

# Exploiting Social Network Structure for Person-to-Person Sentiment Analysis

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## Abstract

Person-to-person evaluations are prevalent in all kinds of discourse and important for establishing reputations, building social bonds, and shaping public opinion. Such evaluations can be analyzed separately using signed social networks and textual sentiment analysis, but this misses the rich interactions between language and social context. To capture such interactions, we develop a model that predicts individual  $A$ 's opinion of individual  $B$  by synthesizing information from the signed social network in which  $A$  and  $B$  are embedded with sentiment analysis of the evaluative texts relating  $A$  to  $B$ . We prove that this problem is NP-hard but can be relaxed to an efficiently solvable hinge-loss Markov random field, and we show that this implementation outperforms text-only and network-only versions in two very different datasets involving community-level decision-making: the Wikipedia Requests for Adminship corpus and the Convote U.S. Congressional speech corpus.

## 1 Introduction

People's evaluations of one another are prevalent in all kinds of discourse, public and private, across ages, genders, cultures, and social classes (Dunbar, 2004). Such opinions matter for establishing reputations and reinforcing social bonds, and they are especially consequential in political contexts, where they take the form of endorsements, accusations, and assessments intended to sway public opinion.

The significance of such *person-to-person* evaluations means that there is a pressing need for computational models and technologies that can analyze

them. Research on *signed social networks* suggests one path forward: how one person will evaluate another can often be predicted from the network they are embedded in. Linguistic sentiment analysis suggests another path forward: one could leverage textual features to predict the valence of evaluative texts describing people. Such independent efforts have been successful, but they generally neglect the ways in which social and linguistic features complement each other. In some settings, textual data is sparse but the network structure is largely observed; in others, text is abundant but the network is partly or unreliably recorded. In addition, we often see rich interactions between the two kinds of information—political allies might tease each other with negative language to enhance social bonds, and opponents often use sarcastically positive language in their criticisms. Separate sentiment or signed-network models will miss or misread these signals.

We develop (Sec. 3) a graphical model that synthesizes network and linguistic information to make more and better predictions about both. The objective of the model is to predict  $A$ 's opinion of  $B$  using a synthesis of the structural context around  $A$  and  $B$  inside the social network and sentiment analysis of the evaluative texts relating  $A$  to  $B$ . We prove that the problem is NP-hard but that it can be relaxed to an efficiently solvable hinge-loss Markov random field (Broecheler et al., 2010), and we show that this implementation outperforms text-only and network-only versions in two very different datasets involving community-level decision-making: the Wikipedia Requests for Adminship corpus, in which Wikipedia editors discuss and vote on who should be

promoted within the Wikipedia hierarchy (Sec. 4), and the Convote U.S. Congressional speech corpus (Thomas et al., 2006), in which elected officials discuss political topics (Sec. 5). These corpora differ dramatically in size, in the style and quality of their textual data, and in the structure and observability of their networks. Together, they provide a clear picture of how joint models of text and network structure can excel where their component parts cannot.

## 2 Background and related work

### 2.1 Sentiment analysis

In NLP, the label *sentiment analysis* covers diverse phenomena concerning how information about emotions, attitudes, perspectives, and social identities is conveyed in language (Pang and Lee, 2008). Most work assumes a *dimensional model* in which emotions are defined primarily by valence/polarity and arousal/intensity (Russell, 1980; Feldman Barrett and Russell, 1998; Rubin and Talerico, 2009), and the dominant application is predicting the valence of product, company, and service reviews.

We adopt the conceptual assumptions of this work for our basic sentiment model, but our focus is on person-to-person evaluations and their social consequences. This involves elements of work on modeling political affiliation (Agrawal et al., 2003; Malouf and Mullen, 2008; Yu et al., 2008), bias (Yano et al., 2010; Recasens et al., 2013), and stance on debate topics (Thomas et al., 2006; Somasundaran and Wiebe, 2010; Lin et al., 2006; Anand et al., 2011), but these aspects of belief and social identity are not our primary concern. Rather, we expect them to be *predictive* of the sentiment classifications we aim to make—e.g., if two people share political views, they will tend to evaluate each other positively.

Recent work in sentiment analysis has brought in topical, contextual, and social information to make more nuanced predictions about language (Jurafsky et al., 2014; Wilson et al., 2005; Blitzer et al., 2007). We build on these insights with our model, which seeks to modulate sentiment predictions based on network information (and *vice versa*).

### 2.2 Signed-network analysis

Many social networks encode person-to-person sentiment information via *signed* edges between users

summarizing their opinions of each other. In this setting, one can leverage sociological theories of pairwise relationships and group-level organization to identify and understand patterns in these relationships (Heider, 1946; Cartwright and Harary, 1956).

*Balance theory* is based on simple intuitions like ‘a friend of my friend is my friend’, ‘an enemy of my enemy is my friend’, and ‘an enemy of my friend is my enemy’. In graph theory, these are statements about the edge signs of triangles of connected nodes: given the signs of two edges, balance theory predicts the third, as summarized in Fig. 1(a), where the two given edges (gray) determine the third (black).

For directed relationships, Leskovec et al. (2010b) formulate an alternative called *status theory*, which posits that networks organize according to social status: a node has positive edges to others with higher status and negative edges to those with lower status. Fig. 1(a) illustrates the structure of various directed signed triangles, where the sign of the third edge (black) can be inferred based on the signs and directions of the other two (gray).

Leskovec et al. (2010b) show that signed edges in networks emerge in a manner that is broadly consistent with both of these theories and that social-network structure alone can support accurate edge-sign predictions (Leskovec et al., 2010a). Kunegis et al. (2013) predict hidden positive and negative edges in a scenario where all observed edges are positive. Bach et al. (2013) and Huang et al. (2013) frame sign prediction as a hinge-loss Markov random field, a type of probabilistic graphical model introduced by Broecheler et al. (2010). Our model combines these ideas with a sentiment model to achieve even more robust predictions.

