and is more appropriate for indoor environments.

### 2.2 Visibility Partitioning

Partitioning schemes exploit application knowledge about the probable spatial proximity of participants who are likely to want to interact. NPSNET and Spline used a predefined or handcrafted partition of the space. If the virtual environment itself can be analyzed to determine interregion visibility then we can use that information to support network scalability.

A related computer graphics technique is visibility culling (Cohen-Or, Chrysanthou, Silva, & Durant, 2003). One technique that is often used in games is potentially visible sets (PVS) (Airey, Rohif, & Brooks, 1990; Teller & Sequin, 1991). A PVS can be used to exclude a pair of entities from consideration for simulation purposes because they are not mutually visible. However this visibility must be evaluated every time the entities concerned move.

The RING system exploits a PVS data structure to enable scalability of a client-server virtual environment (Funkhouser, 1995, 1996). In the RING system, a server culls messages if it knows that a client can’t possibly see the effect of the message.

Closest in spirit to our frontiers approach is that of update-free regions (UFRs) (Makbili, Gotsman, & Bar-Yehuda, 1999; Goldin & Gotsman, 2004). A UFR is a region of the 2D plane in which one of a pair of users can move without its counterpart being visible as long as they remain within their own UFR. One type of UFR, the visibility-based UFR, is described by a straight wall that occludes direct visibility between users. For such a wall, two lines can be drawn from the endpoints of the wall, partitioning the plane into four regions. If the two users remain in the regions of this partition in which they start, they cannot see each other. Another type of UFR is distance-based, and it is defined simply by a maximum visibility distance to any other user. Frontier sets can be considered to be a type of UFR but they are defined for cells of a map rather than for the
specific users. Compared to the geometric or distance-based UFR approaches, frontiers provide much larger regions where the visibility of two users does not need to be computed because they exploit known occlusion relations in the space, and there is a simpler mechanism for establishment and testing of the frontier. Therefore there is no need to limit the visibility distance and frontiers exploit precomputed visibility data structures that exist in many systems.

3 Frontiers

3.1 Potentially Visible Sets

A potentially visible set (PVS) exploits the fact that from any point of view in a dense architectural environment much, if not most, of the rest of the environment will be occluded (Airey et al., 1990; Teller & Sequin, 1991). For an example of a PVS, see Figure 2. If the environment is divided into regions of space (or cells) then for any cell, it will be possible to identify openings (or portals) through which other cells can be seen. For any cell, it is possible to explicitly compute which other cells are visible from that cell, because if a cell is visible then there must be a line of sight through all the portals between them.

The calculation of a PVS can be done either automatically (Airey et al., 1990; Teller & Sequin, 1991) or by hand for smaller models. For the purposes of this paper we assume that a PVS already exists.

In introducing frontiers, we will first assume that the PVS is symmetric; that is, if cell A can see cell B, cell B can see cell A. In a more general system portals may be unidirectional in which case the PVS will be asymmetric. Even if portals are bidirectional some asymmetries may arise because of the complexity of the visibility analysis. For example, the PVS in the game Quake II (see Section 6) is asymmetric and the asymmetries give a slightly conservative visibility estimate. Asymmetries can be dealt with by minor extensions to the algorithms we will describe.

3.2 Frontier Definition

A PVS will be based on a cell-based subdivision of the world. A frontier is defined relative to pairs of cells in that subdivision. Given two cells A and B, a frontier comprises two sets of cells $F_{AB}$ and $F_{BA}$ such that no cell in $F_{AB}$ is visible to a cell in $F_{BA}$ and vice versa. For cells A and B, $F_{AB} \cap F_{BA} = \emptyset$, otherwise any cell in the intersection must be visible from both $F_{AB}$ and $F_{BA}$. Figure 3a gives an example of a frontier. We will use the term frontier to refer to a pair of such sets, or to only one of the sets when the meaning is clear. The complete set of frontiers for a whole environment will be referred to as a frontier set.

There are potentially many frontiers for a pair of cells. No frontier will exist between two cells if the two cells are visible to each other. If B is not in the PVS of A, then frontiers can be initialized with $F_{AB} = A$, $F_{BA} = B$. In Figure 3 we see one possible pair of frontiers for two cells A and I. In this map no frontier would exist between cells D and H because they are mutually visible.

