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Teaching Computational Thinking

An Integrative Approach for Middle and High School Learning

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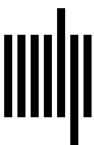
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