### 2.3 Synthesis of sentiment & network analysis

Models of sentiment and signed networks have been successful at a variety of tasks. However, missing from the current scientific picture is a deep understanding of the ways in which sentiment expression and social networks interact. To some extent, these interactions are captured by adding contextual and demographic features to a text-based sentiment model, but those features only approximate the rich relational structure encoded in a signed network.

Thomas et al. (2006) and Tan et al. (2011) capitalize on this insight using an elaboration of the

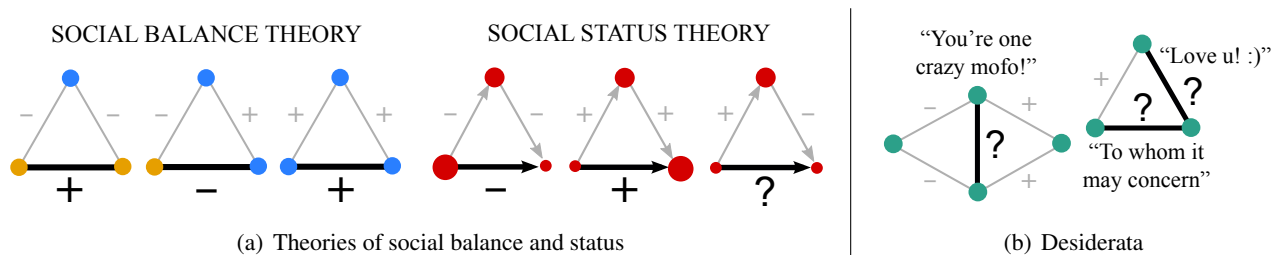


Figure 1: **(a)** Predictions of social balance and status theories for the bold black edge, given the thin gray edges. Balance theory reasons about undirected, status theory about directed, triangles. In the status diagrams, node size signifies social status. A positive edge may be replaced by a negative edge in the opposite direction, and *vice versa*, without changing the prediction. Status theory makes no prediction in the rightmost case. **(b)** Situations of the sort we aim to capture. At left, the network resolves textual ambiguity. At right, the text compensates for edge-label sparsity.

graph-cuts approach of Pang and Lee (2004). They are guided by an assumption of *homophily*, i.e., that certain social relationships correlate with agreement on certain topics: Thomas et al. (2006) use party affiliation and mentions in speeches to predict voting patterns, and Tan et al. (2011) use Twitter follows and mentions to predict attitudes about political and social events. Related ideas are pursued by Ma et al. (2011) and Hu et al. (2013), who add terms to their models enforcing homophily between friends with regard to their preferences.

We adopt some of the assumptions of the above authors, but our task is fundamentally different in two respects. First, whereas they model person-to-item evaluations, we model person-to-person evaluations; these are also the focus of Tang et al. (2013), who, though, use an unsigned network, whereas our work is geared toward distinguishing positive and negative edge labels. Second, the above models make overarching homophily assumptions, whereas we allow our model to explore the full set of triangle configurations suggested by Fig. 1(a).

### 3 Model

Here, we argue that combining textual and structural features can help predict edge signs. We formulate a model, show that it is computationally hard, and provide a relaxed version that is computationally tractable, building on work by Bach et al. (2013).

#### 3.1 Desiderata

In many real-world scenarios, rich features are associated with edges between two people, such as comments they made about each other, messages they

exchanged, or other behavioral features. Such features may contain a strong sentiment signal useful for predicting edge signs and may be used to fit a conventional sentiment model (Sec. 2.1).

However, the sign of an edge also depends on the signs of surrounding edges in the network (Sec. 2.2). A purely edge-feature-based sentiment model cannot account for the network structure, since it reasons about edges as independent of each other.

We argue that considering sentiment and network structure jointly can result in better predictions than either one on its own. Fig. 1(b) provides two illustrative examples. Here, the gray edge signs are observed, while the polarities of the black edges are to be predicted. In the left network, the text of the black edge (*‘You’re one crazy mof!’*) might suggest a negative polarity. However, a negative black edge would make both triangles inconsistent with balance theory (Fig. 1(a)), whereas a positive black edge makes them consistent with the theory. So, in this case, the network context effectively helps detect the teasing, non-literal tone of the statement.

In the right network of Fig. 1(b), only one of three edge signs is observed. Predicting two positive edges would be consistent with balance theory, but the same would be true for predicting two negative edges. The text on the lower black edge (*‘To whom it may concern’*) does not carry any clear sentiment signal, but the *‘Love u! :)’* on the other edge strongly suggests a positive polarity. This lets us conclude that the bottom edge should probably be positive, too, since otherwise the triangle would contradict balance theory. This shows that combining sentiment and network features can help when jointly reasoning about several unknown edge signs.

### 3.2 Problem formulation

We now formulate a model capable of synthesizing textual and network features.

**Notation.** We represent the given social network as a signed graph  $G = (V, E, x)$ , where the vertices  $V$  represent people; the edges  $E$ , relationships between people in  $V$ ; and the sign vector  $x \in \{0, 1\}^{|E|}$  represents edge polarities, i.e.,  $x_e = 1$  ( $x_e = 0$ ) indicates a positive (negative) polarity for edge  $e \in E$ .

Some types of relationships imply directed edges (e.g., following a user on Twitter, or voting on a candidate in an election), whereas others imply undirected edges (e.g., friendship on Facebook, or agreement in a network of politicians). We formulate our problem for undirected graphs here, but the extension to directed graphs is straightforward. We define a *triangle*  $t = \{e_1, e_2, e_3\} \subseteq E$  to be a set of three edges that form a cycle, and use  $T$  to indicate the set of all triangles in  $G$ . Finally, we use  $x_t = (x_{e_1}, x_{e_2}, x_{e_3}) \in \{0, 1\}^3$  to refer to  $t$ 's edge signs.

