Discovery of Fourier-dependent time lags in cataclysmic variables

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ABSTRACT
We report the first study of Fourier-frequency-dependent coherence and phase/time lags at optical wavelengths of cataclysmic variables (MV Lyr and LU Cam) displaying typical flickering variability in white light. Observations were performed on the William Herschel Telescope using ULTRACAM. Light curves for both systems have been obtained with the SDSS filters $u'$, $g'$ and $r'$ simultaneously with cadences in the range $\approx 0.5–2$ s, and allow us to probe temporal frequencies between $\approx 10^{-3}$ and $\approx 1$ Hz. We find high levels of coherence between the $u'$, $g'$ and $r'$ light curves up to at least $\approx 10^{-2}$ Hz. Furthermore, we detect red/negative lags where the redder bands lag the bluer ones at the lowest observed frequencies. For MV Lyr time lags up to $\approx 3$ s are observed, whilst LU Cam displays larger time lags of $\approx 10$ s. Mechanisms which seek to explain red/negative lags observed in X-ray binaries and active galactic nuclei involve reflection of photons generated close to the compact object on to the surface layers of the accretion disc, where the lag delay is simply the light travel time from the emitting source to the reflecting accretion disc area. Although this could be a viable explanation for the lags observed in MV Lyr, the lags observed in LU Cam are too large to be explained by reflection from the disc and/or the donor star. We suggest reprocessing on the thermal time-scale of boundary layer photons on to the accretion disc as a possible mechanism to explain the lags observed in accreting white dwarfs, or reverse (inside-out) shocks within the disc travelling through cooler disc regions as they move outwards.

Key words: accretion, accretion discs–binaries: close–stars: individual: MV Lyr–stars: individual: LU Cam–novae, cataclysmic variables–X-rays: binaries.

1 INTRODUCTION
Cataclysmic variables (CVs) are close interacting binary systems where a late-type star transfers material to a white dwarf (WD) companion via Roche lobe overflow. With a system orbital period ranging from hours to minutes, the transferred material from the secondary star forms an accretion disc surrounding the WD. As angular momentum is transported outwards in the disc, material will approach the innermost regions close to the WD in the absence of strong magnetic fields, and eventually accrete onto the compact object. X-ray binaries (XRBs) are also compact interacting binaries which are similar to CVs in many ways, but where the accreting compact object is either a black hole (BH) or a neutron star. Both CVs and XRBs, as well as active galactic nuclei (AGN; accreting extragalactic supermassive BHs), have been shown to display aperiodic variability on a broad range of time-scales, with often very strong fractional root-mean-square (rms) amplitude. XRBs have shown variability ranging from milliseconds to hours, whilst for CVs this ranges from seconds to days. This difference can be mainly attributed to the fact that the innermost edges of the accretion discs in CVs sit at a few thousand gravitational radii ($r_g$), whilst for XRBs it can reach down to just a few $r_g$. The fact that material can get deeper within the gravitational potential of XRBs, as compared to CVs, also explains why they are more luminous and emit predominantly in X-rays, compared to CVs, which emit predominantly at optical/UV wavelengths.

Aperiodic broad-band variability (also referred to as flickering) has extensively been studied in X-rays for XRBs over several decades in temporal frequency (see for example Terrell 1972; van
der Klis 1995; Belloni et al. 2000; Homan et al. 2001; Belloni, Psaltis & van der Klis 2002). As CVs emit mostly at optical/UV wavelengths, timing studies of these objects had to rely on optical observing campaigns from Earth, which are inevitably hindered by large interruptions, poor cadence, and in many cases poor signal-to-noise ratios. Furthermore, the key time-scales to probe in CVs are much longer than in XRBs, requiring long, uninterrupted observations. Recently, CV timing studies have been facilitated thanks to the advent of the kepler satellite (Gilliland et al. 2010; Jenkins et al. 2010), which is able to provide long, uninterrupted and high-precision light curves in the optical light from space. Thanks to these capabilities it is now possible to probe over four orders of magnitude in temporal frequency in CVs. One important discovery in this respect is that the flickering properties of CVs in the optical are very similar, at least phenomenologically, to those observed in X-rays for XRBs (Mauche 2002; Warner, Woudt & Pretorius 2003; Scaringi et al. 2012a,b). More specifically, the discovery of linear rms–flux relations in the CV MV Lyr (as well as in XRBs and AGN; Uttley & McHardy 2001; Uttley, McHardy & Vaughan 2005) seems to rule out simple additive processes as the source of flicker noise (e.g. superposition of many independent ‘shots’), and instead strongly favoured multiplicative processes (e.g. mass-transfer variations travelling from the outer to inner disc for the latter) as the source of variability.

