

Position paper – progress towards standards in integrated (aerobic) MBR modelling

C. Brepols , J. Comas , J. Harmand, M. Heran , Á. Robles , I. Rodriguez-Roda , M. V. Ruano , I. Smets  and G. Mannina 

ABSTRACT

Membrane bioreactor (MBR) models are useful tools for both design and management. The system complexity is high due to the involved number of processes which can be clustered in biological and physical ones. Literature studies are present and need to be harmonized in order to gain insights from the different studies and allow system optimization by applying a control. This position paper aims at defining the current state of the art of the main integrated MBR models reported in the literature. On the basis of a modelling review, a standardized terminology is proposed to facilitate the further development and comparison of integrated membrane fouling models for aerobic MBRs.

Key words | integrated model, MBR modelling, terminology

C. Brepols  (corresponding author)
Erttverband,
Am Erttverband 6, D 50126,
Bergheim, Germany
E-mail: christoph.brepols@erttverband.de

J. Comas 
I. Rodriguez-Roda 
Catalan Institute for Water Research (ICRA) and
Universitat de Girona (LEQUIA-UdG),
Girona, Spain

J. Harmand
LBE, INRA, Univ. Montpellier,
Narbonne, France

M. Heran 
Université Montpellier,
Montpellier, France

Á. Robles 
M. V. Ruano 
Universitat de València,
Valencia, Spain

I. Smets 
KU Leuven,
Leuven, Belgium

G. Mannina 
Engineering Department,
University of Palermo,
Palermo, Italy
and
College of Environmental Science and Engineering,
Tongji University, China

INTRODUCTION

Worldwide membrane bioreactors (MBRs) are employed for aerobic wastewater treatment in a strongly increasing number of installations and larger plant capacities (Brepols *et al.* 2017; Xiao *et al.* 2019; Mannina *et al.* 2020a). The performance of MBR processes is driven by complex interactions between biological processes, fluid (rheological) properties and membrane filtration. The nature of the membrane feed (wastewater–biomass–matrix), membrane and module characteristics and the hydrodynamic environment influence fouling behaviour by reactor set-up and load as well as numerous operating modes (Zhang *et al.* 2006). Various computational models have thus been used to describe and master unit processes of MBR operations under dynamic conditions (Fenu *et al.* 2010; Naessens *et al.* 2012a, 2012b).

Despite the efforts performed in MBR-based technology modelling, this topic has not yet fully matured and needs further work. Specifically, the research community has not yet reached a general consensus about some critical issues related to the biological and physico-chemical processes and their kinetics (e.g. kinetics of soluble microbial product (SMP) formation and degradation process, precipitation processes, biodegradability in terms of high sludge retention time or aerobic/anaerobic conditions), fouling propensities of components and, consequently, to translate them into mathematical expressions (e.g. SMP modelling, influent fractionation, etc.). Furthermore, up to now, a complete, clear and generally accepted nomenclature/terminology surrounding the MBR modelling field is still lacking. This

complicates comparisons among different models and impedes insights from previous applications.

With this position paper, the IWA Task Group (TG) on Membrane Bioreactor Modelling and Control aims at establishing a next step towards standardized MBR modelling. This paper will mainly focus on the so-called integrated MBR models which jointly take into account biological and physical (membrane filtration) processes. Modelling of the latter is often accomplished by resistance-in-series (RIS) models for membrane fouling.

Building upon previous and recent literature reviews (Chang *et al.* 2009; Naessens *et al.* 2012a, 2012b; Di Bella & Di Trapani 2019; Hamedi *et al.* 2019) a brief summary and update is given to identify current trends in MBR modelling with special regard to integrated MBR models and the temporal and spatial scale of modelling applications in research and engineering.

In the modelling of biological wastewater treatment processes, issues with ambiguous terminologies and nomenclature have been addressed previously (Corominas *et al.* 2010; Rieger *et al.* 2013). Which of these issues persist in the used MBR models is examined. Based upon the approach of Rieger *et al.* (2013) a way to provide a common and unambiguous terminology for variables, parameters and processes is proposed.