3.3 Example Usage

Consider two users moving around the environment depicted in Figure 3a. If Anne is in cell A, and Bob is in cell I at time $t_0$, then a frontier can be established, $F_{AI} = \{A,B,C,F\}$, $F_{IA} = \{G,H,I\}$ as shown in Figure 3a. If Anne remains in $F_{AI}$ and Bob remains in $F_{IA}$ then they can never see each other. If this were a networked virtual environment this would mean that if Anne and Bob both exchanged location information at $t_0$ they would not have to send any further updates.
If either Anne or Bob leaves his or her frontier, then one of two situations arises: either a new frontier can be set up between the two cells Anne and Bob are currently in, or the cells they are in are mutually visible. In Figure 3b, at time $t_1$, Anne leaves FAI established at $t_0$ and enters cell E. At this time Bob is in cell H. There is a new frontier $FEH_{1005} = \{A, B, C, E, F\}$, $FHE_{1005} = \{H, I\}$. At time $t_2$, Figure 3c, Anne moves to cell D. There is no frontier between cells D and H because the cells are mutually visible. At time $t_3$, Figure 3d, Bob moves to cell I. A frontier can be established $FDI_{1005} = \{A, B, C, D, E, F\}$ and $FID_{1005} = \{I\}$.

4 Distance-Based Frontier Creation

Section 3 introduced frontiers and suggested a way of using them for culling events between a pair of users. In this scenario, any viable frontiers are useful because otherwise the assumption is that the users can see each other. For example, a frontier consisting of just the two original cells themselves is a viable frontier if the two cells cannot see each other. However the example scenario also suggests that the best frontiers for a pair of cells are those that are expected to be viable the longest given a predicted or observed model of movement of users around the space. A good approximation to this can be achieved by trying to achieve frontiers where the two halves are roughly equal in size, and as large as possible.

Another issue that we have to address is at what point we should construct the frontiers. In the event culling example, the actual frontier doesn’t need to be calculated until it is known what cells the two users are in. We do have to guarantee that both clients will calculate the same frontier. However if we wish to create a good frontier this may take more time than we have available in a real-time simulation.

In this section we introduce a very simple method for creating frontiers at runtime. In Section 5 we will consider an alternate and more expensive method of frontier construction. Both algorithms defer frontier creation until the frame (in the simulation) when it is required. In order to describe the distance-based method we first introduce a novel data structure, the enhanced potentially visible set.
4.1 Enhanced Potentially Visible Set

The distance-based creation method makes use of a visibility distance metric. A PVS records all cells that are visible from the current cell. We interpret this to mean that the visibility distance from A to B (dist(A,B)) is 1 if B ∈ PVS_A and dist(A,A) = 0. If B $\not\in$ PVS_A, then dist(A,B) is the length of the shortest chain of cells comprising A, C_1, $\ldots$, C_n, B such that C_1 ∈ PVS_A, C_{i+1} ∈ PVS_{C_i} $\ldots$, B ∈ PVS_{C_n}. This can be calculated by taking the matrix that forms the original PVS, setting each element (A,B) to 1 if A ∈ PVS_B and setting it to $\infty$ otherwise, and then running any all-shortest paths algorithm. We call the final matrix an enhanced potentially visible set (EPVS), see Figure 5.

This EPVS data structure requires more space than a PVS, because the latter is a bit array and the EPVS stores an integer distance. Thus the EPVS requires $O(N^2 \log_2(\text{MaxDistance(EPVS)}))$ rather than $O(N^2)$. However, as we will see, the maximum distance in an EPVS is not high in the models we have been testing (the maximum being 8; see Section 7.1).

4.2 Distance-Based Frontiers

Once the EPVS is calculated, frontiers can be specified as follows. Considering two cells A, B:

\[ F_{AB} = \{C | \text{dist}(A,C) \leq \text{dist}(B,C) - 1\} \quad (1) \]

\[ F_{BA} = \{D | \text{dist}(B,D) < \text{dist}(A,D) - 1\} \quad (2) \]

$F_{AB}$ and $F_{BA}$ are mutually invisible. To show this, if it isn't true then there exist C ∈ $F_{AB}$ and D ∈ $F_{BA}$ such that dist(C, D) ≤ 1. This implies

\[
\begin{array}{|c|c|c|}
\hline
0 & 1 & 1 \\
2 & 1 & 2 \\
2 & 3 & 3 \\
\hline
\end{array}
\]

