Robust model for estimating pumping station characteristics and sewer flows from standard pumping station data

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ABSTRACT

Flow data represent crucial input for reliable diagnostics of sewer functions and identification of potential problems such as unwanted inflow and infiltration. Flow estimates from pumping stations, which are an integral part of most separate sewer systems, might help in this regard. A robust model and an associated optimization procedure is proposed for estimating inflow to a pumping station using only registered water levels in the pump sump and power consumption. The model was successfully tested on one month of data from a single upstream station. The model is suitable for identification of pump capacity and volume thresholds for switching the pump on and off. These are parameters which are required for flow estimation during periods with high inflows or during periods with flow conditions triggering pump switching on and off at frequencies close to the temporal resolution of monitored data. The model is, however, sensitive within the transition states between emptying and filling to observation errors in volume and on inflow/outflow variability.

Key words | flow estimation, level data, power consumption, pumping station, urban hydrology

INTRODUCTION

An efficient planning and evaluation of rehabilitation/replacement actions in sewer systems requires long-term flow data (Staufer et al. 2012); however, such data are often not available as flow monitoring is challenging and often costly in the harsh conditions occurring in sewers. Level sensors are more widespread in the systems, since they are cheaper and require less maintenance. For this reason, flow is often computed indirectly from level observations at, for example, overflow structures where the local hydraulic properties of the system allow for it (Isel et al. 2014; Ahm et al. 2016; Borup et al. 2016). Level sensors are also usually installed in pumping stations, and using data from these to compute reliable flow estimates will potentially facilitate better analysis and control of sewer systems (Carstensen et al. 1996; Löwe et al. 2016). Pumping stations consist of a pump sump (wet well) that collects wastewater inflow and a pump. The pumping is controlled by simple control rules, especially in smaller systems. The pump switches on when the pump sump is filled to some predefined level and then switches off again when the pump sump has been emptied. Pumping stations are often equipped with two (or more) pumps. This enables to increase the pump capacity during higher inflow rates and it increases the life span of the system as pumps usually alternate after each pumping cycle during low-flow conditions. The pump redundancy also enables maintaining one pump while operating the pumping station with a second pump and increases the resilience of the whole system against complete failure.

Pump sumps are usually equipped with level gauges which measure water level in the pump sump. Furthermore, the electrical power consumption of the pump is measured. These data are primarily intended for pumping control and diagnostics and can be accessed through a SCADA system (Olsson et al. 2005). They also represent valuable sources of proxy flow data, as the average inflow into the pump sump within the time step $\Delta t$ can be estimated as:

$$Q_{in} = (\Delta V(h) + Qp \times Tp)/\Delta t$$

(1)

where $\Delta V$ is the change of water volume in the pump sump, which is a function of measured water level $h$ given by the pump sump geometry, $Qp$ is the pump capacity and $Tp$ is the duration of pumping (time when the pump is on). However, pumping stations are not primarily optimized
for flow monitoring and data are often collected with insufficient temporal resolution. Thus, exact times of pumping are often unknown as well as the exact pump capacity and control rules which govern the switching of the pump on and off. This causes uncertainties in inflow estimation during high flow rates when the pump is constantly running for a long period or during flow conditions, triggering pump switching on and off at frequencies close to the temporal resolution of monitored data. Independent flow observations would obviously be beneficial, but such data redundancy is very rare in the water sector, and making use of whatever non-ideal data from pumping stations that is available can be a first step before further investments in data acquisition for flow estimation are made.

In this article, we suggest a pumping station inflow model with pump capacity and control rules as model parameters (we further refer to these parameters as pumping station characteristics). Furthermore, we propose a procedure to fit the model using pumping station data only. This enables us to estimate the pump capacity as well as the control rules, i.e. parameters needed for reliable pump sump inflow estimation during periods with high flows. The proposed methodology in its current form assumes constant pump capacity and is therefore only suitable for pump sumps where the pump capacity can be regarded as being independent from the water level in the pump sump.