**Optimization problem.** We assume that the structure of the network (i.e.,  $V$  and  $E$ ) is fully observed, whereas the edge signs  $x$  are only partially observed. Further, we assume that we have a sentiment model that outputs, for each edge  $e$  independently, an estimate  $p_e$  of the probability that  $e$  is of positive polarity, based on textual features associated with  $e$ . The task, then, is to *infer the unobserved edge signs* based on the observed information.

The high-level idea is that we want to infer edge signs that (1) agree with the predictions of the sentiment model, and (2) form triangles that agree with social theories of balance and status. It is not always possible to meet both objectives simultaneously for all edges and triangles, so we need to find a trade-off. This gives rise to a combinatorial optimization problem, which we term TRIANGLE BALANCE, that seeks to find edge signs  $x^*$  that minimize an objective consisting of both edge and triangle costs:<sup>1</sup>

$$x^* = \arg \min_{x \in \{0, 1\}^{|E|}} \sum_{e \in E} c(x_e, p_e) + \sum_{t \in T} d(x_t). \quad (1)$$

The first term is the *total edge cost*, in which each edge  $e$  contributes a cost capturing how much its inferred sign  $x_e$  deviates from the prediction  $p_e$  of the

<sup>1</sup>Of course, the entries of  $x^*$  corresponding to observed edges are not variable but fixed to their observed values in Eq. 1.

sentiment model. The second term, the *total triangle cost*, penalizes each triangle  $t$  according to how undesirable its configuration is under its inferred signs  $x_t$  (e.g., if it contradicts status or balance theory).

We use the following edge cost function:

$$c(x_e, p_e) = \lambda_1(1 - p_e)x_e + \lambda_0 p_e(1 - x_e). \quad (2)$$

Here,  $\lambda_1, \lambda_0 \in \mathbb{R}_+$  are tunable parameters that allow for asymmetric costs for positive and negative edges, respectively, and  $p_e$  is the probability of edge  $e$  being positive according to the sentiment model alone. Intuitively, the more the inferred edge sign  $x_e$  deviates from the prediction  $p_e$  of the sentiment model, the higher the edge cost. (Note that at most one of the two sum factors of Eq. 2 is non-zero.)

The triangle cost for triangle  $t$  is signified by  $d(x_t)$ , which can only take on 8 distinct values because  $x_t \in \{0, 1\}^3$  (in practice, there are symmetries that decrease this number to 4). The parameters  $d(x_t)$  may be tuned so that triangle configurations that agree with social theory have low costs, while those that disagree with it (e.g., ‘the enemy of my friend is my friend’) have high costs.

### 3.3 Computational complexity

The problem defined in Eq. 1 is intuitive, but, as with many combinatorial optimization problems, it is hard to find a good solution. In particular, we sketch a proof of this theorem in Appendix A:

**Theorem 1.** TRIANGLE BALANCE is NP-hard.

### 3.4 Relaxation as a Markov random field

The objective function of Eq. 1 may be seen as defining a Markov random field (MRF) over the underlying social network  $G$ , with edge potentials (defined by  $c$ ) and triangle potentials (defined by  $d$ ). Inference in MRFs (i.e., computing  $x^*$ ) is a well-studied task for which a variety of methods have been proposed (Koller and Friedman, 2009). However, since our problem is NP-hard, no method can be expected to find  $x^*$  efficiently. One way of dealing with the computational hardness would be to find an *approximate binary* solution, using techniques such as Gibbs sampling or belief propagation. Another option is to consider a continuous relaxation of the binary problem and find an *exact non-binary* solution whose edge signs are continuous, i.e.,  $x_e \in [0, 1]$ .

We take this latter approach and cast our problem as a *hinge-loss Markov random field* (HL-MRF). This is inspired by Bach et al. (2013), who also use an HL-MRF to predict edge signs based on triangle structure, but do not use any edge features. An HL-MRF is an MRF with continuous variables and with potentials that can be expressed as sums of hinge-loss terms of linear functions of the variables (cf. Broecheler et al. (2010) for details). HL-MRFs have the advantage that their objective function is convex so that, unlike binary MRFs (as defined by Eq. 1), exact inference is efficient (Bach et al., 2013).

We achieve a relaxation by using sums of hinge-loss terms to interpolate  $c$  over the continuous domain  $[0, 1]$  and  $d$ , over  $[0, 1]^3$  (even though they are defined only for binary domains). As a result, the HL-MRF formulation is equivalent to Eq. 1 when all  $x_e$  are binary, but it also handles continuous values gracefully. We now interpret a real-valued ‘sign’  $x_e \in [0, 1]$  as the degree to which  $e$  is positive.

We start by showing how to transform  $c$ : even though it could be used in its current form (Eq. 2), we create a tighter relaxation by using

$$\tilde{c}(x_e, p_e) = \lambda_1 \|x_e - p_e\|_+ + \lambda_0 \|p_e - x_e\|_+, \quad (3)$$

where  $\|y\|_+ = \max\{0, y\}$  is the hinge loss. At most one term can be active for any  $x_e \in [0, 1]$  due to the hinge loss, and  $c(x_e, p_e) = \tilde{c}(x_e, p_e)$  for binary  $x_e$ .