Additional similarities between the broad-band timing properties of XRBs and AGN are observed in X-rays when analysing simultaneous light curves obtained in two energy bands. Frequency-dependent phase/time lags are detected for both XRBs and AGN over a wide range of frequencies (Vaughan & Nowak 1997; Nowak 2003; Fabian et al. 2009; Uttley et al. 2005; Cassatella, Uttley & Maccarone 2012a; Cassatella et al. 2012b; De Marco et al. 2012), where X-ray hard/blue photons lag X-ray soft/red ones at low frequencies (by ≈ hours for AGN and by ≈ seconds for XRBs), and where the opposite is observed at higher frequencies (by <1 h for AGN and by <1 s for XRBs). Additionally, in some XRBs, the X-ray phase lags are observed to change sign as a function of intensity, hardness and/or frequencies (Reig et al. 2000). The reason for these Fourier-dependent phase/time lags is still debated, but viable scenarios exist to explain the observed phenomena. For example, the fluctuating accretion disc model (Lyubarskii 1997; Arévalo & Uttley 2006) assumes fluctuations in the mass-transfer rate within the disc to cause the observed variability over a wide range of frequencies, with long time-scale variability being produced further out in the accretion disc as compared to the fast time-scale variability produced further in. As the long time-scale variations propagate inwards, they couple to the fast time-scale variations, which also explains the observed rms–flux relations (Uttley & McHardy 2001; Heil, Vaughan & Uttley 2012; Scaringi et al. 2012b). A consequence of this model is that we should observe blue/hard photons lagging redder/softer ones at the longest observable frequencies as a consequence of fluctuations propagating inwards and thus passing through different (and hotter) emitting regions in the disc. On the other hand, the soft/negative lag (where soft photons lag hard ones) should be observed at the highest frequencies, and are explained by reprocessing of X-ray photons produced close to the compact object (by the Comptonized component observed as a power law in hard X-ray spectra) on to the accretion disc, either as a thermal blackbody (e.g. X-ray heating from the disc) or, in the case of AGN, as an additional soft photoionized reflection component. In this case, the size of the negative lags would provide an indication of the size of the reprocessing region in the disc: hard/blue photons are seen first as they are reprocessed closer in the accretion disc than the soft/red ones, and the time lag would simply be the light travel time from the central compact object to the reprocessing region plus a small reprocessing time.

A comprehensive analysis of coherence, phase and time lags at optical wavelengths has never been performed, and because of this no such study has ever been attempted for CVs. In this paper, we present the first analysis with data obtained on the 4.2 m William Herschel Telescope (WHT), using ULTRACAM, to study Fourier-dependent coherence, phase and time lags over three orders of magnitude in temporal frequency for two CVs, LU Cam and MV Lyr. This analysis provides useful insight into the broad-band variability behaviour of CVs, and reveals further similarities to the behaviour observed in X-rays for XRBs and AGN.

MV Lyr is classified as being a VY Scii nova-like system, spending most of its time in a high state (V ≈ 12–13), but occasionally (every few years) undergoing short-duration (weeks to months) drops in brightness (V ≈ 16–18; Hoard et al. 2004). The reason for these sudden drops in luminosity is not ccd.. mg Lag clear, but suggestions involving star spots on the secondary inhibiting mass transfer have been proposed (Livio & Pringle 1994). An orbital period of 3.19 h has been determined for the system, as well as a low inclination of i ≈ 11°–13° (Skillman, Patterson & Thorstensen 1995). Scaringi et al. (2012a,b) have already studied the single-band variability behaviour using Kepler data, and here we concentrate on the multiband behaviour of this system at higher frequencies. Much less is known for LU Cam apart from its orbital period of 3.6 h inferred from optical spectroscopy (Sheets et al. 2017). We decided to observe LU Cam with ULTRACAM to study in more detail the variability behaviour after one of us (PJJ) noted its strong variability on time-scales of weeks in the data of the Palomar Transient Factory (Law et al. 2009; Rau et al. 2009).