 MATERIAL AND METHODS

Taarnby catchment – data specification

The pumping station used in this study is a part of a combined sewer system in a small urban catchment located in the coastal town Taarnby, Denmark (Figure 1, left) and characterized by flat terrain with altitudes not exceeding 10 m above sea level. The pumping station serves a sub-catchment with approximately 400 inhabitants and a pipe length of about 2 km. The volume of the pump sump is 24 m³, but it is mostly operated within the approximate range 2–5 m³ (Figure 1, right). The pumping station has a duplex pumping system with two pumps, each having a nominal pump capacity 9 L/s. The pumps alternate after each pumping cycle during dry weather flows and run simultaneously when the inflow rate into the pump sump exceeds the capacity of a single pump. In this investigation, we concentrate on dry weather flows and do not distinguish between the two pumps, implicitly assuming the pumps have the same characteristics.

The exact pumping capacity and level respective of volume thresholds for switching the pump on and off are unknown. Level data and electrical power consumption data are sampled at irregular time steps of Δt ≈ 5 min. One month of observations from May to June 2017 is used for...
this study. This period was characterised by dry weather with only very few light rain events.

**Pumping station inflow model**

The pumping station inflow model should be capable of estimating flow from pump sump data during both filling (no pumping) and emptying periods (pumping). Figure 2 (left) shows a time series of volume and electrical power consumption observations during dry weather. The pump sump is being filled for about five time steps (≈25 min) and emptied within one or two time steps (5–7 min). A positive electrical power consumption indicates times when the pump is on. The state of the pump between these records is however not known and the exact time of pumping is thus unknown as well. For example, the first pumping on the figure could last only 5 min from 18:30 to 18:35, but also almost 15 min from any time after 18:25 (last record with no pumping) to any time before 18:40 (first record with no pumping). We combine the electric power consumption data (l) and volume data (V) from consecutive time steps k and k-1 to estimate the exact pumping times. For this, four pump states (A–D) are defined (Figure 2):

- A: pump sump filling: \( I_{k-1} = I_k = 0 \)
- B: transition between filling and emptying period: \( I_{k-1} = 0 \land I_k > 0 \)
- C: pump sump emptying: \( I_{k-1} > 0 \land I_k > 0 \)
- D: transition between emptying and filling period: \( I_{k-1} > 0 \land I_k = 0 \)

The pumping times (\( T_p \)) within state A equal zero and within state C equal the time step size \( \Delta t \). The pumping times within state B are estimated from volume data assuming constant inflow \( Q_{in} \) during the time step \( \Delta t_k \) (Figure 2, right). The period before the threshold \( V_{max} \) is reached (\( T_{f k} \)) and the period the pump is on (\( T_{p k} \)) can then be expressed as follows:

\[
T_{f k} = (V_{max} - V_{k-1})/Q_{in}
\]

\[
T_{p k} = (V_{max} - V_k)/(Qp - Q_{in})
\]

where \( V_{k-1} \) is the last volume record when the pump was off, \( V_k \) the first record with pump being on and thus labelled as B, and \( Qp \) is the pump capacity.

Similarly, the pumping time during state D is estimated by expressing the period during pumping (\( T_{p k} \)) and after it has stopped (\( T_{f k} \)) using the volume threshold \( V_{min} \):

\[
T_{p k} = (V_{k-1} - V_{min})/(Qp - Q_{in})
\]

\[
T_{f k} = (V_k - V_{min})/Q_{in}
\]

**Parameter estimation**

The pump capacity \( Qp \) and volume thresholds \( V_{max} \) and \( V_{min} \) are regarded as model parameters and are considered
constant. The model assumption of constant pump capacity is a simplification which is further discussed in the discussion section. The model is fitted to the inflow \( Q_{inA} \) estimated during state A using Equation (1) and considered constant during subsequent states B–D. The assumption of constant inflow is discussed in the Discussion section. The three parameters are optimized separately. The pump capacity \( Q_p \) is optimized by minimizing the cost function \( L_{Qp} \):

\[
L_{Qp} = \sum_{k \in C} |Q_{inA} - Q_{inC_k}|
\]

where \( Q_{inA} \) is the inflow estimated from Equation (1) during the state C. The \( V_{max} \) threshold is optimized for state B by minimizing the cost function \( L_{V_{max}} \):

\[
L_{V_{max}} = \sum_{k \in B} |\Delta k - \bar{\Delta}k|
\]

where \( \Delta k \) is the observed duration of time step \( k \), i.e. the time difference between two consecutive records, and \( \bar{\Delta}k \) is the duration of time step \( k \) estimated as:

\[
\bar{\Delta}k = Tp_k + Tf_k
\]

where \( Tp_k \) and \( Tf_k \) are obtained from Equations (2) and (3). The \( V_{min} \) threshold is optimized similarly as for \( V_{max} \) by minimizing the cost function \( L_{V_{min}} \) defined for state D:

\[
L_{V_{min}} = \sum_{k \in D} |\Delta k - \bar{\Delta}k|
\]

where \( \Delta k \) is calculated according to Equation (8) using \( Tp_k \) and \( Tf_k \) obtained from (4) and (5). The optimization is performed by a combination of golden section search and successive parabolic interpolation (Brent 1973) implemented in the optimize() function available within the statistical computing language R (R Core Team 2017).