To rewrite  $d$ , notice that, for any  $x_t \in \{0, 1\}^3$ , we can write  $d$  as

$$d(x_t) = \sum_{z \in \{0, 1\}^3} d(z) \delta(x_t, z), \quad (4)$$

where  $\delta(x_t, z) = 1$  if  $x_t = z$  and 0 otherwise. While  $\delta$  is not convex, we can use

$$f(x_t, z) = \|1 - \|x_t - z\|_1\|_+ \quad (5)$$

as a convex surrogate. When  $x_t$  is binary, either  $x_t = z$  so  $\|x_t - z\|_1 = 0$  or  $x_t \neq z$  so  $\|x_t - z\|_1 \geq 1$ , and hence  $f(x_t, z) = \delta(x_t, z)$ . To prove convexity, note that, for any fixed binary  $z \in \{0, 1\}^3$ ,  $\|x - z\|_1 = \sum_{i=1}^3 |x_i - z_i|$  is linear in  $x \in [0, 1]^3$ , since  $|x_i - z_i|$  equals either  $x_i$  (if  $z_i = 0$ ) or  $1 - x_i$  (if  $z_i = 1$ ). It follows that  $f$  is a hinge-loss function of a linear transformation of  $x_t$  and therefore convex in  $x_t$ .

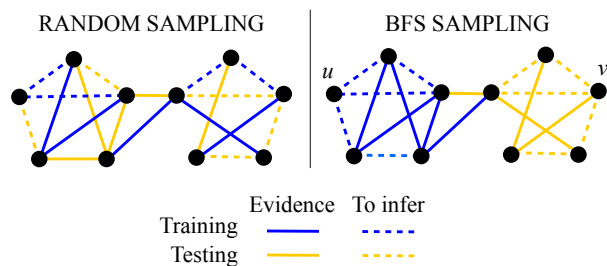


Figure 2: Options for training and testing our model.

Requiring the triangle cost  $d(z)$  to be nonnegative for all triangle types  $z \in \{0, 1\}^3$ , we can use

$$\tilde{d}(x_t) = \sum_{z \in \{0, 1\}^3} d(z) f(x_t, z) \quad (6)$$

as a convex surrogate for  $d$ . Our overall optimization problem is then the following relaxation of Eq. 1:

$$x^* = \arg \min_{x \in [0, 1]^{|E|}} \sum_{e \in E} \tilde{c}(x_e, p_e) + \sum_{t \in T} \tilde{d}(x_t). \quad (7)$$

This objective has the exact form of an HL-MRF, since it is a weighted sum of hinge losses of linear functions of  $x$ . We use the *Probabilistic Soft Logic* package<sup>2</sup> to perform the optimization, which is in turn based on the alternating-direction method of multipliers (ADMM) (Boyd et al., 2011).

**Learning.** Clearly, a solution is only useful if the cost parameters ( $\lambda_1$ ,  $\lambda_0$ , and  $d(z)$  for all  $z \in \{0, 1\}^3$ ) are set appropriately. One option would be to set the values heuristically, based on the predictions made by the social balance and status theories (Sec. 2.2). However, it is more principled to learn these parameters from data. For this purpose, we leverage the learning procedures included in the HL-MRF implementation we employ, which uses the voted-perceptron algorithm to perform maximum-likelihood estimation (Bach et al., 2013).

Since our data points (edges) interact with each other via the network, some words on how we perform training and testing are in order. Fig. 2 shows two options for obtaining training and testing sets (we use both options in our experiments). In the ‘random sampling’ paradigm, we randomly choose a set of edges for training (blue), and a disjoint set of edges for testing (yellow). In ‘BFS sampling’, we

<sup>2</sup><http://psl.umiacs.umd.edu>

run a breadth-first search from seed node  $u$  to obtain a coherent training set (blue), and likewise from a seed node  $v$  to obtain a coherent testing set (yellow), taking care that no edges from the training set are also included in the testing set.

During both training and testing, an arbitrary portion of the edge signs may be fixed to observed values and need not be inferred. These are the solid edges in Fig. 2; we refer to them as *evidence*. Further, we define the *evidence ratio* as the number of evidence edges, divided by the number of all edges considered (solid and dashed).

The learning algorithm may use the structure ( $V$  and  $E$ ) of the training graph induced by all blue edges (solid and dashed), the predictions  $p_e$  of the sentiment model for all blue edges, and the signs of the solid blue edges to predict the dashed blue edges.

During testing, the network structure of all yellow edges, the sentiment predictions for all yellow edges, and the signs of the solid yellow edges may be used to predict the dashed yellow edge signs. In principle, all training edges could be used as extra evidence for testing (i.e., all blue edges may be made solid yellow). However, in our experiments, we keep the training and testing sets fully disjoint.

**Technical details.** For clarity, we give further details. First, the distribution of positive and negative signs may be skewed; e.g., we observe a prior probability of 76% positive signs in our Wikipedia corpus (Sec. 4). Therefore, as also done by Bach et al. (2013), we add a cost term to our objective (Eq. 7) that penalizes deviations from this prior probability (as estimated on the training set). This ensures that the model can default to a reasonable prediction for edges that are not embedded in any triangles and about which the sentiment model is uncertain.

Second, intuitively, we should not penalize deviating from the sentiment model when it is itself uncertain about its prediction (i.e., when  $p_e$  is far from both 0 and 1). Rather, we want to rely more heavily on signals from the network structure in such cases. To achieve this, we introduce 10 pairs of cost parameters  $(\lambda_1^{(1)}, \lambda_0^{(1)}), \dots, (\lambda_1^{(10)}, \lambda_0^{(10)})$ . Then, we divide the interval  $[0, 1]$  into 10 bins, and when  $p_e$  falls into the  $i$ -th bin, we use  $\lambda_1^{(i)}$  and  $\lambda_0^{(i)}$  in Eq. 3. This way, larger costs can be learned for the extreme bins close to 0 and 1 than for the intermediate bins around 0.5.

Finally, hinge-loss terms may optionally be squared in HL-MRFs. We use the squared hinge loss in Eq. 5, since initial experimentation showed this to perform slightly better than the linear hinge loss.

## 4 Wikipedia experiments

Our first set of experiments is conducted on the Wikipedia Requests for Adminship corpus, which allows us to evaluate our model’s ability to predict person-to-person evaluations in Web texts that are informal but pertain to important social outcomes.

