Unsteady Viscous Flow in a High Speed
Core Compressor

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ABSTRACT

A probe incorporating a miniature high-frequency response pressure transducer has been traversed behind the first three stages of a high-speed multistage compressor operating at throttle settings corresponding to near choke, peak efficiency and near surge. A novel method of compensating for transducer temperature sensitivity was employed. Consequently, time-averaged pressures derived from the transducer were found to be in good agreement with pneumatic pressure measurements. Analysis of the unsteady pressure measurements revealed both the periodic and random fluctuations in the flowfield. This provided information on rotor-rotor interaction effects and the nature of viscous blade wake and secondary flows in each stage.

INTRODUCTION

Further improvements in the efficiency, stage-loading, and stable operating range of compressors rely heavily upon developing improved computational flow modelling and design methods. In turn, the improvement of computational methods requires detailed measurements to be taken in representative compressors to create data bases for code validation. A number of workers have undertaken detailed measurements of the flow in axial compressors. Ravindranath & Lakshminarayana (1980) and Lakshminarayana & Govindan (1981) investigated the characteristics of blade wake development while Dring et al (1983), Lakshminarayana et al (1985) and Dong et al (1987) extended these studies to include secondary flow development in the hub and tip regions. Further, Wagner et al (1978) and Zeirke & Okiishi (1982) investigated the effects of bladerow interaction. These studies have done much to improve understanding of axial compressor flows and highlighted the complex, viscous, three-dimensional, interactive, and unsteady nature of the flowfield. However, all the cited studies have been limited to low-speed research compressors. Therefore, although blade geometry and stage loading may be representative of commercial compressors, flow Mach numbers are not.

Published measurements taken in high-speed compressors have been limited to single stage transonic fans (Weyer & Hungenberg (1976), Ng & Epstein (1985) and Gertz (1986). These indicate significant flowfield unsteadiness that has been attributed to shock oscillation. While the mechanism producing these unsteady effects has yet to be explained fully, it is likely that their existence, along with quasi-steady compressibility effects, have a significant influence upon the development of wake and endwall flows. Matters are further complicated by complex interaction between the stages within multistage compressors. Hence it is necessary to carry out investigations within high-speed (engine-relevant) compressors in order to improve the fundamental understanding of the phenomena involved and to explore the applicability of low-speed data for computational code validation.

Propulsion Department of the Royal Aerospace Establishment (RAE) is engaged in a programme to employ high frequency response instrumentation to investigate unsteady viscous flow within high-speed axial compressors and fans. The work reported in this paper documents preliminary activity 'piggy-backed' onto a major conventional rig measurement programme reported by Ginder (1991). A single sensor probe, containing a high-frequency response pressure transducer, was used to measure the unsteady flow within the first three stages of the five-stage C147 high-speed core compressor. Errors due to temperature sensitivity of the pressure transducer were corrected using a combination of careful calibration and an expedient method of measuring transducer diaphragm temperature. This system is described, together with the data acquisition and processing techniques employed. The time-averaged pressures derived from the compensated transducer signals are compared with conventional pneumatic measurements to illustrate the success of the method. Finally, unsteady pressure measurements taken at rotor exit are presented and discussed.

EXPERIMENTAL PROCEDURE

The Test Compressor

The RAE C147 research compressor is a high-speed machine representative of the rearmost stages of a military or highly loaded civil core compression system. It is of large scale, approximately 1 m in diameter, with extended axial gaps between the blade rows to allow detailed traverse measurements to be taken. To date it has been tested in two configurations. The initial build, reported by Calvert et al (1989), was a four stage compressor of 4.0 pressure ratio. For the second build, the blading was redesigned using the RAE S1-S2 calculation system (also described by Calvert et al.
Unsteady pressure measurements were taken in the second build of C147. Radial traverses were carried out behind rotors 0, 1 and 2 while the compressor was operating at three conditions on the 95% speed characteristic. The operating points, defined as near choke (A), peak efficiency (B) and near surge (C), are shown in Fig 1.