UPDATED LITERATURE REVIEW

Physico-chemical or mechanical unit operations

Various computational models have been used to describe and master (physico-chemical or mechanical) unit processes of MBR operations under dynamic conditions. Simple mechanistic approaches have been used to model energy consumption of MBRs based on heuristic rules and models of pumping and aeration energy (Verrecht *et al.* 2008). Although they can provide information on various design options, these models generally do not predict filtration performance based on membrane fouling.

Biodegradation

Activated sludge models (ASM) are well established and widely used (Langergraber *et al.* 2004; Rieger *et al.* 2013) and have been applied to simulate biomass kinetics in MBR systems (Fenu *et al.* 2010). Additional sub-processes or complementary models of different or additional biological pathways can be implemented to describe e.g. greenhouse-gas

(GHG) emissions (Mannina *et al.* 2018c; Massara *et al.* 2018; Wisniewski *et al.* 2018) and energy consumption (Grau *et al.* 2007). ASMs have also been modified to include the presence and fate of soluble microbial products (SMPs) which allegedly play an important role in membrane fouling, in so-called hybrid ASM models (Zuthi *et al.* 2012). Hybrid ASM models could also be used to model the fate of extracellular polymeric substances (EPS) or diluted organic matter.

Filtration

Different MBR models have focused on the physical aspects of the fouling process by various methods with the aim of describing several processes involved in membrane fouling. Among them, mathematical models are the most widely developed, which include empirical hydrodynamic models, conventional mass transfer and tangential filtration models, fractal permeation models, sectional resistance models and RIS models (Ng & Kim 2007; Chang *et al.* 2009; Naessens *et al.* 2012a).

Regarding the number of publications, RIS models seem to be highly popular. Based on an application of Darcy's law, non-stationary mathematical equations are used to describe the total hydraulic resistance. The filtering system (physical membrane plus internal and external fouling) is characterized by different resistance contributions, which can be correlated to local parameters (cross-flow velocity, mixed liquor suspended solids (MLSS) concentration, etc.), the resistances to filtration and the viscosity of a Newtonian fluid. Usually, fouling analysis is based on a quantification of the total resistance as the sum of different resistances-in-series, each related to a specific fouling mechanism: the so-called resistance decomposition (Di Bella & Di Trapani 2019).

When applied to MBR with activated sludge, the RIS concept should be used with caution (Chang *et al.* 2009), because the complex living suspension is not easily represented by simple addition of resistances and the additivity of components often cannot be found. Furthermore, various complementing or competing concepts on fouling phenomena in MBR have to be acknowledged (e.g.: superficial cake deposition, deep-bed fouling, complete or partial pore-clogging). The analytical detection and identification of foulants is challenging. Fouling classifications and fouling mechanisms reported in the literature highlight the diverse nature of membrane fouling: reversible, irreversible, irremovable fouling and cake layer deposition, intermediate blocking, concentration polarization, pore blocking, pore narrowing, etc. Predicting long-term filtration performance is further complicated by the applied

membrane cleaning strategies, and by the wide range of physical scales of the examined MBR systems (Drews 2010; Wang *et al.* 2014; Di Bella *et al.* 2018).

Computational fluid dynamics (CFD) modelling in the wastewater treatment (WWT) field is continuing to grow and is used to solve increasingly complex problems. CFD models have been used to describe various aspects of the MBR filtration process (Naessens *et al.* 2012b) at different scales, from entire WWTPs (Brannock *et al.* 2009) to microscopic levels (Lohaus *et al.* 2018), such as the importance of fluid dynamics for MBR fouling mitigation (Böhm *et al.* 2012; Liu *et al.* 2019) or optimization of MBR design and operation (Liu *et al.* 2018). A proposal towards good modelling practice has been described by Wicklein *et al.* (2016).