In Section 2, we will describe our ULTRACAM observations and data reduction procedures to obtain the coherence and phase/time lags. Section 3 will provide the main results and comment on the observed Fourier-dependent features. Our discussions and comparison to similar phenomena observed in XRBs and AGN are presented in Section 4, whilst our conclusions are drawn in Section 5.

2 OBSERVATIONS AND DATA REDUCTION

Both LU Cam and MV Lyr light curves presented in this paper were obtained with ULTRACAM (Dhillon et al. 2007) at the Cassegrain focus of the 4.2 m WHT on La Palma, Spain. ULTRACAM is a CCD camera designed to provide imaging photometry at high temporal resolution in three different filters simultaneously. The instrument provides a 5 arcmin field on its three 1024 × 1024 E2V 47-20 CDs (i.e. 0.3 arcsec pixel−1) on the WHT. Incident light is first collimated and then split into three different beams using a pair of dichroic beamsplitters. For all observations presented here, one beam was dedicated to the SDSS u’ (3543 Å) filter, another to the SDSS g’ (4770 Å) filter and the third to the SDSS r’ (6231 Å) filter. Because ULTRACAM employs frame-transfer chips, the dead time between exposures is negligible (≈0.02 s). The settings used for each observation can be found in Table 1, including exposure times and total number of frames. No binning was used and the readout speed was always set to slow as it provides the lowest detector readout noise (≈3 electrons).

1 However, instruments such as ULTRACAM allow for fast, multicolour and simultaneous photometry, and has been operational for several years.
All data were reduced using the ULTRACAM pipeline software. All frames were first debiased and then flat-fielded, the latter using the median of twilight sky frames taken with the telescope spiralling during twilight before observations. For MV Lyr, two bright reference stars were used to perform differential photometry, whilst four bright comparison stars were used for LU Cam. Furthermore, LU Cam was observed in the $u'$ band in co-add mode. For this mode, one $u'$-band exposure is performed for every two $g'$ and $r'$ exposures to increase signal-to-noise, but nevertheless all three exposures remain synced. To place all filters on the same time stamp, we averaged pairs of the $g'$ and $r'$ exposures. Portions of the extracted light curves for MV Lyr and LU Cam in the three filters are shown in Fig. 1.

For each observing run (two for MV Lyr and one for LU Cam), we obtained time-averaged power spectral densities (PSDs) by splitting each observing run (each lasting $\approx 6$ h) into six non-overlapping segments. For each segment (and for each band) we computed the fast Fourier transform (FFT) and applied the rms normalization of Belloni & Hasinger (1990) so that the square root of the integrated PSD power over a specific frequency range yields the rms variability of the degree of linear correlation between two simultaneously observed light curves in two different filters (or energy bands as used in X-rays). Specifically, it provides the fraction of the mean-squared variability at a specific frequency of one light curve which can be directly attributed to the other by a linear transformation (e.g. a simple time shift and flux re-scaling). As a simple intuitive example, two simultaneously observed light curves in two filters which display a constant time shift relating one to the other will display perfect coherence as well as a constant time lag, at all frequencies.

Let us consider two simultaneously observed light curves in two different filters $r(t)$ and $u(t)$. We here use a similar notation to that used in Nowak (2003), so that $r(t)$ is the longer wavelength band and $u(t)$ the short-wavelength band [$s(t) and h(t)$, respectively, in Nowak (2003)]. To compute the coherence (and indeed any other higher order Fourier statistic), we require an ensemble of independent measurements for each band in order to reduce statistical noise. Thus, both $r(t)$ and $u(t)$ are split into $M$ independent segments, where $M = 6$ in our case for both LU Cam and MV Lyr, so that each segment is about 1 h long. For each light-curve segment, $r_{i} = 1 \rightarrow M(t)$ and $u_{i} = 1 \rightarrow M(t)$, we compute the FFT $X_{r,i}(f)$ and $X_{u,i}(f)$, respectively, together with the corresponding power spectra $P_{r,i}(f) = |X_{r,i}(f)|^2$ and $P_{u,i}(f) = |X_{u,i}(f)|^2$ and cross-spectra $C_{r,u}(f) = X_{r,i}^*(f) X_{u,i}(f)$ (where $^*$ denotes the complex conjugate).