### 4.1 Dataset description

For a Wikipedia editor to become an administrator, a *request for adminship* (RfA)<sup>3</sup> must be submitted, either by the candidate or by another community member. Subsequently, any Wikipedia member may cast a supporting, neutral, or opposing vote. This induces a directed, signed network in which nodes represent Wikipedia members and edges represent votes (we discard neutral votes).

We crawled and parsed all votes since the adoption of the RfA process in 2003 through May 2013.<sup>4</sup> This signed network was previously analyzed by Leskovec et al. (2010b; 2010a). However, there is also a rich textual component that has so far remained untapped for edge-sign prediction: each vote is typically accompanied by a short comment (median/mean: 19/34 tokens). A typical positive comment reads, ‘*I’ve no concerns, will make an excellent addition to the admin corps*’, while an example of a negative comment is, ‘*Little evidence of collaboration with other editors and limited content creation.*’ The presence of a voting network alongside textual edge features makes our method of Sec. 3 well-suited for this dataset.

The RfA network contains 11K nodes, 160K edges (76% positive), and close to 1M triangles.

### 4.2 Experimental setup

**Train/test sets.** We follow the train–test paradigm termed ‘BFS sampling’ in Sec. 3.4 and Fig. 2, choosing 10 random seed nodes, from each of which we perform a breadth-first search (following both in- and out-links) until we have visited 350 nodes. We

<sup>3</sup><http://en.wikipedia.org/wiki/Wikipedia:RfA>

<sup>4</sup>Data available online (West, 2014).

thus obtain 10 subgraphs with 350 nodes each. We train a model for each subgraph  $i$  and test it on subgraph  $i + 1 \pmod{10}$ , ensuring that edges from the training graph are removed from the testing graph.

The BFS sampling paradigm was used because the alternative (‘random sampling’ in Fig. 2) produces subgraphs with mostly isolated edges and only a few triangles—an unrealistic scenario.

**Evaluated models.** We evaluate three models:

1. A standard, text-based sentiment model that treats edges as independent data points;
2. our full model as specified in Sec. 3.4, which combines edge costs based on the predictions of the text-based sentiment model with triangle costs capturing network context;
3. a version of our model that considers only triangle costs, while ignoring the predictions of the text-based sentiment model (akin to the model proposed by Bach et al. (2013)).

We refer to these models as ‘*sentiment*’, ‘*combined*’, and ‘*network*’, respectively.

**Sentiment model.** Our text-based sentiment model is an  $L_2$ -regularized logistic-regression classifier whose features are term frequencies of the 10,000 overall most frequent words. The  $L_2$ -penalty is chosen via cross-validation on the training set. Since comments often explicitly contain the label (‘*support*’ or ‘*oppose*’), we remove all words with prefixes ‘*support*’ or ‘*oppos*’. We train the model only once, on a random sample of 1,000 comments drawn from the set of all 160K comments (the vast majority of which will not appear in our 10 subgraphs).

**Evidence ratio.** Regarding the other two models, recall from Sec. 3.4 our definition of the *evidence ratio*, the fraction of edge signs that are fixed as evidence and need not be inferred. In our experiments, we explore the impact of the evidence ratio during training and testing, since we expect performance to increase as more evidence is available. (We use the same evidence ratio for training and testing, but this need not necessarily be so.)

**Metrics.** As our principal evaluation metrics, we use the areas under the curve (AUC) of the receiver operating characteristic (ROC) curve as well as the precision–recall (PR) curves. There are two PR

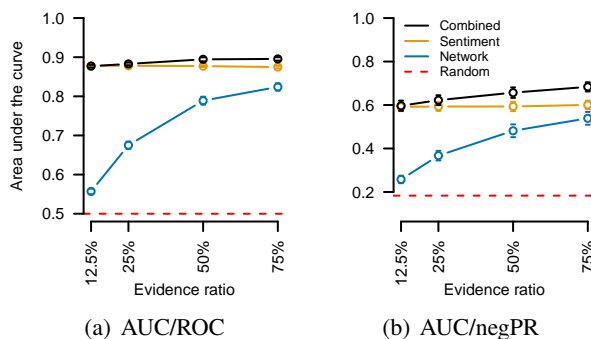


Figure 3: AUC as function of evidence ratio (Wikipedia), with standard errors.

curves, one for the positive class, the other for the negative one. Of these two, the positive class is less interesting: due to the class imbalance of 76% positive edges, even a random guesser would achieve an AUC of 0.76. The PR curve of the negative class is more informative: here, it is much harder to achieve high AUC, since random guessing yields only 0.24. Moreover, the negative edges are arguably more important, not only because they are rarer, but also because they indicate tensions in the network, which we might be interested in detecting and resolving. For these reasons, we report only the AUC under the negative PR curve (AUC/negPR) here.

Additionally, we report the area under the ROC curve (AUC/ROC), a standard metric for quantifying classification performance on unbalanced data. It captures the probability of a random positive test example receiving a higher score than a random negative one (so guessing gives an AUC/ROC of 0.5).

### 4.3 Results

**Performance as a function of evidence ratio.** The AUCs as functions of the evidence ratio are shown in Fig. 3(a). (We emphasize that these plots are not themselves ROC and PR curves; rather, they are derived from those curves by measuring AUC for a range of models, parametrized by evidence ratio.)

Since we use the same sentiment model in all cases (Sec. 4.2), its performance (yellow) does not depend on the evidence ratio. It is remarkably high, at an AUC/ROC of 0.88, as a consequence of the highly indicative, sometimes even formulaic, language used in the comments (examples in Sec. 4.2).