![Fig. 1 The performance characteristics of C147 build 2; A, B and C denote traverse operating points.](image)

Table 1

<table>
<thead>
<tr>
<th>Compressor/probe geometry</th>
<th>Rotor 0</th>
<th>Rotor 1</th>
<th>Rotor 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tip speed (m/s)*</td>
<td>313</td>
<td>304</td>
<td>299</td>
</tr>
<tr>
<td>Blade passing frequency (Hz)*</td>
<td>8623</td>
<td>10588</td>
<td>11680</td>
</tr>
<tr>
<td>Mean chord (m)</td>
<td>0.0590</td>
<td>0.0485</td>
<td>0.0440</td>
</tr>
<tr>
<td>Mean aspect ratio</td>
<td>1.559</td>
<td>1.296</td>
<td>1.034</td>
</tr>
<tr>
<td>Mean pitch-chord ratio</td>
<td>0.551</td>
<td>0.550</td>
<td>0.552</td>
</tr>
<tr>
<td>Probe diameter</td>
<td>0.049</td>
<td>0.059</td>
<td>0.065</td>
</tr>
<tr>
<td>Mean pitch</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>X*</td>
<td>0.154</td>
<td>0.195</td>
<td>0.208</td>
</tr>
<tr>
<td>Mean rotor chord</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* At 95% speed  
** X = Mean streamwise distance from rotor trailing edge to the transducer diaphragm.

Traverse Probes

Three probes were used to take the unsteady pressure measurements. Each contained a single Kulite type XCQ-062 (344 kPa absolute) pressure transducer of 1.57 mm diameter mounted 1.65 mm below a pneumatic Pitot tube as shown in Fig 2. Two of the transducers employed a 0.07 mm thick coating of silastomer rubber to protect the pressure sensing diaphragm while the third utilised a perforated metal (Kulite 'type B') screen for protection. The relative size of the probes to the rotor rows traversed is shown in Fig 3 and detailed in Table 1 along with additional information concerning the blade rows.

Unpublished measurements, taken by Oxford University for RAE, show that the natural resonant frequency of the 'coated' transducer diaphragm was of the order of 500 kHz. The frequency response characteristics ensured a 'flat' amplitude response with negligible phase angle lag over a 100 kHz bandwidth. Frequency response of the 'screened' transducer is determined by the natural resonant frequency of the screen geometry coupled to that of the cavity between the screen and the transducer diaphragm. Measurements made by Oxford University show that this is 50-60 kHz. Measurements taken behind rotor 0 in C147, with both types of transducer, indicate that both measurements were generally in good qualitative and quantitative agreement but that some attenuation of peak unsteadiness levels occurred with the screened transducer.

![Fig. 2 The pressure probe used during the traverses.](image)

![Fig. 3 The size of the traverse probe relative to the compressor.](image)
The sensitivity of a screened transducer probe to yaw angle was measured in an open jet wind tunnel at a Mach number of 0.7. Results showed that transducer output varied by less than 1% over ±10° range. Prior to each rotor exit traverse in C147, the probe was yawed to ensure that its axis was aligned with the mean flow at 50% span. Limited checks carried out at other radii indicated that deviation from the mean mid-span flow angle was less than ±10°.

Transducer Temperature Compensation

The strain gauge elements, that sense transducer diaphragm deflection, are prone to changes in resistance with temperature because of their high thermal coefficient of resistance. Consequently transducer pressure sensitivity and null-pressure reading (or zero-offset) change with temperature. Hence large pressure measurement errors arise if the sensitivity and zero-offset, used to convert the transducer output voltage to pressure, are not those associated with the temperature experienced by the transducer diaphragm. At RAE Bedford, Welch and Pyne (1980) showed that if the transducer is excited with a constant voltage, changes in strain gauge bridge resistance induce a change in current drawn by the bridge which can in turn be sensed as a change in voltage across a 'sense' resistor placed in series with the transducer polarising voltage. A prototype system using this approach was produced which coupled commercially available signal conditioning amplifiers to a 'sense' resistance monitoring module (Fig 4). Setting-up of the system required the transducer to be immersed in a chamber where both pressure and temperature could be varied. Hence, the transducer pressure sensitivity and zero-offset were determined from the transducer output (Vo) for a range of constant temperature. Similarly, the 'sense' voltage (Vs), which is independent of pressure, was monitored. Subsequently, the variations of Vo and Vs with temperature were coded into a data processing program. Hence, during the compressor measurements, Vs was used to determine transducer diaphragm temperature which in turn was used to derive the associated pressure sensitivity and zero-offset in order to convert Vo to the correct absolute pressure level.