For each FFT, the Poisson (white) noise levels can be calculated as $|N_{r,i}|^2 = \frac{2}{\sigma_{r,i}^2}$ and $|N_{u,i}|^2 = \frac{2}{\sigma_{u,i}^2}$ for both bands [using the Belloni & Hasinger (1990) normalization]. Because in our case the errors obtained from the differential photometry will not be Poissonian (and could possibly be correlated between the different filter light curves due to systematic seeing effects in the comparison stars), we fit each independent PSD with a power law plus a constant to estimate the mean white noise levels $|N_{r,i}|^2$ and $|N_{u,i}|^2$. The intrinsic power for each segment in the $r$ light curve is then defined as $|R_{r,i}|^2 = |N_{r,i}|^2 + P_{r,i}(f) + C_{r,u}(f) = |N_{u,i}|^2 + P_{u,i}(f) + C_{u,r}(f)$.

\begin{table}[h]
\centering
\caption{ULTRACAM journal of observations during the observing runs.}
\begin{tabular}{|l|l|l|l|l|}
\hline
Object & Run & Dates        & Exposure/frame (s) & Frames  \\
\hline
MV Lyr & 1  & 2012 August 31 & 0.844              & 27 735  \\
MV Lyr & 2  & 2012 September 1 & 0.326            & 41 670  \\
LU Cam & 3  & 2012 January 10 & 2.276             & 18 502  \\
\hline
\end{tabular}
\end{table}

Figure 1. ULTRACAM light curves obtained in the $u'$ (bottom blue), $g'$ (middle green) and $r'$ (top red) filters for the CVs MV Lyr (top two panels) and LU Cam (bottom panel). The light curves have all been normalized by their respective mean count rate. The $r'$ and $u'$ light curves have also been shifted by 0.2 and $-0.2$, respectively, for clarity. Both systems clearly display variability on a wide range of frequencies.

2.1 Coherence function

The coherence function, $\gamma^2$, is a Fourier-frequency-dependent measure of the degree of linear correlation between two simultaneously observed light curves in two different filters (or energy bands as used in X-rays). Specifically, it provides the fraction of the mean-squared variability at a specific frequency of one light curve which can be directly attributed to the other by a linear transformation (e.g. a simple time shift and flux re-scaling). As a simple intuitive example, two simultaneously observed light curves in two filters which display a constant time shift relating one to the other will display perfect coherence as well as a constant time lag, at all frequencies.

Let us consider two simultaneously observed light curves in two different filters $r(t)$ and $u(t)$. We here use a similar notation to that used in Nowak (2003), so that $r(t)$ is the longer wavelength band and $u(t)$ the short-wavelength band [$s(t) and h(t)$, respectively, in Nowak (2003)]. To compute the coherence (and indeed any other higher order Fourier statistic), we require an ensemble of independent measurements for each band in order to reduce statistical noise. Thus, both $r(t)$ and $u(t)$ are split into $M$ independent segments, where $M = 6$ in our case for both LU Cam and MV Lyr, so that each segment is about 1 h long. For each light-curve segment, $r_{i} = 1 \rightarrow M(t)$ and $u_{i} = 1 \rightarrow M(t)$, we compute the FFT $X_{r,i}(f)$ and $X_{u,i}(f)$, respectively, together with the corresponding power spectra $P_{r,i}(f) = |X_{r,i}(f)|^2$ and $P_{u,i}(f) = |X_{u,i}(f)|^2$ and cross-spectra $C_{r,u}(f) = X_{r,i}^*(f) X_{u,i}(f)$ (where $^*$ denotes the complex conjugate).