The network-only model (blue) works poorly on very little evidence (AUC/ROC 0.56 for 12.5% ev-



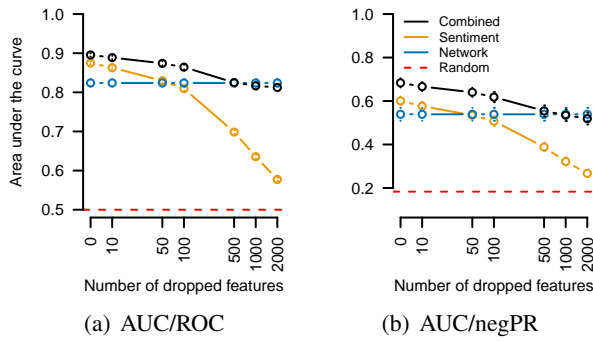


Figure 4: AUC as function of number of dropped features (Wikipedia), with standard errors. Evidence ratio 75%.

idence) but improves steadily as more evidence is used (AUC/ROC 0.82 for 75% evidence): this is intuitive, since more evidence means stronger context for each edge sign to be predicted.

Although the network-only model works poorly on little evidence, our full model (black), which synthesizes the sentiment and network models, is not affected by this and effectively defaults to the behavior of the sentiment-only model. Furthermore, although the network-only model never attains the performance of the sentiment-only model, combining the two in our full model (black) nonetheless yields a small performance boost in terms of AUC/ROC to 0.89 for 75% evidence. The gains are significantly larger when we consider AUC/negPR instead of AUC/ROC: while the sentiment model achieves 0.60, the combined model improves on this by 13%, to 0.68, at 75% evidence ratio.

**Performance as a function of sentiment-model quality.** It seems hard to improve by much on a sentiment model that achieves an AUC/ROC of 0.88 on its own; the Wikipedia corpus offers an exceptionally explicit linguistic signal. Hence, in our next experiment, we explore systematically how our model behaves under a less powerful sentiment model.

First, we measure, for each feature (i.e., word), how informative it is on its own for predicting the signs of edges (quantified by its mutual information with the edge sign), which induces a ranking of features in terms of informativeness. Now, to make the sentiment model less powerful in a controlled way, we drop the top  $m$  features and repeat the experiment described above for a range of  $m$  values (where we keep the evidence ratio fixed at 75%).



Figure 5: Normalized cost  $\lambda^{(i)}$  (defined in Sec. 4.3; logarithmic scale) for deviating from sentiment-model predictions  $p_e$ , for bins  $i = 1, \dots, 10$  (Wikipedia). Upper bin boundaries on the  $x$ -axis. Values shown are averages over 10 folds. Evidence ratio 75%.

Fig. 4 shows that the performance of the sentiment model (yellow) declines drastically as more features are removed. The combined model (black), on the contrary, is much less affected: when the performance of the sentiment model drops to that of the network-only (blue; ROC/AUC 0.81), the combined model is still stronger than both (0.86). Even as the sentiment model approaches random performance, the combined model still never drops below the network-only model—it simply learns to disregard the predictions of the sentiment model altogether.

**Learned edge costs.** Recall from the final part of Sec. 3.4 that each output  $p_e$  of the sentiment model falls into one of 10 bins  $[0, 0.1], \dots, [0.9, 1]$ , with separate edge-cost parameters  $\lambda_1^{(i)}$  and  $\lambda_0^{(i)}$  learned for each bucket  $i$ . The rationale was to give the model the freedom to trade off edge and triangle costs differently for each edge  $e$ , depending on how informative the sentiment model’s prediction  $p_e$  is.

The goal of this section is to understand whether our model indeed exposes such behavior. Recall from Eq. 3 that  $\lambda_1$  is the constant with which the absolute difference between  $p_e$  and the inferred edge sign  $x_e$  is multiplied when  $x_e > p_e$ , while  $\lambda_0$  is the constant when  $x_e < p_e$ . If  $p_e$  falls into bin  $i$ , the sum  $\lambda_1^{(i)} + \lambda_0^{(i)}$  expresses the cost of deviating from  $p_e$  in a single number; further, dividing this sum by the sum of all costs (i.e.,  $\lambda_1^{(i)}$  and  $\lambda_0^{(i)}$  for all bins  $i$ , plus the costs  $d(z)$  of all triangle types  $z$ ) yields a normalized edge cost for each bin  $i$ , which we call  $\lambda^{(i)}$ .

Fig. 5 plots  $\lambda^{(i)}$  for all bins  $i = 1, \dots, 10$ . We observe that deviating from the sentiment model costs more when it makes a strong prediction (i.e.,  $p_e$



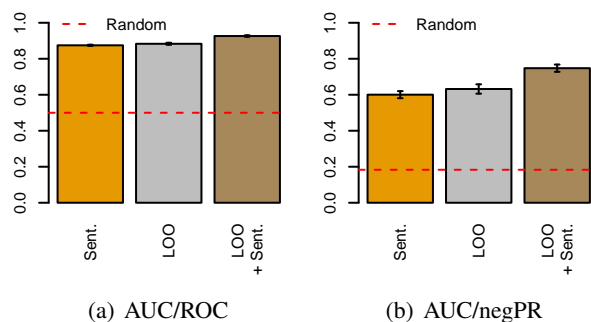


Figure 6: Performance in a leave-one-out (LOO) scenario (Wikipedia), with standard errors. For comparison: performance of the sentiment model alone.

close to 0 or 1) than when it makes a non-informative one (e.g.,  $p_e \approx 0.5$ ). When  $p_e \approx 1$ , nearly 100% of the total cost is spent to ensure  $x_e \approx p_e$ , whereas that fraction is only around 0.1% when  $p_e \approx 0.6$ .