Ideally the calibrated performance of a transducer should not change significantly with time. However measurements taken at RAE have recorded transducer ‘calibration drift’ corresponding to up to 1% of transducer full scale deflection over several weeks. This calibration drift was quantified by calibrating the transducers several times during the test series. Further checks carried out at other radii indicated that deviation from the mean mid-span flow angle was less than ±10°. Prior to each rotor exit traverse in C147, the probe was yawed to ensure that its axis was aligned with the mean flow at 50% span. Limited checks carried out at other radii indicated that deviation from the mean mid-span flow angle was less than ±10°.

Data Acquisition and Processing

The unsteady pressure signals were recorded on a CEL Datalab Multitrap data acquisition system. This consists of three main components: a waveform recorder, a 20 Mbyte Winchester disc and a host Hewlett Packard HP510 micro-computer. The RAE system is capable of sampling 17 channels simultaneously at up to 1 MHz with better than 10-bit accuracy. The analogue-to-digital storage modules have a capacity of 256K samples per channel and can be partitioned into segments which allow the capture of data sampled to a once-per-revolution trigger signal. This trigger pulse was generated using an inductive probe to monitor the passing of a ferrite tipped rotor 2 blade. On receipt of the first pulse, the recorder is switched on to record the passing of a predetermined number of blade passages and the data stored in the first memory segment. After a complete rotor revolution, the second trigger pulse initiates sampling of the same blade passages, and the data stored in the second memory segment. This continues until the memory is full. The data are then downloaded to the micro-computer where they are processed on-line, to yield the periodic and random fluctuations within the pressure signals and subsequently stored on disc. The equations used to derive these parameters are given in the Appendix. The signals were captured at a 1 MHz sample rate which allowed 115 samples per rotor 0 passage and 85 per rotor 2 passage. Typically records of 512µS duration were captured on receipt of each trigger pulse and the data base built up over 128 consecutive rotor revolutions. Table 2 details the number of blade passages covered by each 512µS data set and also indicates the radial extent of the measurements and the type of probe used (ie, ‘B-screen’ or silastomer rubber coated). Continuous instantaneous data records were also captured typically recording 2 complete rotor revolutions. These were subsequently subjected to spectral analysis.

<p>| Table 2 |
| Radial and circumferential extent of the rotor exit measurements |</p>
<table>
<thead>
<tr>
<th>Rotor 0</th>
<th>Rotor 1</th>
<th>Rotor 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. of radial measurements</td>
<td>16</td>
<td>16</td>
</tr>
<tr>
<td>Measurement nearest tip (% span)</td>
<td>97.1</td>
<td>98.6</td>
</tr>
<tr>
<td>Measurement nearest hub (% span)</td>
<td>2.7</td>
<td>6.9</td>
</tr>
<tr>
<td>No. of rotor blade passages recorded</td>
<td>4.3</td>
<td>5.4</td>
</tr>
<tr>
<td>Transducer type used</td>
<td>'B-screen' &amp; silastomer coated</td>
<td>'B-screen' coated</td>
</tr>
</tbody>
</table>
TEST RESULTS

Time Averaged Total Pressure Measurements

Fig 5 illustrates the spanwise variation of time-averaged total pressure measured at exit from rotor 0 while operating at peak efficiency (point B). The data are expressed as a ratio of total pressure at compressor inlet. The results contain an indication of the extent of absolute pressure uncertainty due to 'calibration drift'. This corresponds to ±2.7% of reading behind rotor 0, ±0.8% behind rotor 1 and ±1.1% behind rotor 2. These figures could have been reduced by carrying out more frequent calibrations. Fig 5a and 5b show that agreement between the transducer and adjacent Pitot measurements is within 2% behind rotors 0 and 1 respectively.

In addition to this encouraging quantitative agreement, the profiles are in excellent qualitative agreement. Because the adjacent Pitot is far less sensitive to yaw angle than the transducer, it may be concluded that no significant errors were incurred in the transducer measurements through traversing at a fixed yaw angle. Unfortunately no adjacent Pitot measurements were taken at peak efficiency operation behind rotor 2. However, those taken behind rotor 2 at near choke flow and near surge were found to agree with the transducer results to within 0.5%. Pneumatic measurements were also taken using Pitot tubes mounted on the stator blades. At peak efficiency operation only those at rotor 1 and rotor 2 exit were available. Figs 5b and 5c show that agreement with the transducer data is less satisfactory than the adjacent Pitot measurements, especially away from mid-span. However, it should be noted that these two measurements were not made in the same meridional plane and hence not in the same position relative to upstream stator wakes and other blade row interference effects. While overall agreement between the transducer and pneumatic measurements is encouraging and instills confidence in the temperature error compensation system, it must be borne in mind that the pneumatic measurements are subject to uncertainty due to possible averaging effects in the transmission lines. These are difficult to quantify accurately. Hence the transducer measurements are further compared with predictions arising from throughflow analysis. This shows that agreement to within 1.75% is found behind rotor 0 and rotor 2 at mid-span. Agreement behind rotor 1 is within 2.75%.