For each FFT, the Poisson (white) noise levels can be calculated as $|N_{r,i}|^2 = \frac{2}{\sigma_{r,i}^2}$ and $|N_{u,i}|^2 = \frac{2}{\sigma_{u,i}^2}$ for both bands [using the Belloni & Hasinger (1990) normalization]. Because in our case the errors obtained from the differential photometry will not be Poissonian (and could possibly be correlated between the different filter light curves due to systematic seeing effects in the comparison stars), we fit each independent PSD with a power law plus a constant to estimate the mean white noise levels $|N_{r,i}|^2$ and $|N_{u,i}|^2$. The intrinsic power for each segment in the $r$ light curve is then defined as $|R_{r,i}|^2 = |N_{r,i}|^2 + P_{r,i}(f) + C_{r,u}(f) = |N_{u,i}|^2 + P_{u,i}(f) + C_{u,r}(f)$.
\[ P_{i,i} = |N_{i,i}|^2, \text{ and similarly for the } u \text{ light curve as } |U_i|^2 = P_{u,i} - |N_{u,i}|^2. \]

From this, we first define the raw coherence (i.e. the coherence without taking into account white noise) at a specific frequency as

\[ \gamma_{raw}^2(f) = \frac{1}{\langle\langle |C(f)|^2\rangle\rangle} \frac{\langle\langle |C(f)|^2\rangle\rangle}{\langle\langle |X(f)|^2\rangle\rangle \langle\langle |X_d(f)|^2\rangle\rangle}, \]

where the double angled brackets denote averages over adjacent frequency bins considered \( n_f \) in total as well as averages between the \( M \) independent segments. This notation will be used throughout the paper. The frequency binning in our case is logarithmic, with the frequency bins considered \( \log \) over/underestimated for our observations as the errors are not strictly Poissonian. Specifically, we expect errors in adjacent filter light curves to be correlated to some degree due to systematic effects in the comparison stars. For example, the apparent rise of the different colour combination, the apparently significant errors of the different colour combination, the apparently significant effects appearing in multiple band selection at high frequencies must be treated with caution. Nevertheless, we are confident that our coherence and phase/time lag estimates are reliable for frequencies below \( \approx 10^{-2} \text{ Hz} \) where uncertainties in the noise levels are.

\[ \Phi(f) = \arg\{\langle\langle |C(f)|^2\rangle\rangle\}, \]

with associated errors defined as

\[ \delta \Phi(f) = \frac{1}{\sqrt{m}} \sqrt{1 - \gamma_{raw}^2} \frac{2\gamma_{raw}^2}{2\gamma_{raw}^2}. \]

The Fourier phase lag is defined as the phase of the average cross power spectrum, defined as

\[ \Phi(f) = \frac{\Phi_{i,i}(f)}{\Phi_{i,i}(f) + \Phi_{u,u}(f)}. \]

Similarly, the error on the time lag is defined as \( \delta \tau(f) = \frac{\delta \Phi(f)}{2\pi f}. \)

### 3 RESULTS

Fig. 3 shows the coherence functions, phase and time lags for the three observing runs and all three colour combinations \( u' - r', u' - g' \) and \( g' - r' \). Both LU Cam and MV Lyr show high levels of coherence at the lowest observed frequencies in all three colour combinations. We note that above \( \approx 10^{-2} \text{ Hz} \) the noise levels start to affect our observations, resulting in larger error bars in this frequency range. The coherence is a fourth-order statistic and is very sensitive to uncertainties in the noise subtraction (Nowak 2003; Bendat & Piersol 2010).

The noise levels we infer from the PSD fits may also be slightly over/underestimated for our observations as the errors are not strictly Poissonian. Specifically, we expect errors in adjacent filter light curves to be correlated to some degree due to systematic effects in the comparison stars. For example, the apparent rise above 1 in the intrinsic coherence plots of MV Lyr in the \( r' - g' \) combination is due to an overestimation of the white noise level. Because of these uncertainties and possible correlations within errors of the different colour combination, the apparently significant features appearing in multiple band selection at high frequencies must be treated with caution. Nevertheless, we are confident that our coherence and phase/time lag estimates are reliable for frequencies below \( \approx 10^{-2} \text{ Hz} \) where uncertainties in the noise levels are.
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Negligible compared to the variability power, as also illustrated by the raw coherence plots.