Results

The model was first optimized for the whole experimental period. Figure 3 shows the parameter space of pump capacity \( Q_p \) evaluated for states C and volume thresholds \( V_{max} \) and \( V_{min} \) evaluated for states B and D. All the parameters converge to well-defined minima.

The optimal value for pump capacity was found to be 8.6 L/s, which is close to the nominal pump capacity. The maximal and minimal volume thresholds for switching the pump on and off were found to be 4.72 m\(^3\) and 2.27 m\(^3\). The volumes observed at the beginning of transition time steps classified as B (i.e. during which pumping started) and D (i.e. during which pumping stopped) are shown in Figure 4. The \( V_{max} \) threshold corresponds to the 95.4% quantile of observed volumes for state B and the \( V_{min} \) threshold to the 1.7% quantile for state D. The range is estimated by inaccuracies of the level control float switches of the pump on and off, or by observation errors. The maximal volume observed (4.86 m\(^3\)) corresponds...
to a water level 2.2 cm above the estimated \( V_{\text{max}} \) threshold and the minimal observed volume (2.16 m\(^3\)) corresponds to a water level 1.7 cm below the estimated \( V_{\text{min}} \) threshold.

The total inflow volume \( V_{\text{in}} \) is 4,867 m\(^3\), and the pumped volume \( V_p \) is 4,957 m\(^3\), i.e. 1.8\% higher. The pumped volume estimated without the pumping model (Equations (2)–(5)) is 5,731 m\(^3\), i.e. 17.7\% larger than \( V_{\text{in}} \). The close match of \( V_{\text{in}} \) and \( V_p \) indicates that the suggested model and optimization procedure is conceptually correct and improve the description of the pumping process when pumping data have low temporal resolution.

The parameter obtained for daily subsets vary noticeably although their mean is almost identical with the parameter values obtained for the whole dataset (difference does not exceed 0.1\%). The standard deviation in pump capacity \( (Q_p) \) is 0.39 L/s, and in \( V_{\text{max}} \) as well as in \( V_{\text{min}} \) it is 0.06 m\(^3\). The magnitude of the estimated parameters is clearly dependent on the inflow rates estimated for daily data subsets (Figure 5). The link between the mean daily inflow and the pump capacity is relatively mild (Pearson’s \( r = 0.35 \)), whereas the \( V_{\text{max}} \) and \( V_{\text{min}} \) magnitudes are strongly linked to daily inflows having Pearson’s correlation coefficients 0.91 and –0.93, respectively. The dependence of the estimated parameters on the average inflows may partly reflect the behaviour of the real system, but it is more likely due to estimation procedure and the assumptions behind it, such as the constant pumping rate.

**DISCUSSION**

The suggested procedure is suitable for estimating pumping station characteristics; however, inflows estimated during states B and D are sensitive to the observation errors in volume, the inflow variability and also the possible outflow (pumping rate) variability. The violation of the assumption of constant inflow and constant pumping rate during emptying periods does, however, not substantially influence the estimated pumping station characteristics when the variability in inflow/outflow is random.
The variability of inflows is random in case of upstream pumps, nevertheless, our further investigations (not presented here) revealed that this does not always hold for downstream pumps. In the specific case where downstream pumping is triggered by short pulses of high flows from upstream pumps, the inflow rates during the last time step before pumping can be substantially larger than the average inflow rates during pumping. Such systematic deviation then influences the estimated pump capacity and thus makes the estimated flows more uncertain. To take such effects into account the model would have to be extended. A probabilistic formulation of inflow might improve the results as demonstrated, for example by (Leonhardt et al. 2014), on a combined sewer overflow structure with a storage tank. Reformulating the model into a stochastic grey-box (state space) model (Juhl et al. 2016) may be another feasible approach to describe uncertainties in inflow.