It is interesting to note the development of the extent of the annulus wall flows. At the tip, significant total pressure deficit (associated with the endwall boundary layer and overlap tip leakage flow) is noted behind 95% span in the rotor 0 measurements. In the rotor 1 and 2 measurements dynamic head decrease begins at 90% and 82% span respectively. At the hub however, rather than the expected fall in total pressure within the hub-annulus boundary layer, it is observed to increase. This is thought to be a consequence of kinetic energy imparted to the fluid by the rotating endwall.

Rotor Exit Unsteadiness

Fig 6 shows the instantaneous total pressure fluctuations measured behind rotor 0 at peak efficiency operation (point B). Data at three radii are illustrated, i.e., near the hub (38% span), at mid-span (51% span), and near the tip (86% span). Included in the same figure are measurements reproduced from Ng & Epstein (1985) taken at the same spanwise stations behind a NASA Lewis transonic fan. The NASA rotor is fully transonic with inlet relative Mach numbers varying between 0.75 and 1.35 from hub-to-tip while C147 rotor 0 inlet relative Mach number varies from 0.79 at the hub to 0.94 at the tip at 95% speed. Despite the difference in shock system strength between the two rotors, the instantaneous pressure measurements are remarkably similar in qualitative appearance. That is, at the hub, the blade wakes are clearly visible as strong absolute total pressure deficits while their strength diminishes with increasing span. Most striking are the pressure oscillations in the inviscid core flow. These are noted in both rotor flows and are characterised by a frequency three or four times that of blade passing. Spectral analysis of the C147 rotor 0 data confirm that the oscillations are primarily second and third harmonics of rotor 0 blade passing. No frequencies that could be attributed to downstream rotors are evident. In the NASA rotor they were seen to increase in amplitude by a factor of two in moving from hub to tip. In the C147 case, although they appear more significant because of the decrease in wake total pressure deficit, the intra-passage oscillations are of similar amplitude over much of the blade span. Quantitatively the strength of the intra-passage oscillations represents 6% of the NASA rotor total pressure ratio at the tip and 4% at mid-span. The C147 intra-passage oscillations represent 4-5% of rotor total pressure ratio.
Fig. 7 Phase-locked average total pressure ratio and random unsteadiness measurements taken behind C147 rotor 0 at peak efficiency operation.

The effects of compressor operating point and bladerow interaction

In the previous discussion, the phase-locked average (ie, periodic) and random unsteady pressure fluctuations were presented as single pressure-time traces. However, while this form of presentation lends itself to detailed consideration of the measurements it does not provide a convenient way of assessing the overall flowfield. Hence, the data have been further processed to provide a pictorial representation of the flowfield variation with span. The random unsteadiness field provides a convenient tool with which to assess the salient features and spatial extent of the viscous flowfield and as such will be considered first. The phase-locked average field will then be discussed. It should be noted that the phase-locked average pressure field must be interpreted carefully because the pressure variations depicted represent absolute total pressure variations while it is intuitive to think in terms of the rotor relative field during their interpretation. Consequently these data are somewhat limited in the information they can provide concerning the aerodynamic performance of the associated rotor. This underlines the need to employ probes capable of measuring unsteady flow angle variation, with which it would be possible to transpose the measurements to the rotor relative field. To this end, RAE have procured two dynamic yawmeters of the type described by Cock (1989). These will permit measurement of unsteady tangential flow angle.

In the previous discussion, the phase-locked average field will be considered first. The phase-locked average field provides a convenient tool with which to assess the salient features and spatial extent of the viscous flowfield and as such will play an important role in future work at RAE.

The effects of compressor operating point on the viscous field, manifest in the random unsteadiness data, are shown in Figs 8 and 9 where measurements taken at near choke flow (A) and near surge (C) behind all three rotors are presented respectively. Data taken at peak efficiency (B) have been excluded for brevity although it should be pointed out that these measurements bear close qualitative agreement to those at near choke flow. The random unsteady fluctuations in Figs 8 and 9 are quantified as a percentage of local rotor exit total pressure.