Both LU Cam and MV Lyr also show similar features in the phase/time lags below $\approx 10^{-2}$ Hz. Specifically, we detect significant red/negative lags for both systems, where low-energy photons are seen arriving after the high-energy ones. In the case of LU Cam, negative lags are observed with an $\approx 10$ s delay below $10^{-3}$ Hz, whilst for MV Lyr this is much smaller at $\approx 3$ s. Furthermore, in both systems the negative lags are most pronounced in the $r' - u'$ combination, which might be expected as this is the filter combination with the largest wavelength difference. At higher frequencies, the time lags in MV Lyr seem to asymptote to 0, whilst for LU Cam they seem to swap sign reaching a few seconds at the highest observable frequencies. However, because the Poisson noise level in this frequency range affects our observations as described above, the high-frequency results must be treated with caution.

4 DISCUSSION

As this is the first study of this kind in CVs, it is non-trivial to predict the Fourier-dependent behaviour we have observed. We will thus address our results in the context of different time-scales which could potentially explain the observed lags in MV Lyr and LU Cam.

4.1 Viscous time-scale

If we take the fluctuating accretion disc model, which is frequently invoked to explain the Fourier time lags observed in the X-ray domain for XRBs and AGN (Uttley & McHardy 2001; Arévalo & Uttley 2006; Uttley et al. 2011; Cassatella et al. 2012a,b), we would expect to observe blue/positive lags in the optical for CVs. This would be a consequence of fluctuations propagating inwards through the disc on the viscous time-scale, and emitting redder photons before the blue ones as a consequence of accretion rate fluctuations passing through lower and then higher temperature emitting regions as they move inwards through the disc. What we observe in MV Lyr and LU Cam is the opposite: variations in blue photons are observed preceding the variations in the red photons. Because of this we must rule out this time-scale as a possible explanation for the observed lags.

4.2 Light travel time-scale

Red/negative lags somewhat similar to those observed here have also been observed in X-rays for XRBs and AGN (referred to as soft/negative lags). For example, De Marco et al. (2012) have shown how soft/negative lags are observed in X-rays for a sample of AGN, up to hundreds of seconds. The main interpretation for these lags is that they represent the light travel time to the disc from the variable continuum source. The continuum source illuminates the disc, which in the case of AGN leads to a soft photoionized reflection spectrum, while in XRBs the absorbed photons are also reprocessed and re-emitted as (soft X-ray) thermal radiation at the local disc blackbody temperature. Thus, in this model, the delay is simply the light-crossing time (plus a small reprocessing time, assuming also that the time-scale for thermal reprocessing is small;
see Section 4.3), which for XRBs will be milliseconds, and for AGN will be of the order of tens to hundreds of seconds. This scenario could potentially explain the \( \approx 1 - 3 \) s lags observed in MV Lyr, placing the reflecting/reprocessing region between 0.4 and 0.8 R\(_\odot\) [if we take the system parameters from Linnell et al. (2005) and Hoard et al. (2004)]. This range is both consistent with the outer edges of the disc and/or the secondary star.

Although the lag values are consistent with the expected binary separation in MV Lyr, this model would require the \( r \)-band emission to be dominated by the reprocessed light, otherwise the lags would be diluted by the variable central continuum emission. Furthermore, this interpretation seems to be unlikely for disc reprocessing at these large radii, since the disc is unlikely to reprocess much of the central continuum emission (van Paradijs & Verbunt 1984; de Jong, van Paradijs & Augusteijn 1996). Additionally, the much larger lags of \( \approx 10 \) observed in LU Cam rule out the possibility of the lag being produced by light travel times to the outer disc and/or secondary star. LU Cam does however leave the possibility that the reflecting region would sit at large radii, at \( \approx 6 \) R\(_\odot\), outside of the binary orbit, may be in the form of circumbinary disc/torus, although we would have to be viewing the system from a very specific angle. If this were the case, we would also expect the large-scale varying emission to be weak compared to the direct continuum emission from close to the compact object. This would imply that the observed lags from the reprocessing region at large distances would be diluted from the direct continuum emission, meaning that the intrinsic lags should be even larger than the ones observed in LU Cam. We note however that for the possibilities presented here, further spectral analysis would be required to investigate these possibilities.