Figure 5 Example of part of an enhanced potentially visible set (EPVS). The figure shows the distances from cell A to the other cells from Figure 2. These distances would form one row of the EPVS.
dist(A,D) ≤ dist(A,C) + 1 \Rightarrow dist(A,D) - 1 ≤ dist(A,C) \tag{3}

and

dist(B,C) ≤ dist(B,D) + 1 \tag{4}

From Equations 3 and 1

dist(A,D) - 1 ≤ dist(A,C) ≤ dist(B,C) - 1 \tag{5}

from Equation 4

dist(B,C) - 1 ≤ dist(B,D) - 1 + 1 \tag{6}

and then combining Equations 5 and 6

dist(A,D) - 1 ≤ dist(B,D)

which contradicts Equation 2 and the fact that D is in \( F_{BA} \).

To create a pair of frontiers at runtime requires us to iterate through all cells. For each cell \( C \), we look up \( dist(A, C) \) and \( dist(B, C) \) and use Equations 1 and 2 to add \( C \) to \( F_{AB} \) or \( F_{BA} \), if applicable. This requires \( 2N-2 \) value lookups, and \( O(N) \) storage space per pair. If there are \( M \) clients, each of those clients might need to do this calculation for \( M-1 \) other clients every frame. However, the point of using frontiers is that the recalculation of frontiers is done relatively rarely. Also there are several other processes in the client, such as rendering, that potentially require a scan of every cell in the spatial partition, so these lookups do not come at a prohibitive cost. The pseudocode for this function is shown in Figure 6.

5 Greedy Frontier Creation

The frontiers calculated in the previous section consider only visibility distance to cells when partitioning. This means that in certain situations, where for example one cell is very highly connected, but the other is not, the frontiers might have quite different cell counts. A better approach might be a greedy algorithm that tries to balance the number of cells in each frontier.
Figure 7 gives pseudocode for a region-growing approach to the creation of frontiers. If the PVS is symmetric, to add a cell C to a frontier FAB, C must not be visible to any cell in FBA. Likewise, a cell C can only be added to FBA if it is not visible to any cell in FAB. Key to this is maintaining an aggregate PVS of a set of cells. As a cell is added to a frontier, the PVS of the frontier under construction is merged with the PVS of the cell being added. The algorithm proceeds by alternately adding a cell to FAB and FBA. A first approach chooses candidates to add by following the adjacency graph in a breadth-first manner across the cells and portal graph from A and B.

In Steed and Angus (2005) we precomputed the complete sets of frontiers, requiring $\sim O(N^3)$ time to compute and $O(N^3)$ space to store the complete result because for every pair of cells we had to classify and then store every other cell. Thus for reasonably sized worlds, such as those encountered in certain online games, this necessitated compression of the PVS for which we used a lossy compression scheme (van de Panne & Stewart, 1999).

In this paper, we delay actual frontier computation to runtime and we do not need to compress the PVS. Calculation of a single frontier pair still requires approximately $O(N)$ computation every time a client changes cell but in comparison to distance-based frontiers, greedy frontiers are more expensive to compute. We need to process the cells in connectivity order and this is not cache coherent, whereas the calculation for distance-based frontiers was. In fact, because combining PVSs of cells is itself an $O(N)$ activity, the actual calcula-

```cpp
AttemptEstablishGreedyFrontierWithOther (cellA, cellB) {
    frontierA = frontierB = \emptyset

    /* A frontier can only be set up if a and b cannot see each other. */
    IF b \not\in\text{PVS}(a) THEN {
        frontierA = \{a\}
        frontierB = \{b\}
        pvsFrontierA = \text{PVS}(a)
        pvsFrontierB = \text{PVS}(b)
    }

    /* GetLeaves() returns a list of all cells adjacent to x. */
    growA = a.GetLeaves()
    growB = b.GetLeaves()

    WHILE NOT (growA.Empty() AND growB.Empty()) DO {
        IF NOT growA.Empty() THEN {
            nextCell = growA.PopTop()
            IF (cell \not\in \text{pvsFrontierB}) THEN {
                frontierA.push(nextCell)
                pvsFrontierA = pvsFrontierA \cup \text{PVS}(nextCell)
                FOR EACH c \in \text{nextCell.GetLeaves()} DO {
                    IF (c \not\in\text{frontierA}) AND (c \not\in\text{growA}) THEN
                        growA.PushEnd(c)
                }
            }
        }
        IF NOT growB.Empty() THEN {
            /* Repeat block above, swapping A and B. */
        }
    }
}
```

Figure 7. Pseudocode for the function AttemptEstablishGreedyFrontierWithOther.
tion is theoretically $O(N^2)$. However in practice, PVS combination is a logical OR of two rows in a binary matrix and it doesn’t occur for every cell. For the worlds we have considered, observed performance is very close to linear time.