It can be seen from Fig 8 that the random unsteady flowfield recorded behind all three rotors at near choke flow exhibit strong similarities. The flow is repeatable from one passage to another and is characterised by three regions: (1) an inviscid intra-blade core flow, (2) 2D-type blade wakes away from the endwalls, (3) regions of vortical activity in the hub endwall-wake area and towards the tip casing. The vortical activity toward the hub is thought to indicate separation of the suction surface/endwall boundary layer due to low momentum fluid in the endwall boundary layer being swept into the endwall-corner under the action of the cross passage pressure gradient. The extent of these features bears close similarity to high loss regions measured behind low-speed rotors by Dring et al (1982), Lakshminarayana et al (1985) and by Dong et al (1987). The measurements shown in Fig 8 indicate that these features are offset slightly to the pressure surface side of the 2D wake flow; this is probably a consequence of different amounts of underturning within the endwall-corner separation relative to that in the 2D wake and the fact that the measurements were taken some way downstream of the rotor trailing edge (see Table 1). It is interesting to note that the spatial extent of these features increases within successive rotors. At the blade tip, the regions of high random unsteadiness appear to be positioned towards the pressure surface side of the nearest blade wakes. However, the blade tip clearance levels measured during the test series indicated tip-gaps of the order of 1% span which is not consistent with the existence of large scraping vortices (Inoue & Kuromaru (1989)). Rather, it is thought that the observed vortical flow is due to tip clearance flow and that the observed spatial position, relative to the 2D-type wake, is a consequence of cross passage migration and the fact that the measurements were taken downstream of the rotor trailing edge. Indeed, this is borne out by measurements (not presented in this paper) of the unsteady...
static pressure field over C147 rotor 0 in which it was possible to trace cross passage migration of the tip clearance flow consistent with the above observations.

Attention is now turned to the near surge data (C) shown in Fig. 9. While increasing compressor pressure ratio from point A to B (not illustrated in this paper) was accompanied by very little change in the qualitative and quantitative extent of the random unsteady flowfields, the change in moving from point B to C is marked. Behind rotor 0, the previously unadulterated core flow (Fig 8a and 9a), is now characterised by markedly higher levels of unsteadiness particularly between 50% span and the tip. Also, the rotor 0 blade wakes are seen to thicken (to 20-25% pitch compared with 10-15% at lower pressure ratios). In addition, the wake flow is not so readily characterised by the distinct coexistence of hub-endwall corner separation and 2D-type wakes, the former being notably less in evidence. Similar behaviour has been observed in measurements taken behind a low-speed compressor rotor operating at different pressure ratios by Dring et al (1982).

The corresponding near surge data for rotors 1 and 2 become progressively more complex due to the effect of upstream blade wakes. In the rotor 1 measurements (Fig 9b) it is possible to attribute the most influential upstream wakes to rotor 0 through consideration of their pitch and orientation, although chopped stator 0 wakes are also visible. That the major upstream blade row influence, other than that of rotor 1, originates from rotor 0 was also confirmed by spectral analysis of the instantaneous data. This indicated a strong fundamental rotor 0 blade passing frequency component. Because of the different number of rotor 0 and rotor 1 blades (79 and 97 respectively) some of the rotor 0 wakes pass unimpeded through the rotor 1 passages whereas others impinge upon, or pass close to, the rotor 1 blades themselves. Where close proximity occurs the rotor 1 unsteadiness is augmented, particularly in the endwall corner separation. As this phenomenon is related to the number of blades in each row, a cyclic “waxing and waning” of the rotor 1 unsteadiness is set up about the annulus which in this case is locked to the rotating reference frame. Detailed examination of the data reveals maximum endwall-corner separation unsteadiness levels are attained every 6 to 7 rotor 1 blades. This is commensurate with rotor-rotor interaction between stages 0 and 1.

Examination of the rotor 2 field (Fig 9c) reveals that a number of upstream blade wakes are evident. Spectral analysis of instantaneous data reveals that the most influential upstream influences are rotor 0 and rotor 1. However, whereas it was quite possible to arrive at the same conclusion through subjective examination of the rotor 1 field, this is not possible for rotor 2 due to the complexity of the data. The progressive increase in complexity of the rotor exit field is commensurate with the attention being shifted to more embedded rotor flows. Fig 10 presents the circumferentially
averaged variation of random unsteadiness with span for the rotor exit flows at the three operating points. These data reinforce the trends already noted in the discussion of Figs 8 and 9. That is: (1) the level of random unsteadiness rises within successive rotor flows at the same operating point, (2) increasing compressor pressure ratio (ie rotor loading) increases the intensity of the random unsteady field. However, the increase in intensity of the random unsteady field becomes more marked as compressor surge is approached.