**Leave-one-out setting.** Our model predicts many missing edge signs simultaneously, using joint inference. Another scenario was proposed by Leskovec et al. (2010a), who predict signs one at a time, assuming all other edge signs are known. We call this a *leave-one-out* (‘LOO’ for short) setting. Assume we want to predict the sign of the edge  $(u, v)$  in the LOO setting, and that  $u, v$ , and  $w$  form a triangle. The type of this triangle can be described by the directions and known polarities of the two edges linking  $u$  to  $w$ , and  $v$  to  $w$ , respectively. The edge  $(u, v)$  may be embedded in several triangles, and the histogram over their types then serves as the feature vector of  $(u, v)$  in a logistic regression; as additional features, counts of  $u$ ’s positive/negative out-links and  $v$ ’s positive/negative in-links are used.

Since predictions in the LOO setup can draw on the full triangle neighborhood of the edge in question, we expect it to perform better than the network-only model in which edge signs in the triangle neighborhood are often missing. This expectation is confirmed by Fig. 6, which shows that the LOO model (gray) achieves an AUC/ROC (AUC/negPR) of 0.88 (0.63), with the network-only model (Fig. 3) at just 0.82 (0.54) at 75% evidence ratio.

However, LOO is outperformed by our combined model incorporating sentiment information (Fig. 3), which attains an AUC/ROC (AUC/negPR) of 0.89 (0.68). Finally, when we add the sentiment prediction as another feature to the LOO model (‘LOO +

Sent.’ in Fig. 6), we do best, at 0.93 (0.75).

To summarize, we make two points: (1) By combining sentiment and network features, our model achieves better performance than a network-only model (LOO) that has access to significantly more network information. (2) Incorporating sentiment information helps not only in our setup as described in Sec. 4.2, but also in the previously proposed leave-one-out setup (Leskovec et al., 2010a).

## 5 U.S. Congress experiments

We now evaluate our model in a setting in which the linguistic person-to-person evaluations are less direct and reliable than in the RfA corpus but the signed network is considerably denser.

### 5.1 Dataset description

The ‘Convote’ corpus of Congressional speeches (Thomas et al., 2006) consists of 3,857 speech segments drawn from 53 debates from the U.S. House of Representatives in 2005. There is a mean of 72.8 speech segments per debate and 32.1 speakers per debate. Segments are annotated with the speaker, their party affiliation, the bill discussed, and how the speaker voted on that bill (positive or negative).

Thomas et al. (2006) and others represent this corpus as a bipartite person–item graph with signed edges from Congresspeople to the bills (items) they spoke about, and they add additional person–person edges encoding who mentioned whom in the speech segments. We take a different perspective, extracting from it a dense, undirected person–person graph by linking two Congresspeople if they ever voted on the same bill, labeling the edge as positive if they cast the same vote at least half of the time. We directly use the sentiment model trained by Thomas et al. The resulting graph has 276 nodes, 14,690 edges (54% positive), and 506,327 triangles.

### 5.2 Experimental setup

We split the network  $G = (V, E)$  into 5 folds using the ‘random sampling’ technique described in Sec. 3.4 and Fig. 2: the set of nodes  $V$  is fixed across all folds, and the set of edges  $E$  is partitioned randomly so that each fold has 20% of all edges. In the full graph, there is one clique per debate, so each fold contains the overlay of several subgraphs, one per debate and each 20% complete on average.

Here, random sampling was used because the alternative (‘BFS sampling’ in Fig. 2) would produce nearly complete subgraphs, on which we found the prediction task to be overly easy (since the problem becomes more constrained; Sec. 5.3).

We compare the three models also used on the Wikipedia dataset (Sec. 4.2). Our sentiment model comes right out of the box with the Convote corpus: Thomas et al. (2006) distribute the text-level scores from their SVM classifier with the corpus, so we simply work with those, after transforming them into probabilities via logistic regression (a standard technique called Platt scaling (Platt, 1999)). Thus, let  $q_u$  and  $q_v$  be the probabilistic sentiment predictions for  $u$  and  $v$  on a given bill. The probability that  $u$  and  $v$  agree on the bill is  $q_u q_v + (1 - q_u)(1 - q_v)$ , and we define the probability  $p_e$  of a positive sign on the edge  $e = \{u, v\}$  as the average agreement probability over all bills that  $u$  and  $v$  co-voted on.

For instance, the speech containing the sentence, ‘*Mr. Speaker, I do rise today in strong support of H.R. 810,*’ receives a probability of 98% of expressing a positive opinion on H.R. (i.e., House of Representatives) bill 810, whereas the prediction for the speech containing the words, ‘*Therefore, I urge my colleagues to vote against both H.R. 810 and H.R. 2520,*’ is only 1%. Hence, the edge between the two respective speakers has a probability of  $98\% \times 1\% + 2\% \times 99\% = 3\%$  of being positive.

### 5.3 Results

Fig. 7 summarizes our results. As in the Wikipedia experiments, we report AUCs as a function of the evidence ratio. The sentiment model alone (yellow) achieves an AUC/ROC (AUC/negPR) of 0.65 (0.62), well above the random baselines at 0.5 (0.46). The network-only model (blue) performs much worse at the start, but it surpasses the sentiment model even with just 12.5% of the edges as evidence, a reflection of the dense, high-quality network structure with many triangles. When we combine the sentiment and network models (black), we consistently see the best results, with the largest gains in the realistic scenario where there is little evidence.