The violation of the assumption of constant pump capacity may systematically influence the parameter estimates. The pump capacity in reality depends also on the total hydraulic head, which is lower for higher water levels. The difference in water levels for the \( V_{min} \) and \( V_{max} \) thresholds is, in our case, only approximately 40 cm, nevertheless, pressure heads for pumping stations in flat terrains are typically only a few meters and thus even a relatively small change in hydraulic head may influence the pump capacity noticeably. The pump capacity is estimated for state C, during which the water levels are lower than during state B and, on the other hand, higher than during state D. The underestimated pump capacity during state B results in an overestimated \( V_{max} \) threshold. This overestimation is more pronounced during periods of higher inflow rates where emptying of the pump sump is slower and thus water levels at the end of state B are on average higher than during periods of lower inflow rates. In contrast, overestimation of the pump capacity during state D results in underestimated of \( V_{min} \) threshold and this underestimation is more pronounced for lower inflow rates. This could explain the strong link between the estimated \( V_{min} \) and \( V_{max} \) thresholds and the average daily inflow rates. The extension of the model to consider pump pressure head, as for example Carstensen & Harremoës (1999) did in their model of a storage tunnel, may further improve the description of pumping and thus also the reliability of the estimated pumping station characteristics and the estimated inflows. Such extension will, however, require data of higher temporal resolution to be able to identify further parameters describing the relation between pump capacity and water level in the pump sump.

The absence of independent flow measurements does not enable us to draw conclusion on the exact accuracy of the proposed method. The indirect evaluation of the model including the estimated pumping station characteristics using the inflow/outflow balance is here based on estimated pumping times and pump capacity. Total pumping times are often monitored together with the total electrical consumption for the purpose of pump diagnosis and might therefore also be used for indirect evaluation of a model like the one proposed here. We did not, however, have access to such data for the current study.

Leaky or defect non-return valves is a frequently occurring phenomenon in pump sumps and this can result in a substantial amount of pumped water flowing back into the pump sump after a pumping cycle. This does not affect the proposed methods’ ability to estimate pump sump characteristics, since the method does not distinguish between the sources of inflowing water. It does, however, affect the interpretation of the inflow time series obtained using the method since the estimated inflow in that case represents both return flow and water entering the right way into the pump sump.

Further work on validating the method and extending it to pumping stations in series may benefit from an improved dataset including (i) total pumping time and electricity

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**Figure 5** | Pump capacity (left) and volume thresholds (centre, right) found for daily subsets and compared to average daily inflows. Linear trend lines show relations between average daily inflows \( Q_{in} \) and the estimated parameter values.
consumption for each of the two pumps in a pumping station, (ii) level and electrical power consumption data recorded at a sufficiently high resolution to identify the pump switching more exactly as well as any systematically increased flows just after pumping that may indicate defect non-return valves, and (iii) direct flow observations allowing the results to be independently confirmed.

CONCLUSIONS

A model for inflows to pumping stations was proposed and an optimization procedure was suggested to estimate the pump capacity and volume thresholds for switching the pump on and off. The model also enables to estimate timing of the pump switching, which is often unknown due to suboptimal sampling frequency of water level and electrical power consumption data. This enables us to identify more exactly the duration of the pumping in each pumping cycle. Furthermore, a way of evaluating the performance of the model without independent flow observations was suggested. The model performance was successfully tested on one month of data from a pumping station operated within a small urban catchment with a separate sewer system in Taarnby, Denmark.

The model is suitable for estimating characteristics of upstream pumping stations which are not systematically influenced by inflow pulses from upstream pumping. Estimation of pumping station characteristics is valuable for pumping diagnostics. Reliable identification of pump sump capacity is also valuable for estimating inflows into pump sumps during periods with high flow rates when the pump is on for a long period. The model is, however, sensitive within the transition states between emptying and filling to observation errors in volume and on inflow/outflow variability. This sensitivity does not substantially influence the estimation of pumping station characteristics when the variably in inflow/outflow is random. The inflow variability can be considered random for upstream pumping stations; however, the model will require explicit consideration of upstream inflow pulses to be applicable also for downstream pumps. Further development will concentrate on considering a variable hydraulic head and a robust quantification of errors affecting the inflow estimation.

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