Fig. 10 Time-averaged random unsteadiness measured behind rotors 0, 1 and 2.

Attention is now turned to the ac-coupled phase-locked average (periodic) pressure field. Qualitatively the appearance of the data did not change dramatically with operating condition as observed for the random unsteadiness data. Hence, only the near surge (point C) data are presented in Fig 11 where they are quantified as a percentage of local time-averaged total pressure at rotor exit. However, while the data at different operating points were qualitatively similar, their quantitative extent (particularly behind the embedded rotors) did change.

From Fig 11a it can be seen that the excess total pressure oscillations, noted previously in Figs 6 and 7, dominate the rotor 0 intra-passage flowfield. Further, these features are aligned radially to form coherent structures extending over much of the blade span. However, they are particularly apparent in the lower half of the annulus. The quantitative extent of the range of maximum to minimum pressures encountered in the flowfield is similar to the three operating conditions. That is, for the rotor 0 measurements illustrated in Fig 11a, they range between +5.5% and -11.0% while figures of +6.5% to -14.1% and +6.8% to -10.9% were recorded at near maximum flow and peak efficiency operation. The rotor 1 and 2 periodic flowfields are significantly different from the rotor 0 data in their appearance. While the rotor 0 field is quantitatively repeatable from one passage to another this is not so behind rotors 1 and 2. That is, although radially aligned intra-passage total pressure excess regions are seen behind rotors 1 and 2 the flow is dominated by localised pressure excess regions. These are found towards the tip in the rotor 1 field and at both hub and tip behind rotor 2. The strength of these features is not repeatable from one passage to another. Rather, their intensity "wax and wane" over a wavelength consistent with the rotor-rotor interaction observed in the random unsteadiness data described earlier. The peak pressures attained in these regions equate to 9.9% and 10.6% of the local time-averaged total pressures encountered behind rotor 1 and rotor 2 respectively. These peak pressure levels were noted to increase significantly with increasing compressor pressure ratio. That is, the peak pressure excess levels in the rotor 1 field increase by 18% in moving from choke flow to near surge. Similarly a 24% increase accompanies the movement from choke flow to near surge operation behind rotor 2. Of course in the absence of unsteady flow angle measurements it is difficult to ascertain to what extent these absolute total pressure excess regions are manifestations of relative flow angle or relative total pressure fluctuations. However, it is interesting to note that in the rotor 1 measurements the strongest total pressure excess regions in the phase-locked average field were found in the same blade passages that contained the most vigorous hub-corner vortical activity as measured in the random unsteadiness field.

Fig. 11 AC-coupled phase-locked average total pressure expressed as a percentage of local time-averaged total pressure. All of the measurements were taken at near surge operation.

CONCLUSIONS

A high frequency response total pressure probe has been traversed behind the first three rotors of a high-speed five stage core compressor (C147). Measurements were taken at maximum flow, peak efficiency, and near surge operation at 95% speed. Major conclusions resulting from the work are outlined below.

1. A reliable, and easily implemented approach to correcting semi-conductor transducer temperature errors has been applied successfully. Comparisons between transducer
REFERENCES


APPENDIX: PROCESSING OF THE PHASE-LOCKED DATA

The multiple instantaneous records captured in respose to the once-per-revolution trigger pulse were processed in the following manner to determine the periodic (phase-locked average) and random fluctuations within the pressure transducer signals.

a. The phase-locked average $V(t)$ is defined as the sum of the individual instantaneous data records measured over the number of rotor revolutions (or instantaneous data records) recorded, ie

$$V(t) = \frac{1}{N} \sum_{k=1}^{N} V_k(t)$$

where $V_k(t) =$ instantaneous data values

$N =$ number of rotor revolutions

b. The random unsteadiness $V_r(t)$ is determined by comparing each instantaneous data trace with the phase-locked average trace, squaring the difference between the two traces, summing and mean over $N$ revolutions, and finally dividing by the time-averaged dc component of the phase-locked average $V(t)$ ie,

$$V_r(t) = \sqrt{\frac{1}{N} \sum_{k=1}^{N} [V_k(t) - V(t)]^2}$$

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