Integrated models

Combinations of hybrid models with physical filtration models (mostly RIS models) have been denoted as integrated models (Mannina *et al.* 2011; Zuthi *et al.* 2013). These models allow combined simulations of several of

the abovementioned crucial aspects that are important in MBR operations (Table 1). Currently these models seem to represent the most complete and complex level for the modelling of MBR systems, considering interactions among the different parts of the system (see Figure 1), despite their limitations.

Alternative models are based on particle size distribution (PSD). Given that the cake layer on the membrane consists of deposited particles of which the sub-micron-sized particles have a negative effect on the structure and porosity of the layer, models have been proposed that take into account the particle size distribution and its impact on cake layer build-up and the resulting membrane fouling (Lu & Hwang 1993; Yoon *et al.* 1999; Picioreanu *et al.* 2004; Broeckmann *et al.* 2006; Park *et al.* 2006; Shin *et al.* 2013; Cao *et al.* 2015). Due to the complex and somehow still unknown mechanisms for fouling development, there have also been approaches for data-driven modelling of fouling in MBRs (Araujo Pimentel *et al.* 2015; Dalmau *et al.* 2015; Ahmad Yasmin *et al.* 2017; Schmitt & Do 2017).

Table 1 | Feature comparison of selected MBR modelling studies using an integrated RIS model approach

Reference/Model features	Lee <i>et al.</i> (2002)	Wintgens <i>et al.</i> (2003)	Di Bella <i>et al.</i> (2008)	Zarragoitia-González <i>et al.</i> (2008)	Zarragoitia <i>et al.</i> (2009)	Mannina <i>et al.</i> (2011)	Sarioglu <i>et al.</i> (2012)	Zuthi <i>et al.</i> (2012)	Janus & Ulanicki (2016)	Mannina <i>et al.</i> (2018a, b)
Biological sub-model										
Biomass growth (e.g. X_{TSS})							x	x		x
ASM (SMP hybrid)	x	x	x	x	x	x			x	x
SMP	x		x	x	x	x		x		x
EPS									x	x
Process sub-models										
Process control				x					x	
Energy		x			x				x	x
Experimental set-up										
Laboratory-scale				x	x	x		x		
Pilot-scale			x		x		x			x
Full-scale		x								
Short time series (<1 week)		x					x			
Long time series (>1 week)		x	x	x	x	x	x	x		x
Calibration method										
Heuristic		x					x	x		
Stochastic (e.g. sensitivity analysis)						x		x		x