We can refine the greedy algorithm by modifying the breadth-first search, which represented by the lists growA and growB in Figure 7. We have found that sorting these lists on map distance to the original cell rather than a plain breadth-first search provides frontier sets that are balanced in cell size.

6 Application of Frontiers to Quake II

Frontiers have many potential applications. We want to demonstrate their utility by addressing the issue of scalability for network virtual environments.

Quake II (IdSoftware, 1997) is a first-person shooter game that was originally released in 1997. It uses a client-server architecture. A machine can be set up as a dedicated server, or one participant can host a server. Typical games have around 16 participants.

Quake II is an example of a game that uses a PVS structure. Primarily this is used to aid the runtime rendering speed because the PVS provides rapid culling of invisible parts of a model. It can also be used to cull moving entities such as participants or projectiles since these are located inside cells. A subsidiary use of the PVS is to aid network scalability. The server need only forward packets to a participant’s client if that participant can potentially see the entity concerned.

We have adopted Quake II rather than a newer game because IdSoftware has made the source code for the game and associated game tools available under the GNU Public License. This has allowed us to examine the behavior of the client and server and make tests such as using modified PVS files within the runtime renderer to confirm that they were correct.

Each game map in Quake II has its own static PVS. Typical map sizes in Quake II are between 1000 and 3000 cells. Figure 8 shows an example part of a PVS.

6.1 Network Trials

We have tested the frontier set concept by using network logs of groups of participants using Quake II. Staff and students at UCL were invited to take part in a Friday afternoon deathmatch on a Quake II server. We used the q2dm3, q2dm4, and q2dm8 maps that are included with the retail version of Quake II. A time limit switched between these maps at five-minute intervals. We invited participants for a one-hour session, though many connected early to practice, and some stayed late to settle grudges. Some participants connected from home or student halls, though most were on the local area network. For the analysis in Section 7.3 we have focused on three of the five-minute game periods where there were 16 or more participants connected.

The game clients were not customized, but were patched to the latest binary version (3.20). The game server was compiled from the available source code (3.21). The server was modified to record for each server frame (i.e., at 10 Hz) all the participant positions, and the corresponding PVS cells. These logs were then used offline to compute how many packets would be sent under different client-server and peer-to-peer schemes.
From the log files we then ran a series of simulations of network behavior for six networking schemes.

1. **Client-server.** Game clients send a packet describing their participant's position to the game server at the game frame rate. The server immediately relays packets to those other game clients that might see the participant's new position.

2. **Client-server aggregated.** Game clients send a packet describing their position to the game server at the game frame rate. The game server accumulates packets and once a frame sends one packet back to each game client describing the behavior of all other participants if any are visible.

3. **Naïve peer-to-peer.** Game clients send a packet to every other game client at the game frame rate.

4. **Perfect peer-to-peer.** A theoretical game client that sends a packet to only those game clients who need it at the game frame rate.

5. **Distance-based frontiers.** A game client that sends a packet to only those game clients who need them, or sends a packet to maintain a distance-based frontier.

6. **Greedy frontiers.** A game client that sends a packet to only those game clients who need them, or sends a packet to maintain a greedy frontier.

Client-server and naïve peer-to-peer represent the most commonly used networking models. Client-server aggregated is actually how Quake II works: it packages together all the position information for visible participants and returns it to the client at the game frame rate. In the simplified networking model, this will be impossible to beat by any other technique, but in real situations it introduces considerable latency into the game. It does of course also use larger data packets, and this complicates issues. In our analysis we have pessimistically assumed that aggregated packets take up no more resources than standard packets that contain the data for a single client. We return to these issues in Section 8.1.

The perfect peer-to-peer is impossible to implement because in order to decide whether to send a packet to another client it is necessary to know that client’s position already. This case is included for comparison with frontiers.

We expect that the frontier peer-to-peer schemes will send significantly fewer packets than naïve peer-to-peer. Of course, all the peer-to-peer systems have lower latency than all the client-server approaches.