### 4.3 Thermal time-scale

Another, possibly more plausible, scenario could be that the accretion disc is reprocessing energy originating from close to the compact object, for example in the boundary layer, on the local thermal time-scale. In MV Lyr, the boundary layer can reach \( \approx 100\,000 \) K (Godon & Sion 2011), allowing the colder disc (of \( \approx 10,000 \) K in the outer edges) to efficiently absorb such photons (as opposed to reflect them through Compton scattering as is the case for XRBs). In this scenario, one can imagine variable radiation influencing the accretion disc, where the observed red/negative lags are not only due to the light-crossing time from the source to the disc, but also due to the thermal reprocessing time of photons within the disc before they are re-emitted and observed. In this case, the relevant time-scale to consider is the thermal time-scale

\[
f_{th} = \frac{1}{\alpha \Omega}.
\]

where \( \Omega \) is the Keplerian frequency at a specific disc radius, and \( \alpha \) is the disc viscosity parameter, also at a specific disc radius (Shakura & Sunyaev 1973). With an accretion disc reaching the WD surface of \( \approx 0.01 \) R\(_\odot\), the corresponding thermal time-scale at the innermost edges of the disc is of the order of tens of seconds, depending on \( \alpha \). Our LU Cam result could potentially be explained through this process if \( \alpha \approx 0.7 \), which is considered to be high for accretion discs in CV systems. If on the other hand the reprocessing of photons were to occur at larger radii (say close to the outer edges of the disc at \( \approx 0.5 \) R\(_\odot\)), then the thermal time-scale would be much longer. In both scenarios however we would only expect the surface layer of the disc to reprocess photons, greatly reducing the time-scale inferred from equation (8) and possibly explaining the observed lags in MV Lyr and LU Cam. We note that the above scenario is a very general example, and we can imagine magnetic fields (instead of photon radiation) affecting the disc, which reprocesses the energy, and emitting photons after some delay, but again comparable to the thermal time-scale. The larger red/negative lags observed in AGN are also explained by a similar process, where the inner disc edge lies at a few au. The main difference is that for AGN (and XRBs), the X-ray photons originating close to the compact object are re-emitted nearly instantaneously as they photoionize the surface layers of the disc. In CVs on the other hand, the optical/UV emission close to the WD cannot photoionize the disc, but instead heats it up, and photons from the disc are then re-emitted on the thermal time-scale.

One last possible explanation for the observed lags in LU Cam and MV Lyr is that of reverse (inside-out) shocks within the accretion disc (Krausl et al. 2013), possibly originating from the WD boundary layer accretion disc. These waves would then transport energy outwards in the disc. In this scenario, the light-curve variations in the \( n \) band will be observed before those in the \( r \) band as a consequence of the shock(s) moving outwards in the disc and passing through the hotter inner edges and later through the cooler outer edges. The thermal time-scale of the disc (Frank, King & Raine 2002) would also be the relevant time-scale for the propagation of the shockwave, potentially in line with our observations. This interpretation, as well as all others presented here, requires thorough modelling in order to explain the lag phenomena observed in MV Lyr and LU Cam. Such modelling is however beyond the scope of this paper.

### 5 CONCLUSION

We have presented the first analysis of coherence, phase and time lags for CVs at optical wavelengths using ULTRACAM, mounted on the WHT. Our analysis is based on two objects, namely MV Lyr and LU Cam, which both show significant red/negative lags at frequencies below \( \approx 10^{-2} \) Hz, where blue photons are observed before the red ones. For MV Lyr this lag is observed to a maximum of \( \approx 3 \) s, whilst for LU Cam the lag is much larger at \( \approx 10 \) s. Furthermore, we established that both objects show high levels of coherence over a wide range of frequencies up to at least \( \approx 10^{-3} \) Hz. Mechanisms to explain the observed phenomena have been proposed, involving reprocessing of boundary layer photons (or other sources of energy close to the compact object) from the inner edge of the accretion disc on the local thermal time-scale, or reverse (inside-out) shocks travelling outwards in the disc. A thorough study of the implications of the results presented here, together with detailed modelling of the accretion disc reprocessing, is beyond the scope of this paper. We note however that any models trying to reproduce the observed Fourier-dependent behaviour in XRBs and AGN will, in future, need to address the features presented here as well, in order to provide a self-consistent model explaining the variability behaviour through all wavelengths (including optical) and throughout the different compact accretors (including WDs). Here we have only presented results on two CVs, and noted that both display significant lags at optical wavelengths. We might also expect that most flickering CVs will display similar lags, which will provide further grounds on which to test models seeking to explain the variability properties observed throughout the different types of compact accreting objects.

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