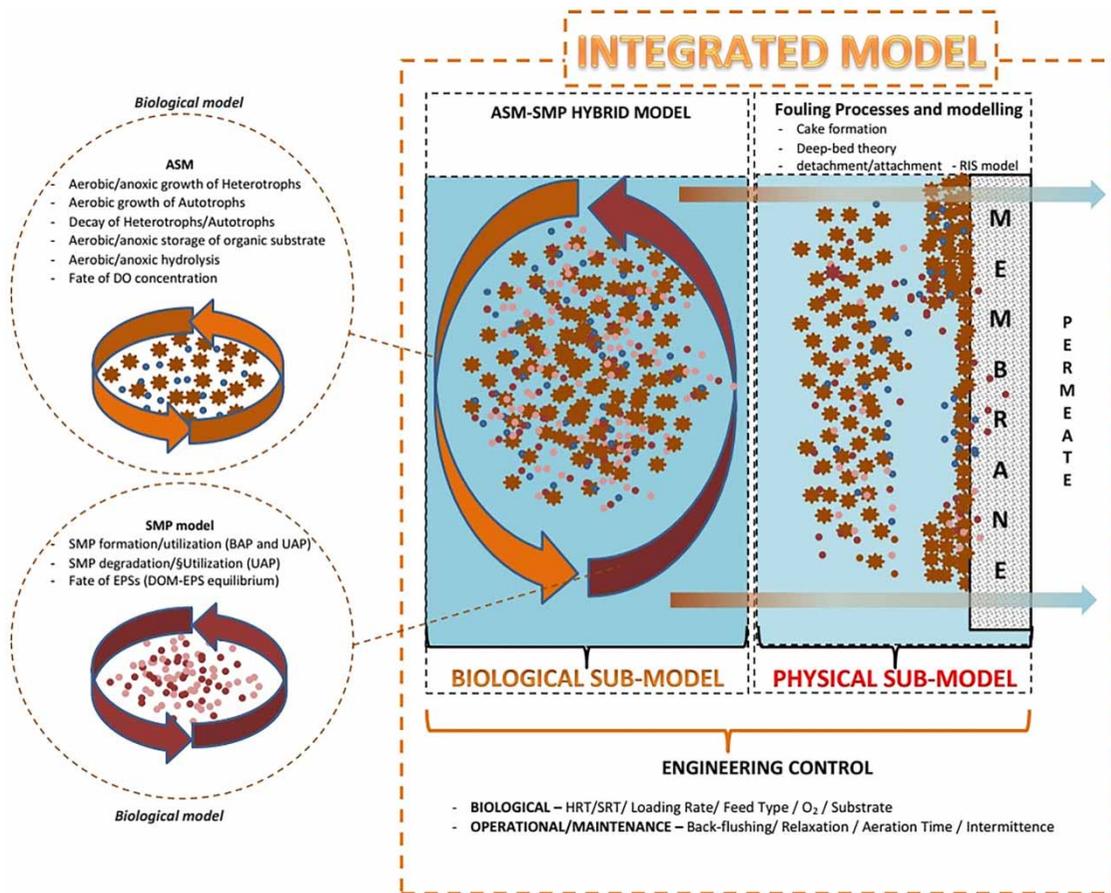


Figure 1 | Integrated approach for MBR modelling (RIS: resistance in series, HRT: hydraulic retention time, SRT: sludge retention time).

Model-based control

Several other authors have theoretically analysed and experimentally validated energy savings of different types of advanced control in aerobic MBR technology based on models or knowledge-based approaches (Drews *et al.* 2007; Ferrero *et al.* 2011, 2012; Huyskens *et al.* 2011; Monclús *et al.* 2012; Villarroel *et al.* 2013; González *et al.* 2018). Process improvements and optimized MBR control strategies (improvement of effluent quality, reduction of fouling and energy costs) can be achieved through model-based methodologies (Yusuf *et al.* 2016; Odriozola *et al.* 2017; Kalboussi *et al.* 2018). Different open-loop and closed-loop control systems have thus been developed and validated for MBRs, even at full-scale (Smith *et al.* 2006; Vargas *et al.* 2008; Vera *et al.* 2014; Mannina *et al.* 2020b). Model-based approaches are a cost-efficient means to explore operational strategies for both control of biological processes (e.g. nitrification/denitrification) and membrane filtration (Robles *et al.* 2014; Sun *et al.* 2016; Perera *et al.* 2017). Additionally, model-based

optimizations are tools in sensitivity and uncertainty analysis of the MBR process operation.

Depending on their experimental set-up, the spatial and temporal scale and the intention of their work, authors have promoted various concepts for fouling modelling or RIS aggregation (see Table 1). The abovementioned papers reveal difficulties in identifying filtration resistances, their combinations and dynamics. Model calibration methods are not likely to be documented or are carried out on constrained data-sets. Models are seldom validated on alternative set-ups or time-lines. Uncertainties in experimental set-ups, analytical methods and model assumptions are generally not evaluated or discussed (Mannina & Di Bella 2012; Mannina *et al.* 2017).

TERMINOLOGY AND NOTATION

Terminologies and notations of model parameters are a source of difficulties in comparing concepts and results across reported models. RIS models show overlaps and

inconsistencies in their model nomenclature (Di Bella & Di Trapani 2019), and terminology among these models can be ambiguous. These findings resemble the conclusions from an earlier examination of activated sludge models (Corominas *et al.* 2010; Rieger *et al.* 2013). It is thus attempted within this paper to draw outlines of a notational framework, while a full and unabridged framework description would exceed the limits of this publication. Still this draft is meant to be undemanding, distinctive, complete and flexible towards future requirements.