7 **Results from Quake II Simulations**

The three maps q2dm3, q2dm4, and q2dm8 were chosen as they cover a range of different map styles. The map q2dm4 is an extensive map that is largely planar in layout. In contrast, q2dm8 is a compact map with multiple vertical levels with little visibility between the levels. The map q2dm3 is a compact level with a few examples of vertical complexity, but also strong occlusion between different regions.

7.1 **EPVS and Frontier Properties**

Table 1 shows statistics for the EPVS and frontiers calculated for the maps q2dm3, q2dm4, and q2dm8. The maximum width is the greatest distance between any pair of cells in the graph. We can see what we might expect; for q2dm3 and q2dm8, which are the compact levels, the maximum width is 4 and 5, respectively. For q2dm4, which is much more extensive, the maximum width is 8. We also give the average distance between a pair of cells. This gives us an impression of how dense the maps are. The higher the number, the better we expect frontiers to work because it indicates that players are likely to be remote from each other on the visibility metric.

Figure 1 showed a pair of distance-based frontiers for the map q2dm4. Because the maps in Quake II show a lot of inter-cell visibility over quite long distances, often across the whole map, we find that the frontiers often show quite ragged shapes where it wouldn’t be possible for a participant to walk to every cell in the frontier without exiting the frontier. This is actually a feature because participants are teleported across the map when they are shot.

Because frontiers represent mutually invisible areas of the map we look at the proportion of the cell pairs that contain viable frontiers, and how much of the map is
contained in these frontiers. We should expect that as worlds get extremely large, there will almost always be a frontier, and the two sets of cells in the frontier will (between them) contain close to 100% of the remaining cells.

Table 1 thus presents two sets of statistics about the two types of frontiers. Frontier density refers to the percentage of pairs for which a frontier can be found. Because there are a very large number of frontier pairs to compare, these values are calculated by sampling 100,000 pairs of frontiers by choosing the two starting cells at random. We see that in the spread out q2dm4, for approximately 93% of pairs of cells, a frontier can be found. Even with the densely packed q2dm3 and q2dm8, for around 84% of pairs of cells a frontier can be found. Of course frontiers can vary in size greatly, from a single cell to a large section of the map. Thus frontier size refers to the average size of a frontier. This is the percentage of cells on the map that are in either of the sides of a frontier on average. It gives an estimate of how efficient the separation of frontiers is. In extremely large worlds, this would tend towards 100%. We can see that the greedy frontiers scheme generates much larger frontiers in general. In q2dm3 and q2dm8 we see that distance-based frontiers algorithm generates frontiers that on average only contain 38% of the map, whereas the greedy frontiers algorithm generates frontiers with over 65% coverage. On visual comparison of the results of the two algorithms, what appears to be happening is that in dense maps such as q2dm3 and q2dm8, we get highly asymmetric frontiers. This happens because the PVS of all the cells at visibility distance one covers a very large proportion of the map, thus meaning that there are very few cells that can be added to the other side. In contrast, with the greedy frontiers algorithm we slowly grow each region meaning that a balance is more likely to be achieved. On q2dm4, both algorithms perform a lot better as might be expected because the map is more spread out. The greedy frontiers scheme still wins but the difference is not so great (82% versus 67%).

This suggests that if size and balance are important, the greedy frontiers algorithm is preferred. However, as we will see in Section 7.3, both types of frontiers were still very useful for culling network packets.

### 7.2 Frontier Usage

From the game server logs we were able to simulate the behavior of the frontier algorithm for a multi-participant situation. Figure 9 shows a sequence of positions of two participants in the game. Two participants repeatedly negotiate distance-based frontiers and then eventually can see each other and must send packets continuously. Although the panels show several renegotiations of frontiers, it should be made clear that in real time these happened roughly 5–10 seconds apart.

The panels in Figure 10 show a complete group of 16 participants in the game, again with distance-based frontiers. We see a variety of types of groups: large mutually visible groups, small groups, and isolated participants. Mutually visible groups have to keep each other up to date every frame. Isolated participants often keep frontiers with every other participant for quite long periods.
of time. When a participant is killed and teleported across the map to a new start point we see a “starburst” of communication as it has to relay its new position to every other participant and establish the relevant frontiers.