Eventually, the network-only model catches up to the combined model, simply because it reaches an upper bound on performance given available evidence. This owes mainly to the fact that, because we

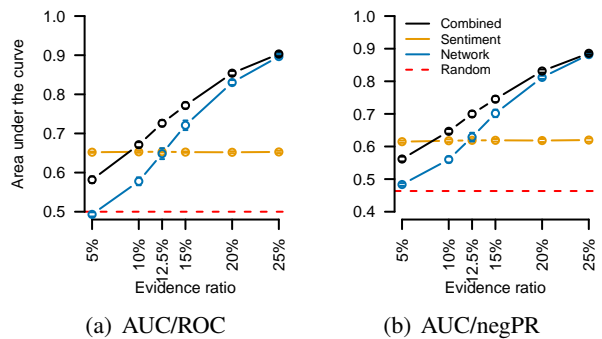


Figure 7: AUC as function of evidence ratio (Convote), with standard errors.

derived the person–person signs from person–item signs, only triangles with an even number of negative edges arise with noticeable frequency. To see why, suppose the corpus contained speeches about just one bill. In a triangle consisting of nodes  $u$ ,  $v$ , and  $w$ , if  $u$  agreed with  $v$  and with  $w$ , then  $v$  and  $w$  must agree as well. (The fact that we have multiple bills in the corpus opens up the possibility for additional triangle types, but they rarely arise in the data.) This constrains the solution space and makes the problem easier than in the case of Wikipedia, where all triangle types are possible.

Our plots so far have summarized precision–recall curves by measuring AUC. Here, it is also informative to inspect a concrete PR curve, as in Fig. 8, which shows all the values at 15% evidence ratio. The network-only model (blue) achieves very high precision up to a recall of about 0.20, where there is a sudden drop. The reason is that, according to the above argument about possible triangle types, the model can be very certain about some edges (e.g., because it is the only non-evidence edge in a triangle, making only a single triangle type possible), which causes the plateau for low recall. The combined model matches the precision on the plateau, but also maintains significantly higher precision as the network-only model starts to do more poorly: even if an edge  $e$  is not fully determined by surrounding evidence, the sentiment model might still give strong signals for  $e$  itself and its neighbors, such that the above reasoning effectively still applies.

## 6 Discussion

We developed a model that synthesizes textual and social-network information to jointly predict the po-

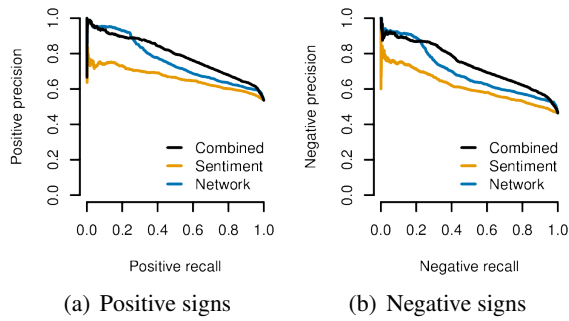


Figure 8: Precision/recall (Convote, evidence ratio 15%).

larity of person-to-person evaluations, and we assessed this model in two datasets. Both involve communal decision making, where people’s attitudes and opinions of each other have profound social consequences, but they are very different. In the Wikipedia corpus, the sentiment signal is strong because of established community norms for how to convey one’s opinions, but the network is sparse. In the Convote corpus, the network is determined by fully observed voting patterns, making it strong, but the speech texts themselves only indirectly and noisily convey person-to-person opinions. In both cases, our method excels because it is adaptive: it learns from the data how best to combine the two signals.

Our model’s adaptivity is important for real-world applications, where one is unlikely to know ahead of time which signals are most trustworthy. We envision the following use-case. One extracts a coherent subgraph of the network of interest, perhaps using one of our sampling methods (Fig. 2) and annotates its edges for their evaluativity. Then, in conjunction with a sentiment model (out-of-the-box or specially trained), one trains our combined model and uses it to predict new edge labels in the network. In this setting, the sentiment model might be unreliable, and one might have the time and resources to label only a small fraction of the edges. Individually, the network and sentiment models would likely perform poorly; in bringing the two together, our single model of joint inference could still excel.

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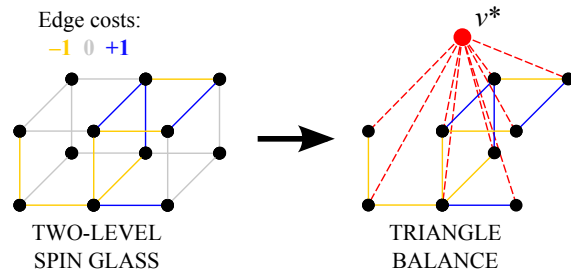


Figure 9: Reduction from TWO-LEVEL SPIN GLASS to TRIANGLE BALANCE.

## A Proof sketch of Theorem 1

Due to space constraints, we only give a proof sketch here; the full proof is available online (West, 2014).

*Proof sketch.* By reduction from TWO-LEVEL SPIN GLASS (TLSG), a problem known to be NP-hard (Barahona, 1982). An instance of TLSG consists of vertices  $V$  arranged in two 2D grids, one stacked above the other, with edges  $E$  between nearest neighbors, and with an edge cost  $c_{uv} \in \{-1, 0, +1\}$  associated with each edge  $\{u, v\}$  (see Fig. 9 for a small instance). Given such an instance, TLSG asks for vertex signs  $x \in \{-1, +1\}^{|V|}$  that minimize the total energy  $H(x) = -\sum_{\{u,v\} \in E} c_{uv} x_u x_v$ . The crucial observation is that TLSG defines vertex costs (implicitly all-zero) and edge costs, and asks for vertex signs, whereas TRIANGLE BALANCE defines edge costs and triangle costs, and asks for edge signs. That is, vertices (edges) in TLSG correspond to edges (triangles) in TRIANGLE BALANCE, and our proposed reduction transforms an original TLSG instance into a TRIANGLE BALANCE instance in which each edge corresponds to exactly one original vertex, and each triangle to exactly one original edge. As shown in Fig. 9, which depicts the reduction schematically, this is achieved by introducing a new vertex  $v^*$  that is connected to each original vertex and thus creates a triangle for each original edge. The full proof (West, 2014) shows how the edge and triangle costs can be constructed such that each optimal solution to the TLSG instance corresponds to an optimal solution to the TRIANGLE BALANCE instance, and *vice versa*.  $\square$

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