One group of state variables is used to describe bulk components which are relevant in the model and which are used in the mass balances of the model. When variables are derived from the biological (ASM) model it is recommended that their notational framework follows existing guidelines (Rieger *et al.* 2013). In integrated MBR models these are usually linking elements between the biological and filtration model. They can be discriminated by their nature and particle size as well as their degradability, their organic or inorganic origin, the name of the compound and other specifications. Components which are responsible for membrane fouling can be distinguished by their actual size and nature, between particulate, colloidal and soluble compounds whose definition may depend on the actual pore-size, permeation and separation characteristics of the membrane filters in use. It is thus important that particle sizes which are relevant for the underlying theories on fouling and the model are clearly specified in the model documentation. Lumped state variables which can be obtained by grouping several variables,

as e.g. the total suspended solids concentration X_{TSS} , eventually need to be discriminated from composite variables which are used to compare model data with experimental data. Table 2 exemplifies the framework. Variables can be named by their main symbol and a lineage of comma-separated subscripts.

NOTATION OF FILTRATION RESISTANCES

RIS models generally employ more or less large numbers of additive resistances which are distinguished according to the applied theories on membrane fouling. Di Bella & Di Trapani (2019) have provided a list of some of the most abundant resistances presented in the technical literature and come to the conclusion that despite many of the reported resistances having the same definition, they are identified with a different nomenclature due to the specific approach used. Furthermore, in some cases, the same nomenclature has been adopted to describe different fouling mechanisms. As a consequence, a more explicit notation is proposed to define the filtration resistance components of the model (Table 3). As examples, intrinsic membrane resistance would be denoted $R_{It,M}$ and reversible cake layer resistance depending on total suspended solids (TSS) concentration could be denoted as $R_{Rv,CL,TSS}$. Other model parameters describe physical and chemical bulk properties, like viscosity or pH-value, while other state variables describe filtration properties like flux, transmembrane pressure (TMP), and permeability. The main symbol can be used to

Table 2 | Notation of state variables describing bulk components

Main symbol Size	Subscript correction factor	Nature	Name of compound	Specifications
X – particulate	U – undegradable	Org – organic,	e.g.	e.g.
C – colloidal	B – biodegradable	Ig – inorganic	TSS	Origin, size-compartment,
S – soluble	A – abiotically convertible		EPS	sub-compound,
			SMP	valence

Table 3 | Proposed notation of subscripts for filtration resistance R in RIS models

Classification	Mechanism	Element, compound, state variable	Further specification
Intrinsic – It	Membrane – M	TSS	Origin
Irreversible – Iv	Cake layer formation – CL	EPS	Compartment
Irremovable – Im	Intermediate blocking – IB	SMP	Sub-compound
Reversible – Rv	Concentration polarization – CP		
	Pore blocking – PB		
	Pore narrowing – PN		

specify the parameter or correction factors, while a lineage of subscripts can be used to specify compound or reaction products and other specifications. Model parameters like hydrodynamic variables, rate coefficients and reduction factors require a notational frame of their own.

CONCLUSIONS AND FUTURE PERSPECTIVES

A common RIS model framework does not exist so far. The development of a mutually accepted notation framework is thus a step towards improved exchange between researchers, modellers and practitioners longing to apply MBR models. However, the outline of a notational framework as proposed here for the biodegradation-related state variables and the different resistances in the RIS-based filtration model is still a work in progress.

In accordance with previous conclusions (Naessens et al. 2012b), it can be stated also that RIS simulation studies show weaknesses regarding good modelling practice and uncertainties in MBR modelling have not been addressed systematically. Uncertainties in wastewater treatment modelling occur during all stages of model development beginning from the scope and definition of a project through data collection and reconciliation, plant model set-up, calibration and validation to simulation and interpretation of results (Belia et al. 2009). A structured discussion on the validity of MBR models and an evaluation of possible sources, locations and levels of uncertainties seem to be inevitable. The assessment of uncertainty for MBR models needs further application to better balance model complexity between biological and physical processes.

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