7.3 Comparison of Networking Schemes

From the simulations we were able to compare the networking schemes. Throughout the analysis we have used a simplified networking model that assumes that clients send and receive packets at the server’s frame rate (10 Hz—the actual server rate for Quake II). We also assume that all communication takes place within a server frame (100 ms) so that we do not have to consider latency when we are communicating frontier information. We discuss this issue in Section 8.1.

As discussed in Section 6.1, a client-server system that aggregates packets is bound to result in fewest packets since each client sends exactly one packet and must receive at most one per frame, resulting in $O(N)$ packets. However, in our simplified model, this is at the expense of over 50 ms increase in latency over the latency for a standard client-server system (50 ms for the average server caching delay, plus the extra travel time for routing the packet via the server rather than direct peer-to-peer). A peer-to-peer system with no scalability must send and receive $O(N^2)$ packets a second, but the latency is as low as possible.

Table 2 shows comparisons of the six networking schemes described in Section 6.1. For each map and each scheme it gives the total number of packets sent...
over the five minutes of the game. It also gives the packets per simulation frame and the packets per client per simulation frame. As expected, naïve peer-to-peer always produces significantly higher numbers of packets than any other scheme. The first point to note is that the frontier-based networking schemes performed well compared to the perfect peer-to-peer technique. Greedy frontiers are superior to distance-based frontiers as might be expected because the frontier regions are larger. Greedy frontiers only generate 17–21% more packets than the perfect peer-to-peer technique. The distance-based frontiers generate up to 45% more packets than perfect peer-to-peer. The most notable point, though, is that the greedy frontier scheme beats the unaggregated client-server technique on all maps. The distance-based frontier is comparable to the unaggregated client-server technique and beats it on one of the three maps.

8 Discussion and Further Work

8.1 Network Issues

In our analysis we have used a simplified networking model where the clients and servers all update at a fixed frame rate and all communication is completed within the frame time. Obviously this is a simplification and clients will vary in their latency and will not have the same frame rate as the server. For the purposes of the validity of the frontier-algorithm this means that we must deal with latency in communication of frontiers. When there is latency, the frontier might become invalid on one client but the other is unaware and does not send the required information. This means that a participant A leaving a cell might move to a location where they can see B, but will not actually see them until a packet has been sent to and received from B. B also potentially sees an incorrect status of A, but only for the time it takes for the update to travel from A to B. It is worth noting that this is no worse than the similar latency issues with server-based filtering: the server does not have the up to date state for the clients for which it is returning filtered data to.

The problem is perhaps best tackled by predicting ahead that the client is going to leave the frontier and speculatively renegotiating the frontier. This could be done by position extrapolation or by a scheme by which clients always test the frontier when they reach one of its boundary cells.

A second set of networking issues revolves around the security and manageability of peer-to-peer services. We have suggested that peer-to-peer is preferable because it is lower latency. However there are several problems in implementing peer-to-peer systems. The first problem is

<table>
<thead>
<tr>
<th>Map</th>
<th>Technique</th>
<th>Total packets sent</th>
<th>Packets per frame</th>
<th>Packets per client per frame</th>
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<td>q2dm3</td>
<td>CS</td>
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<td>75.1</td>
<td>4.7</td>
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<td>92869</td>
<td>31.2</td>
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<td>15.0</td>
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<td></td>
<td>PPP</td>
<td>176098</td>
<td>59.1</td>
<td>3.7</td>
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<tr>
<td></td>
<td>DBF</td>
<td>256040</td>
<td>86.0</td>
<td>5.4</td>
</tr>
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<td></td>
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<td>209524</td>
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<tr>
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<td>47.6</td>
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<tr>
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<td>CSA</td>
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<td>GF</td>
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</table>

*Note: CS = Client-server, CSA = Client-Server Aggregated, NPP = Naïve Peer-to-Peer, PPP = Perfect Peer-to-Peer, DBF = Distance-Based Frontiers, GF = Greedy Frontiers.*
in synchronizing the state among multiple hosts. This was first tackled in the bucket synchronization mechanism implemented in the MiMaze system (Diot & Gau-tier, 1999). MiMaze was one of the first fully distributed multi-participant games on the internet. The second problem is that of cheating. If the clients themselves are compromised, or the traffic between peers is modified, the state can be subverted to one participant’s advantage. This is being tackled within the networking community (GauthierDickey, Zappala, Lo, & Marr, 2004).

To counter the problems of implementing completely decentralized peer-to-peer networks, there is a possibility of hybrid architectures that use both peer-to-peer and client-server strategies. For example, a server could be used to synchronize critical game state such as keeping score and starting game sessions, but the clients could also communicate some state peer-to-peer so that they can render the game state as close to the server’s canonical state as possible.

Finally, although in our analysis the client-server aggregated algorithm performs best overall, we note that the actual situation is more complicated. As noted in Section 6.1 for our analysis we pessimistically assumed that aggregated packets are no larger than individual packets. This is pessimistic, from our point of view, because in reality, if packets are aggregated by the server, they may subsequently be fragmented by the network layer because they may be larger than the allowed maximum packet size. So in actuality, the client-server aggregated algorithm will perform somewhere between the idealized client-server aggregated algorithm we have presented, and the normal client-server algorithm which relays all packets as required.

### 8.2 Other Applications

We have introduced the frontier sets and an application for the culling of packets, in network simulations based on the visibility between clients. As is, the algorithm could be used in any situations where a PVS or similar data structure for culling structure exists.

Potentially it could be used for other network situations where it is useful to cull pairs of entities so that they need not be considered for a potentially expensive pair-wise computation. Essentially all that is required is some metric by which it can be determined that two entities do not need to communicate. For example, frontiers could be built to identify mutually inaudible regions, which would help with provisioning online environments with audio (Funkhouser, Min, & Carlbom, 1999). In this case the criteria for two frontiers to be valid would be that no cell in one was audible to any cell in the other.

### 8.3 Other Construction Techniques

We note that there are several other potential strategies for building frontiers. If there is a complete cells and portals data structure, then it is perhaps possible to analyze the graph itself to identify clusters of cells among which there is strong visibility, but which are not easily visible from other clusters. For example, game maps are sometimes arranged in a hub and spoke manner with a central area through which there is a lot of traffic, with subareas connected by corridors. As another example, in models of buildings it should be possible to find the intrafloor portals and isolate each floor for individual consideration.

More generally, it may be possible to partition the world via a hierarchical data structure such as octrees (Samet, 1989) and build frontiers for partitions of that data structure rather than the individual cells themselves.

Finally we note that if a cell C is in a frontier $F_{AB}$, then it is likely that cell A would be in $F_{CB}$. Thus instead of starting from scratch for each pair, it may be possible to reuse a frontier and adapt it by removing conflicting cells and adding others.

### 9 Conclusions

We have discussed frontier sets, a simple but powerful visibility structure, and we have shown how they can be constructed at runtime. For a pair of nodes, a frontier identifies two regions of mutual invisibility containing those nodes. For any application where there is a
need to cope with a large number of entities in a space that lends itself to spatial partitioning, frontiers should be a useful extension to enable scalability.

We have demonstrated the use of frontiers in simulations of the networked game Quake II. Networked games are a good example of a problem that involves multiple entities, all of which can potentially interact. This leads to an \(O(N^2)\) simulation problem. Fortunately network games often exhibit spatial separation of participants, so that we can usually discount many pairs of participants from potentially expensive operations such as communication of network state. We demonstrated that a network protocol based on frontiers has performance close to a client-server system and close to an ideal model of peer-to-peer systems. An aggregated client-server system is still faster than a frontier-based system, but to counter this, the frontier-based system has a significantly lower latency of communication. Using frontiers it should be possible to build a peer-to-peer game that scales more efficiently than existing peer-to-peer systems.

We have described two schemes for building frontiers at runtime: distance-based frontiers and greedy frontiers. In order to build frontier sets at runtime, we pre-computed an enhanced potentially visible set which only requires \(O(N^2)\) space in the number of cells. Since many games already require a PVS with this space requirement, this means that there is very little space overhead from using frontiers. Overall the simulations indicate that greedy frontiers should provide better performance, but this has to be tempered by the fact that they may be more complex to compute at runtime. Computing distance-based frontiers requires only a simple iteration through each cell in the map; whereas computing greedy frontiers requires an ordered traversal of the portal graph and the maintenance of a combined PVS of the partially completed frontiers.

**Acknowledgments**

All the code modifications we made to the GPL Quake II source code will be available from [http://www.cs.ucl.ac.uk/staff/A.Steed/quake/](http://www.cs.ucl.ac.uk/staff/A.Steed/quake/). This work was supported in part by the UK Equator project EPSRC Grant GR/N15986/01.

**References**


